# Parallel Computing - Notes - v0.13.0

260236

January 2025

### Preface

Every theory section in these notes has been taken from the sources:

- Validity of the single processor approach to achieving large scale computing capabilities. [1]
- Introduction to parallel algorithms, Carnegie Mellon University. [2]
- Course slides. [3]
- Reevaluating Amdahl's law. [4]
- OpenMP by Example, Johnston Hans. [5]
- Introduction to parallel computing, volume 110. [6]
- NVIDIA Tesla: A unified graphics and computing architecture. [7]
- Structured Parallel Programming: Patterns for Efficient Computation. [8]
- The critical directive, OpenMP, Microsoft. [9]
- Multithreading Architecture. [10]
- Lecture 5, Synchronization I University of Michigan, EECS Department, Prof. Ronald Dreslinski. [11]
- Cache, Wikipedia. [12]

#### About:

**G** GitHub repository

These notes are an unofficial resource and shouldn't replace the course material or any other book on parallel computing. It is not made for commercial purposes. I've made the following notes to help me improve my knowledge and maybe it can be helpful for everyone.

As I have highlighted, a student should choose the teacher's material or a book on the topic. These notes can only be a helpful material.

## Contents

1	AM 6					
	1.1	Prerequisites				
	1.2	Definition				
	1.3	How it works				
		1.3.1 Computation				
		1.3.2 PRAM Classificiation				
		1.3.3 Strengths of PRAM 8				
		1.3.4 How to compare PRAM models				
	1.4	MVM algorithm				
	1.5	SPMD sum				
	1.6	MM algorithm				
	1.7	PRAM variants and Lemmas 17				
	1.8	PRAM implementation				
	1.9	Amdahl's and Gustafson's Laws				
<b>2</b>	Fun	damentals of architecture 23				
	2.1	Introduction				
		2.1.1 Simplest processor				
		2.1.2 Superscalar processor				
		2.1.3 Single Instruction, Multiple Data (SIMD) processor 25				
		2.1.4 Multi-Core Processor				
	2.2	Accessing Memory 26				
		2.2.1 What is a memory? $\ldots$ 26				
		2.2.2 How to reduce processor stalls				
		2.2.2.1 Cache				
		$2.2.2.2  \text{Multi-threading}  \dots  \dots  \dots  \dots  \dots  28$				
•	ъ					
3	Pro	gramming models 31				
	3.1	Implicit SPMD Program Compiler (ISPC)				
	3.2	Shared Address Space Model				
	3.3	Message Passing model of communication				
	3.4	Data-Parallel model				
1	Dar	allel Programming Models and othreads 30				
-	1 ar	How to create parallel algorithms and programs				
4.1 How to create parallel algorithms and programs.		Analyze parallel algorithms				
	4.2	Technologies				
	4.0	Threads 47				
	4.4	$\frac{1}{4} \frac{1}{4} \frac{1}{1} \frac{1}$				
		4.4.2 Definition $47$				
		4.4.2 Definition $1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.1.$				
		4431 Creation 40				
		49				
		4/3.3 Loining 51				
		$4.4.3.4  \text{Dotaching} \qquad \qquad$				
		4.4.3.5 Loining through Barriera 59				
		4.4.3.6 Mutayos				
		4.4.0.0 Multexes				
		4.4.3.7 Collution variables $\ldots \ldots \ldots \ldots 34$				

<b>5</b>	5 OpenMP v5.2		
	5.1 Introduction		
	5.2	Basic syntax	
	5.3	Work sharing	
		5.3.1 For	
		$5.3.1.1$ Reduction $\ldots \ldots 65$	
		5.3.2 Sections	
		5.3.3 Single/Master	
		5.3.4 Tasks	
		5.3.4.1 Task dependences	
	5.4	Synchronization	
	5.5	Data environment	
	5.6	Memory model	
	5.7	Nested Parallelism	
	5.8	Cancellation	
	5.9	SIMD Vectorization	
0	CD		
0	GP 6 1	Introduction 100	
	0.1	CDU compute mode	
	0.2		
	0.5	$\begin{array}{c} \text{CODA} & \dots & $	
		6.3.2 Momery model 107	
		6.3.3 NVIDIA V100 Streaming Multiprocessor (SM) 100	
		6.3.4 Bunning a CUDA program on a CPU 112	
		6.3.5 Implementation of CUDA abstractions	
		6.3.6 Advanced thread scheduling	
		6.3.7 Memory and Data Locality in Denth 126	
		6.3.8 Tiling Technique	
		6.3.8.1 Tiled Matrix Multiplication 138	
		6.3.8.2 Implementation Tiled Matrix Multiplication 143	
		6.3.8.3 Any size matrix handling 148	
		6.3.9 Optimizing Memory Coalescing	
		••••• ••••••••••••••••••••••••••••••••	
<b>7</b>	$\mathbf{CU}$	DA 162	
	7.1	Introduction	
	7.2	CUDA Basics	
		7.2.1 GPGPU Best Practices	
		7.2.2 Compilation	
		7.2.3 Debugging	
		7.2.4 CUDA Kernel	
	7.3	Execution Model	
	7.4 Querying Device Properties		
	7.5	Thread hierarchy	
	7.6	Memory hierarchy	
	7.7	Streams	
	7.8	CUDA and OpenMP or MPI 197	
		$7.8.1  \text{Motivations}  \dots  197$	
		(.8.2 UUDA API for Multi-GPUs	
		(.8.3 Memory Management with Multiple GPUs 205	

		7.8.4 Batch Processing and Cooperative Patterns with OpenMP 211
		7.8.5 OpenMP for heterogeneous architectures
		7.8.6 MPI-CUDA applications
8	Mer	mory Consistency 220
	8.1	Coherence vs Consistency
	8.2	Definition
	8.3	Sequential Consistency Model
	8.4	Memory Models with Relaxed Ordering
		8.4.1 Allowing Reads to Move Ahead of Writes
		8.4.2 Allowing writes to be reordered
		8.4.3 Allowing all reorderings
	8.5	Languages Need Memory Models Too
	8.6	Implementing Locks
		8.6.1 Introduction
		8.6.2 Test-and-Set based lock
		8.6.3 Test-and-Test-and-Set lock

### Index

### 1 PRAM

#### **1.1** Prerequisites

Before we introduce the PRAM model, we need to cover some useful topics.

- A Machine Model describes a "machine". It gives a value to the operations on the machine. It is necessary because: it makes it easy to deal with algorithms; it achieves complexity bounds; it analyses maximum parallelism.
- A Random Access Machine (RAM) is a model of computation that describes an abstract machine in the general class of register machines. Some features are:
  - Unbounded number of local memory cells;
  - Each memory cell can hold an integer of **unbounded** size;
  - Instruction set includes simple operations, data operations, comparator, branches;
  - All operations take **unit time**;
  - The definition of time complexity is the number of instructions executed;
  - The definition of space complexity is the number of memory cells used.

#### 1.2 Definition

#### Definition 1: PRAM

A parallel random-access machine (parallel RAM or PRAM) is a shared-memory abstract machine. As its name indicates, the PRAM is intended as the parallel-computing analogy to the random-access machine (RAM) (not to be confused with random-access memory). In the same way that the RAM is used by sequential-algorithm designers to model algorithmic performance (such as time complexity), the PRAM is used by parallel-algorithm designers to model parallel algorithmic performance (such as time complexity, where the number of processors assumed is typically also stated).

The PRAM model has many interesting features:

- Unbounded collection of RAM processors  $(P_0, P_1, \text{ and so on})$ ;
- Processors don't have tape;
- Each processor has **unbounded registers**;
- Unbounded collection of share memory cells;
- All processors can access all memory cells in unit time;
- All communication via shared memory.

#### 1.3 How it works

#### 1.3.1 Computation

A single **processor** of the PRAM, at each computation, is **composed of 5 phases** (carried out in parallel by all the processors):

- 1. Reads a value from one of the cells  $X(1), \ldots, X(N)$
- 2. Reads one of the shared memory cells  $A(1), A(2), \ldots$
- 3. Performs some internal computation
- 4. May write into one of the output cells  $Y(1), Y(2), \ldots$
- 5. May write into one of the shared memory cells  $A(1), A(2), \ldots$

#### 1.3.2 PRAM Classificiation

During execution, a subset of processors may remain idle. Also, some processors can read from the same cell at the same time (not really a problem), but they could also try to write to the same cell at the same time (**write conflict**). For these reasons, PRAMs are classified according to their read/write capabilities (realistic and useful):

- Exclusive Read (ER). All processors can simultaneously read from distinct memory locations.
- Exclusive Write (EW). All processors can simultaneously write to distinct memory locations.
- Concurrent Read (CR). All processors can simultaneously read from any memory location.
- Concurrent Write (CW). All processors can write to any memory location.

#### **?** But what value is ultimately written?

It depends on the mode we choose:

- Priority Concurrent Write. Processors have priority based on which value is decided, the highest priority is allowed to complete write.
- Common Concurrent Write. All processors are allowed to complete write if and only if all the value to be written are equal.
   Any algorithm for this model has to make sure that this condition is satisfied. Otherwise, the algorithm is illegal and the machine state will be undefined.
- Arbitrary/Random Concurrent Write. One randomly chosen processor is allowed to complete write.

#### 1.3.3 Strengths of PRAM

PRAM is attractive and important model for designers of parallel algorithms because:

- It is **natural**. The number of operations executed per one cycle on *P* processors is at most *P* (equal to *P* is the ideal case).
- It is **strong**. Any processor can read/write any shared memory cell in unit time.
- It is **simple**. It abstracts from any communication or synchronization overhead, which makes the complexity and correctness of PRAM algorithm easier.
- It can be used as a **benchmark**. If a problem has no feasible/efficient solution on PRAM, it has no feasible/efficient solution for any parallel machine.

#### 1.3.4 How to compare PRAM models

Consider two generic PRAMs, models A and B. Model A is computationally stronger than model B ( $A \ge B$ ) if and only if any algorithm written for model B will run unchanged on model A in the same parallel time and with the same basic properties.

However, there are some useful metrics that can be used to compare models:

• Time to solve problem of input size *n* on <u>one</u> processor, using best sequential algorithm:

$$T^{*}\left(n\right) \tag{1}$$

• Time to solve problem of input size *n* on **p** processors:

$$T_{p}\left(n\right) \tag{2}$$

• Speedup on p processors:

$$SU_p(n) = \frac{T^*(n)}{T_p(n)}$$
(3)

• Efficiency, which is the work done by a processor to solve a problem of input size *n* divided by the work done by *p* processors:

$$E_p(n) = \frac{T_1(n)}{pT_p(n)} \tag{4}$$

• Shortest run time on any process p:

$$T_{\infty}\left(n\right) \tag{5}$$

• Cost, equal to processors and time:

$$C(n) = P(n) \cdot T(n) \tag{6}$$

• Work, equal to the total number of operations:

$$W(n)$$
 (7)

Some properties on the metrics:

• The time to solve a problem of input *n* on a single processor using the best sequential algorithm *is not equal to* the time to solve a problem of input *n* in parallel using one of the *p* processors available. In other words, **the problem should not be solvable on a single processor on a parallel machine** (otherwise, what would be the point of using a parallel model?)

$$T^* \neq T_1$$

•  $SU_P \le P$ 

• 
$$\operatorname{SU}_P \leq \frac{T_1}{T_{\infty}}$$

- $E_p \leq 1$
- $T_1 \ge T^* \ge T_p \ge T_\infty$

• 
$$T^* \approx T_1 \Rightarrow E_p \approx \frac{T^*}{pT_p} = \frac{\mathrm{SU}_p}{p}$$

• 
$$E_p = \frac{T_1}{pT_p} \le \frac{T_1}{pT_\infty}$$

• 
$$T_1 \in O(C), T_p \in O\left(\frac{C}{p}\right)$$

•  $W \leq C$ 

• 
$$p \approx \text{AREA}$$
  $W \approx \text{ENERGY}$   $\frac{W}{T_p} \approx \text{POWER}$ 

#### 1.4 MVM algorithm

The Matrix-Vector Multiply (MVM) algorithm consists of four steps:

- 1. Concurrent read of vector X(1:n) (transfer N elements);
- Simultaneous reads of different sections of the general matrix A (transfer n<sup>2</sup>/p elements to each processor);
   Compute n<sup>2</sup>/p operations per processor;
- 4. Simultaneous writes (transfer  $\frac{n}{p}$  elements from each processor).

Let i be the processor index, so the MVM algorithm is simply written as:

```
GLOBAL READ (Z \leftarrow X)
GLOBAL READ (B \leftarrow A_i)
COMPUTE (W := BZ)
```

- GLOBAL WRITE (W ightarrow  $y_i$ )
- GEODAL WITTE (W  $\rightarrow g_i$ )

Algorithm 1: Matrix-Vector Multiply (MVM)



Figure 1: Example of MVM algorithm.

The performance of the MVM algorithm is as follows:

• The **time to solve** a problem of size  $n^2$  is equal to the big O of the squared size of the problem as input divided by the number of processors available:

$$T_p\left(n^2\right) = O\left(\frac{n^2}{p}\right)$$

• The **cost** is equal to the number of processors and the time it takes to solve the problem. So it is quite trivial:

$$C = O\left(\not\!\!\!P \cdot \frac{n^2}{\not\!\!\!p}\right) = O\left(n^2\right)$$

• The **work** is equal to the cost, and the **linear power** *P* is equal to the ratio of work and time to solve the problem on *p* processors:

$$W = C$$
  $\frac{W}{T_p} = P$ 

• The **perfect efficiency** is equal to:

$$E_p = \frac{T_1}{pT_p} = \frac{n^2}{p\frac{n^2}{p}} = 1$$

#### 1.5 SPMD sum

The **Single Program Multiple Data (SPMD)** is a term that has been used to **describe computational models** for exploiting parallelism, where **multiple processors work together to execute a program to get results** faster.

In this section, we will see an SPMD approach on a Parallel Random Access Machine (PRAM). We will introduce one of the most common and simple mathematical operations: the sum.

The following pseudocode takes as **input an array** of size  $n = 2^k$ . In this case, n is a power of 2 because it ensures that the array can be evenly divided at each step of the computation. The value k is the number of iterations or levels of the summation process.

```
BEGIN
 1
        GLOBAL READ (A \leftarrow A(I))
2
        GLOBAL WRITE (A \rightarrow B(I))
3
        FOR H = 1 : K
4
              IF i \leq n \div 2^h then begin
5
                   GLOBAL READ (X \leftarrow B(2i -
                                                    1))
6
                   GLOBAL READ (Y \leftarrow B(2i))
7
                   Z := X + Y
 8
                   GLOBAL WRITE (Z \rightarrow B(i))
9
              END
        IF I = 1 THEN
11
              GLOBAL WRITE (Z \rightarrow S)
12
13 END
```

Algorithm 2: Single Program Multiple Data (SPMD) sum

- First, read the entire input array A and copy the read data to another array B.
- Loop over h (1 to k). In each iteration, for each index i less than or equal to n ÷ 2<sup>h</sup>, read values from array B at positions 2i − 1 and 2i; sum these values (and store the result in Z) and store the result (Z) back into B(i).
- Once all iterations are complete, the final sum is stored in a variable S.

For example, if n = 8, then k would be 3, meaning that the algorithm will run for 3 iterations to sum all the elements in parallel.

h	i	adding
	1	1,2
1	2	$^{3,4}$
1	3	$^{5,6}$
	4	$^{7,8}$
2	1	1,2
2	2	$^{3,4}$
3	1	1,2



Figure 2: Computation of the sum of eight elements on a PRAM with eight processors. Each internal node represents a sum operation. The specific processor executing the operation is indicated below each node.

#### Performance of sum

When the size of the array is equal to the number of processors (N = P), the speedup and efficiency decrease:

- $T^*(N) = T_1(N) = N$
- $T_{N=P}(N) = 2 + \log N$
- $\operatorname{SU}_P = \frac{N}{2 + \log N}$
- $T^*(N) = P \cdot (2 + \log N) \approx N \log N$

• 
$$E_p = \frac{T_1}{pT_p} = \frac{N}{N\log N} = \frac{1}{\log N}$$



If the size of the array is much larger than the number of processors  $(N \gg P)$ , the speedup and power are linear, the cost is fixed and the efficiency is maximum (equal to 1):

- $T^*(N) = T_1(N) = N$
- $T_p(N) = \frac{N}{p} + \log p$
- $\operatorname{SU}_P = \frac{N}{\frac{N}{p} + \log p} \approx P$
- $\operatorname{COST} = p\left(\frac{N}{p} + \log p\right) \approx N$
- WORK =  $N + P \approx N$

• 
$$E_p = \frac{T_1}{pT_p} = \frac{N}{p\left(\frac{N}{p} + \log p\right)} \approx 1$$



n = 1'000'000

#### Example 1

Refer to Figure 2 (page 13), the performance metrics are:

- $T_8 = 5$
- $C = 8 \cdot 5 = 40$  (could do 40 steps)
- W = 2n = 16 (16 on 40, wasted 24)

• 
$$E_p = \frac{2}{\log n} = \frac{2}{3} = 0.67$$

• 
$$\frac{W}{C} = \frac{16}{40} = 0.4$$

There is also the **Prefix Sum**, which takes **advantage of idle processors in the sum**. It computes all prefix sums:



Figure 4: Prefix sum.

#### 1.6 MM algorithm

The Matrix Multiply (MM) algorithm consists of three steps:

1. Compute the two matrices  $A_{i,l}$  and  $B_{l,j}$ , so use the concurrent read.

2. Make the **sum**.

3. Store the result using exclusive write.



#### Performance of MM

- $T_1 = n^3$
- $T_{p=n^3} = \log n$
- $SU = \frac{n^3}{\log n}$
- $Cost = n^3 \log n$

• 
$$E_p = \frac{T_1}{pT_p} = \frac{1}{\log n}$$



#### 1.7 PRAM variants and Lemmas

The PRAM model presented here is one of the most commonly used. However, there are other important variants:

- PRAM model with a **limited number of shared memory cells** (small memory PRAM). If the input data set exceeds the capacity of the shared memory, the I/O values can be evenly distributed among the processors.
- PRAM model with **limited number of processors** (small PRAM). If the number of execution threads is higher, processors can interleave multiple threads.
- PRAM model with **limited size of one machine word**.
- PRAM model with access conflicts handling. These are restrictions on simultaneous access to shared memory cells.

**Lemma** 1. Assume P' < P and same size of shared memory. Any problem that can be solved for a P processor PRAM in T steps can be solved in a P' processor PRAM in:

$$T' = O\left(\frac{TP}{P'}\right) \tag{8}$$

*Proof.* Partition P is simulated processors into P' groups of size  $\frac{P}{P'}$  each. Associate each of the P' simulating processors with one of these groups. Each of the simulating processors simulates one step of its group of processors by:

- Executing all their read and local computation substeps first;
- Executing their write substeps then.

QED

**Lemma 2.** Assume M' < M. Any problem that can be solved for a P processor and M-cell PRAM in T steps can be solved on a max (P, M')-processors M'-cell PRAM in  $O\left(\frac{TM}{M'}\right)$  steps.

*Proof.* Partition M simulated shared memory cells into M' continuous segments S, of size  $\frac{M}{M'}$  each. Each simulating processor  $P'_I$   $(1 \le I \le P)$ , will simulate processor  $P_I$  of the original PRAM. Each simulating processor  $P'_I$   $(1 \le I \le M')$ , stores the initial contents of  $S_I$  into its local memory and will use M'[I] as an auxiliary memory cell for simulation of accesses to cell of  $S_I$ . Simulation of one original read operation:

```
1 EACH P'_{I} (I = 1, ..., \max(P, M')) REPEATS FOR K = 1, ..., \frac{M}{M'}

2 WRITE THE VALUE OF THE K-TH CELL OF S_{I} INTO M'[I] (I = 1, ..., M')

3 READ THE VALUE WHICH THE SIMULATED PROCESSOR P_{I} (I = 1, ..., P)

WOULD READ IN THIS SIMULATED SUBSTEP, IF IT APPEARED IN THE

SHARED MEMORY
```

The local computation substep of  $P_I$  (I = 1, ..., P) is simulated in one step by  $P'_I$ . SImulation of one original write operation is analogous to that of read. QED

#### **1.8 PRAM implementation**

The PRAM is an ideal model for creating parallel algorithms. Now we look at *"is it really implementable?*" The short answer is yes.

The longest answer is the following. There are already some examples of PRAM being converted to real machine models, such as Explicit Multi-Threading (XMT), Rigel, Tilera, etc. If conversion is not easy or possible, the implementation can be "direct":

- The concurrent read is implemented as a detect-and-multicast technique.
- The concurrent write is implemented depending on the end result we want to achieve. Fetch-and-operate and prefix-sum are examples of serialized writing; otherwise, the CRCW technique is used:
  - Common CRCW: detect and merge
  - Priority CRCW: detect-and-priorities
  - Arbitrary CRCW: arbitrary

#### Example 2: Boolean DNF (sum of products) common CRCW

A logical formula is considered to be in DNF if it is a disjunction of one or more conjunctions of one or more literals. Consider X as the sum of products of AND/OR operations:

$$X = a_1b_1 + a_2b_2 + \dots$$

The PRAM code, with X initialized to 0 and task index equal to , is:

if  $(a_{\$}b_{\$}) X = 1;$ 

The common result is that not all processors write X and those that do write 1. The time complexity is O(1). It works on common, priority and arbitrary CRCW.

Despite the previous example, exists also the PRAM SoP for the concurrent write. Let boolean X as:

$$X = a_1b_1 + a_2b_2 + \dots$$

The PRAM algorithm is:

if 
$$(a_i b_i) X = 1;$$

Where all cores which write into X, write the same value.

#### ✓ PRAM advantages

- Large body of algorithms.
- Easy to think about it.
- Sync version of shared memory. It eliminates sync and common issues, allows focus on algorithms, but allows adding these issues and allows conversion to async versions.
- Exists architectures for both synch (PRAM) and async (SM) model.
- PRAM algorithms can be mapped to other models.

#### 1.9 Amdahl's and Gustafson's Laws

The **Amdahl's Law** is a formula which gives the **theoretical speedup in latency of the execution of a task at fixed workload that can be expected of a system whose resources are improved**. The law can be stated as:

#### Definition 2: Amdahl's Law

The overall performance improvement gained by optimizing a single part of a system is limited by the fraction of time that the improved part is actually used.

In practice, Amdahl's law says that the computation consists of interleaved segments of two types:

1. Serial segments (which cannot be parallelized);

#### 2. Parallelizable segments.

Therefore, the metrics we can obtain are the time on P processors metric, that it is greater than the fraction of time on a processor divided by the processors P, and the speedup metric, that it is less than the number of processors P:

$$T_P > \frac{T_1}{P} \qquad SU < P$$

Graphically, we can see a fixed part of the line, which is the **serial segment** (no speedup), and a set of instructions that can be **parallelized** (the sum of these segments is equal to the unit time 1).



Furthermore, if we identify the parallelizable segment as f and the serial segment as 1 - f, we obtain the following expressions:

$$SU(P,f) = \frac{T_1}{T_P} = \frac{T_1}{T_1 \cdot (1-f) + \frac{T_1 \cdot f}{P}} = \frac{1}{(1-f) + \frac{f}{P}}$$
(9)
$$\lim_{P \to \infty} SU(P,f) = \frac{1}{1-f}$$

In the following figure we can see the speedup with parameter f. Note the pessimism: for a problem with inherent f = 90%, there is no point in using more than 10 processors.



Figure 5: Amdahl's law, SU(P), parameter f.

The original paper presenting Amdahl's Law [1] can be viewed by clicking on the link below or by scanning the QR code.

Amdahl's Law



Amdahl's law applies only to the cases where the problem size is fixed. In practice, as more computing resources become available, they tend to get used on larger problems (larger datasets), and the time spent in the parallelizable part often grows much faster than the inherently serial work. In this case, Gustafson's law gives a less pessimistic and more realistic assessment of the parallel performance. [8]

**Gustafson's Law** gives the speedup in the execution time of a task that theoretically gains from parallel computing, using a hypothetical run of the task on a single-core machine as the baseline. To put it another way, it is the **theoret**ical "slowdown" of an already parallelized task if running on a serial machine.

Against Amdahl's law, Gustafson suggests the following ideas:

- Portion f is not fixed;
- The absolute serial time is fixed;
- Parallel problem size is increased to exploit more processors;
- Fixed serial time (s of total) and fixed parallel time (1 s of total) are invariants;
- Fixed time model and not fixed size model (as Amdahl's law):

$$SU(P) = \frac{T_1}{T_P} = \frac{s + P \cdot (1 - s)}{s + (1 - s)} = s + P \cdot (1 - s)$$
(10)



Gustafson's law suggests a **linear speedup** and is **empirically applicable to** highly parallel algorithms.

Figure 6: Gustafson's law.

Amdahl's Law states that as computing power increases, computational requirements remain the same. In other words, the analysis of the same data will take less time with more computing power.

*Gustafson*, on the other hand, argues that more computing power leads to more careful and complete analysis of the data. Where it would not have been possible or practical to simulate the impact of nuclear denotation on every building, car, and their contents (including furniture, structural strength, etc.) because such a calculation would have taken more time than was available to provide an answer, the increase in computing power will prompt researchers to add more data to more fully simulate more variables, giving a more accurate result.

The original paper presenting Gustafson's Law [4] can be viewed by clicking on the link below or by scanning the QR code.

Gustafson's Law



### 2 Fundamentals of architecture

The main purpose of this chapter is to introduce some basics of parallel computing theory. It will introduce the simplest and trivial processor and the more complex and efficient variants. The topics introduced are explained in a simple way and without any deepening, because it is only an introduction. For those who have studied computer science, this chapter might be a little boring and you might notice that some topics are explained in a simplistic way.

#### 2.1 Introduction

#### 2.1.1 Simplest processor

Inside a computer, a processor executes instructions.

- Fetch/Decode: Determine which instruction to run next;
- ALU (execution unit): Performs the operation described by an instruction, which may change values in the processor's registers or the computer's memory;
- **Registers**: maintain program state, store values of variables used as inputs and outputs to operations.

The simplest and most basic processor executes **one instruction per clock** cycle.



Figure 7: The simplest and most basic processor.

#### 2.1.2 Superscalar processor

A more "complex" and realistic model is the superscalar processor. This processor can decode and execute up to two instructions per clock. The execution is slightly different from the simplest processor. The processor automatically finds independent instructions in an instruction sequence and can execute them in parallel on multiple execution units.



Figure 8: The superscalar processor.

The superscalar processor takes advantage of **Instruction-Level Parallelism**  $(ILP)^1$  within an instruction stream.

- Processing different instructions from the same instruction stream in parallel (within a core).
- Parallelism is automatically detected by the hardware during execution.

<sup>&</sup>lt;sup>1</sup>Instruction-level parallelism (ILP) is the parallel or simultaneous execution of a sequence of instructions in a computer program. More specifically ILP refers to the average number of instructions run per step of this parallel execution.

#### 2.1.3 Single Instruction, Multiple Data (SIMD) processor

Adding execution units (ALUs) to the simplest processor can increase compute capability. Amortize the cost/complexity of managing an instruction stream across many ALUs using Single Instruction, Multiple Data (SIMD) processing. Therefore, the same instruction is sent to all ALUs. This operation is performed in parallel on all ALUs.

#### ✓ Advantages

- Efficient for data-parallel workloads: amortize control costs over many ALUs.
- Vectorization done by:
  - Compiler (explicit SIMD): parallelism is explicitly requested by the programmer through intrinsics, conveyed through parallel language semantics, and inferred through loop dependency analysis by the "auto-vectorizing" compiler. In other words, the SIMD parallelization is done at compile time, and when we inspect the program binary, we can see the SIMD instructions.
  - At runtime by hardware (<u>implicit SIMD</u>): the compiler generates a binary with scalar instructions, but n instances of the program are always executed together on the processor. The hardware (not the compiler) is responsible for the simultaneous execution of the same instruction by multiple program instances on different data on SIMD ALUS.

#### 2.1.4 Multi-Core Processor

A Multi-Core Processor (MCP) is a microprocessor on a single integrated circuit (IC) with two or more separate central processing units (CPUs), called *cores* to emphasize their multiplicity (e.g., *dual-core* or *quadcore*). Each core reads and executes program instructions, specifically ordinary CPU instructions (such as add, move data, and branch). However, the MCP can execute instructions on separate cores simultaneously, increasing overall speed for programs that support multithreading or other parallel computing techniques.

#### ✓ Advantages

- Provides thread-level parallelism: execute a completely different instruction stream on each core simultaneously.
- Software creates threads to expose parallelism to hardware (e.g., via threading API)

#### 2.2 Accessing Memory

#### 2.2.1 What is a memory?

A computer's memory is organized as an array of bytes. Each byte is identified by its address in memory (its position in that array).

Address	Value
0x0	16
0x1	255
0x2	14
0x3	0
0x4	0
0x5	0
0x6	6
0x7	0
0x8	32
0x9	48
OxA	255
0xB	255
0xC	255
OxD	0
0xE	0
0xF	0
0x10	128
:	:
0x1F	0

Table 1: Example illustration of the program's memory address space of 32 bytes, range from 0x0 to 0x1F.

From the processor's point of view, loading an instruction to access the contents present in memory is done with the 1d assembly instruction. For example, 1d  $R0 \leftarrow mem[R2]$  means "take the value from register R2 and put that value into register R0".

Before we introduce new concepts, let us take a moment to explain some important **terminology**:

- Memory Access Latency, is the time it takes for the memory system to deliver data to the processor.
- Processor Stall. A processor stalls when it cannot execute the next instruction in an instruction stream because of a dependency on a previous instruction that has not been completed. Accessing memory is a major source of stalling, which is one of the main reasons why memory accesses should be limited.

For example, in the following three assembler instructions, the add has to wait for the loading of R2 and R3 values, making parallelization more complicated:

ld r0 mem[r2]
ld r1 mem[r3]
add r0, r0, r1

• Memory Bandwidth, is the rate at which the memory system can provide data to a processor.

Bandwidth is the <u>critical</u> resource in modern computing.

High-performance parallel programs will:

- 1. Organize computation to fetch data from memory less frequently. For example, reuse data previously loaded by the same thread (temporal locality optimizations) or share data across threads (inter-thread cooperation);
- 2. Prefer to perform additional arithmetic to store/reload values;
- 3. **Programs need to access memory infrequently** to take advantage of modern processors.

#### 2.2.2 How to reduce processor stalls

#### 2.2.2.1 Cache

One of the most common solutions is caching.

A cache is a hardware or software component that stores data so that future requests for that data can be served faster; the data stored in a cache might be the result of an earlier computation or a copy of data stored elsewhere.

- A Cache Hit occurs when the requested data is found in a cache;
- A Cache Miss occurs when it cannot.

Cache hits are served by reading data from the cache, which is faster than recomputing a result or reading from a slower data store, so the **more requests** that can be served from the cache, the faster the system performs. [12]

Many modern CPUs have logic that predicts what data will be accessed in the future and "pre-fetches" that data into caches. **Prefetching** reduces stalls because the data is resident in the cache when it is accessed. But beware, the other side of the coin is that if the **guess is wrong**, the **performance is worse than the system without prefetching**!

#### 2.2.2.2 Multi-threading

A Multithreaded Processor is one that has the ability to follow multiple instruction streams without software intervention. In practice, then, this includes any machine that stores multiple program counters (PCs) in hardware within the processor (i.e., on chip, for microprocessor-era machines). [10]

The main idea in this architecture is to **interleave processing of multiple threads on the same core to hide stalls**. In other words, if we can't make progress on the current thread, we work on another one.



practice, we see that a single arithmetic instruction takes 3 clock cycles and the memory stall takes 12 clock cycles. This means that from this situation we are using the CPU at only 20% (3 work clock cycles on 15)! Without suggesting the final solution, try to see what happens when we add another thread.



We have gained three clock cycles, and now we are taking advantage of the 40% of the core.

Now, how many threads do we need to achieve 100% utilization? The answer is simple: the number of clock cycles of the operations to be done before the stall plus the clock cycles of the stall divided by the working operations (operations that are not stalls). In our case:  $15 \div 3 = 5$ .



#### ✓ Multithreaded Processor benefits

- A processor with multiple hardware threads has the **ability to avoid stalls** by executing instructions from other threads when one thread must wait for a long latency operation to complete. The latency of the memory operation is not changed by multithreading, it just no longer causes reduced processor utilization.
- A multithreaded processor hides memory latency by performing

arithmetic from other threads. Program that feature more arithmetic per memory access need fewer threads to hide memory stalls.

#### Type of hardware-supported multithreading

- Core manages execution contexts for multiple threads. This type still has the same number of ALU resources: multi-threading only helps to use them more efficiently in the face of high latency operations such as memory access. The processor decides which thread to run each clock cycle.
- Coarse-Grain Multithreading, also called Block Multithreading or Switch-On-Event Multithreading, has multiple hardware contexts associated with each processor core. A hardware context is the program counter, register file, and other data required to enabled a software thread to execute on a core. However, only one hardware context has access to the pipeline at a time. [10]
- Fine-Grain Multithreading (FGMT), also known as Interleaved Multithreading or Temporal Multithreading, is the type just described on the previous pages, as in the example on page 28.
- Simultaneous Multithreading (SMT) has multiple hardware contexts associated with each core. In a simultaneous multithreaded processor, instructions from multiple threads are available to be issued on any cycle. Therefore, all hardware contexts, and in particular all register files, must be accessible to the pipeline and its execution resources. [10]

In other words, each clock, the core selects instructions from multiple threads to execute on ALUs.

### 3 Programming models

#### 3.1 Implicit SPMD Program Compiler (ISPC)

Before introducing the ISPC compiler, we give the definition of SPMD.

Definition 1: Single Program, Multiple Data (SPMD)

Single Program, Multiple Data (SPMD) is a term that has been used to refer to computational models for exploiting parallelism, where multiple processors work together to execute a program to achieve faster results.

The difference between *SPMD* and *SIMD* (page 25) is that in SPMD parallel execution, multiple autonomous processors simultaneously execute the same program at independent points, rather than in SIMD it is vectorization at the instruction level so that each CPU instruction processes multiple data elements. In other words:

- SPMD: is the **programming abstraction**, because the programmer has to think; the program is written in terms of this abstraction.
- SIMD: in general, the compilers (ISPC) issue special vector instructions that execute the logic performed by each parallel instance created (ISPC gang spawned). In addition, the compilers handle the mapping of conditional control flow to vector instructions.

The difference and the terminology used by ISPC will become clearer in the following pages. We suggest that finish this section and come back here in a moment.

#### Definition 2: Implicit SPMD Program Compiler (ISPC)

**Implicit SPMD Program Compiler (ISPC)** is a compiler for a variant of the C programming language, with extensions for *Single Program, Multiple Data (SPMD)* programming. Under the SPMD model, the programmer writes a program that generally appears to be a regular serial program, though the execution model is actually that a number of program instances execute in parallel on the hardware. In other words, the ISPC gives the programmer some API to do parallelization on the code; it also generates high quality SIMD code to increase performance.

The definition, implementation, and other details are explained in the official Intel GitHub repository.

#### **?** How it works?

Let us take a general main program; when we call an ispc function, it causes a spawn of gang of ISPC program instances upon return, all instances have completed. These instances execute the same ISPC code simultaneously, and each instance has its own copy of local variables. Take the following ISPC code as an example:

```
export void ispc_sinx(
       uniform int N,
2
      uniform int terms,
3
       uniform float* x,
4
       uniform float* result
5
6 ) {
       // assume N % programCount = 0
7
      for (uniform int i=0; i<N; i+=programCount) {</pre>
8
           int idx = i + programIndex;
9
           float value = x[idx];
           float numer = x[idx] * x[idx] * x[idx];
11
           uniform int denom = 6; // 3!
12
           uniform int sign = -1;
13
           for (uniform int j=1; j<=terms; j++) {
14
15
               value += sign * numer / denom
               numer *= x[idx] * x[idx];
16
               denom *= (2*j+2) * (2*j+3);
17
18
               sign *= -1;
           }
19
20
           result[idx] = value;
      }
21
22 }
```

In the example, the programCount (row 8) and programIndex (row 9) variables, uniform (row 2, and so on) data type tell us:

- programIndex gives the index of the SIMD-lane being used for running each program instance (in other words, it's a varying integer value that has value zero for the first program instance, and so forth).
- programCount gives the total number of instances in the gang.
- A variable that is declared with the uniform qualifier represents a single value that is shared across the entire gang.

Together, these can be used to uniquely map executing program instances to input data (programIndex and programCount, uniform data type).

With the ISPC analogy, the **SPMD programming model** should be clear:

- 1. Single thread of control (typically a main program);
- Invoke the SPMD function (in the previous example, the ispc\_sinx function);
- 3. **SPMD execution**, then **multiple instances of the function run in parallel** (multiple logical threads of control);
- 4. Returns and resumes a single thread of control.





Figure 9: Example of execution with 8 instances (programCount equal to 8). For all program instances, there are eight non-contiguous values in memory. A special instruction called gather is needed to implement this, but unfortunately it is a more complex and expensive SIMD instruction rather than a contiguous implementation.

Figure 9 shows a possible execution of the ISPC function using 8 instances. The result is obtained and all is well. But there is one interesting observation. **Each ISPC instance writes each value in a non-contiguous way**. This can be done better:

```
export void ispc_sinx_v2(
       uniform int N,
2
       uniform int terms.
3
       uniform float* x,
 4
       uniform float* result
5
6 ) {
7
       // assume N % programCount = 0
       uniform int count = N / programCount;
8
9
       int start = programIndex * count;
           (uniform int i=0; i<count; i++) {</pre>
10
       for
            int idx = start + i;
            float value = x[idx];
            float numer = x[idx] * x[idx] * x[idx];
13
           uniform int denom = 6; // 3!
uniform int sign = -1;
14
            for (uniform int j=1; j<=terms; j++) {</pre>
16
                value += sign * numer / denom
17
                numer *= x[idx] * x[idx];
18
                denom *= (j+3) * (j+4);
19
                sign *= -1;
20
            }
21
22
            result[idx] = value;
       }
23
24 }
```



Figure 10: Example of execution with 8 instances (programCount equal to 8). A single "packed vector load" instruction efficiently implements this. For all program instances, since the eight values are contiguous in memory.

#### 3.2 Shared Address Space Model

We give a general introduction to memory in the chapter 2.2. In parallel computing theory, **each thread communicates with other threads using read**-/write operations. These instructions operate on a special area called the Shared Address Space (also called Shared Variables).

#### Definition 3: Shared Address Space

The **Shared Address Space** view of a parallel platform supports a common data space that is accessible to all processors. Processors interact by modifying data objects stored in this shared-address-space. [6]

Now the first and trivial question should be: a powerful tool is the possibility to allow communication between threads, but *how can we guarantee that two or more threads accessing the same resource do not create well known problems, such as* race condition?

This property, commonly called **mutual exclusion** or **atomic operation**, can be guaranteed with some techniques:

• Lock/Unlock mutex around a critical section:

```
Lock lock_variable;
Lock lock_variable;
Lock operations, such as spawn of threads
Lock_variable.lock();
Lock_variable.unlock();
Lock_variable.unl
```

• Some languages have first-class support for atomicity of code blocks:

- Intrinsics for hardware-supported atomic read-modify-write operations:
- atomicAdd(x, 10);

The shared address space requires hardware support to be efficiently implemented. The main idea is that each processor can directly reference the contents of any memory location. Some interesting examples that can be explored in depth are: SUN Niagara 2, Knights landing (KNL): 2nd Generation Intel Xeon Phi processor.

#### 3.3 Message Passing model of communication

In parallel computing, the message passing model allows threads (or processes) to communicate by sending and receiving messages. This model is used to facilitate data exchange between threads running in their own private address spaces.

Each thread operates within its private address space, meaning they **do not share memory directly**. When they need to communicate with a specific thread without using a *shared address space model*, they use the *message passing model* to send (or receive) the data.

- Usually, the **sender** specifies
  - the recipient;
  - the buffer to be transmitted;
  - an optional message identifier (a sort of tag).
- Meanwhile, the **receiver** specifies:
  - who the sender is;
  - the buffer where to store data;
  - an optional message identifier (again, a sort of tag).

The message passing model is the **only way to exchange data between threads** because it guarantees three main advantages:

- Data Isolation: Using message passing, each thread maintains its address space, reducing the risk of race conditions.
- Scalability: Message passing scales well with distributed systems and multi-core architectures, making it suitable for large-scale parallel computing.
- Flexibility: It allows for explicit control over data exchange and synchronization, providing Flexibility in parallel program design. Explicit control refers to the fact that in message passing, each communication action is explicitly defined by send and receive operations. This means we can precisely dictate which data is sent, when, and to whom it is sent. Furthermore, the synchronization is managed very well because message passing naturally incorporates synchronization. When a process sends a message, it can block until it is received, ensuring that the sender and receiver are synchronized.

# • Why message passing is preferable to the shared address space model

Unlike shared memory systems that require complex hardware mechanisms to implement system-wide load and store operations, message passing systems do not need this capability. They **only need to communicate messages between nodes**. It can be considered as a great advantage for message passing models, which for this reason is very much used in the supercomputers and clusters. Finally, this model has the ability to **connect commodity hardware systems together to form a large parallel machine**. This means we can use off-the-shelf components to build powerful computing clusters.
#### 3.4 Data-Parallel model

In parallel computing, the **Data-Parallel model** is characterized by **applying the same operation simultaneously across multiple data points**. This model is particularly effective for tasks involving large datasets where the same computation needs to be performed on each data element.

This model organizes computation as operations on sequences of elements (e.g., perform the same function on all elements of a sequence). In programming languages, the basic data type used for this purpose is called Sequence (e.g., C++). Despite the name of the datatype used in the languages, the definition is that it is an ordered collection of elements, where each element can be accessed and manipulated using various sequence operators. The most common operators are:

• Map. The map function is a higher-order function<sup>2</sup> that operates on sequences. It applies a side-effect-free unary function<sup>3</sup>  $f : a \to b$  to all elements of an input sequence, producing an output sequence of the same length.

Example 1: Python Analogy

For a better understanding, we provide a very simple Python code to see how a map function works. In Python there is a map function that does exactly what we say.

```
# Define a trivial function that squares a number
  def square(x):
2
      return x * x
3
  # Create a sample list
5
  numbers = [1, 2, 3, 4, 5]
  # Use the map function to apply the 'square' function
8
9 # to each element in the 'numbers' list
10 squared_numbers = map(square, numbers)
12 # Convert the result to a list and print it
13 print(list(squared_numbers))
  And the result is:
  [1, 4, 9, 16, 25]
```

Now the main idea is: since the map is a function without side effects, we can apply it to all elements of the sequence in any order without changing the output of the program. This allows reordering or parallel processing of sequence elements to optimize performance.

 $<sup>^{2}</sup>$ A higher-order function is a function that can do one or both of the following:

<sup>-</sup> Take other functions as arguments (parameters).

<sup>-</sup> Returns a function or value as its result.

<sup>&</sup>lt;sup>3</sup>A function that takes only one argument and doesn't suffer from side effects.

- <u>Reduction</u>. The reduction born from the need to make parallel operations of iterations. For example, in a for loop, if we need a progressive sum of an element, we should implement some kind of mechanism to manage the synchronization. Using the reduction strategies, the compiler will do this job. We suggest reading the Reduction section (5.3.1.1, page 65) in the OpenMP chapter to understand what we mean.
- Others like  $\underline{\mathbf{scan}}$  and  $\underline{\mathbf{shift}}$ .

# 4 Parallel Programming Models and pthreads

# 4.1 How to create parallel algorithms and programs

Although *parallel algorithms* and *parallel programs* are in the same father set, the parallel computing topic, these two arguments are a little different.

Definition 1: Parallel Algorithms

A **parallel algorithm**, as opposed to a traditional serial algorithm, is an **algorithm which can do multiple operations in a given time**.

**Definition 2: Parallel Programs** 

A parallel program is a program that uses multiple CPU cores, with each core performing a task independently.

However, designing *parallel algorithms* is not an easy task because there is no heuristic for designing *parallel algorithms*. There are some rules that help in the design. The same reasoning applies to *parallel programs*, because they depend on the chosen language and architecture.

Furthermore, there is no single correct solution, but several possible parallel solutions. A good first approach is to start with machine-independent issues (concurrency) and delay target-specific issues as much as possible.

Design a parallel algorithm	Design a parallel program
Understand the problem to be solved	Analyze the target architecture(s)
Analyze data dependencies	Choose the best parallel program- ming model and language
Partition the solution	Analyze the communications (cost, latency, bandwidth, visibility, syn- chronization, etc.)

Table 2: Design parallel algorithms and parallel programs.

The **PCAM** (Partitioning, Communication, Agglomeration, Mapping) methodology described by Argonne National Laboratory is intended to promote an exploratory approach to design in which machine independent issues, such as *concurrency*, are considered early and machine specific aspects of design are deferred until late in the design process. In other words, we immediately consider the machine-independent issues (e.g., concurrency) at the beginning of the design approach, and all machine-specific aspects are postponed to an advanced stage of the design process. This methodology structures the design process into four distinct stages:

- 1. **Partitioning**. The **computation** that is to be performed and the **data** operated on by this computation are **decomposed into small tasks**. Practical issues such as the number of processors in the target computer are ignored, and attention is focused on recognizing opportunities for parallel execution.
- 2. <u>Communication</u>. The communication required to coordinate task execution is determined, and appropriate communication structures and algorithms are defined.
- 3. <u>Agglomeration</u>. The task and communication structures defined in the first two stages of a design are evaluated with respect to performance requirements and implementation costs. If necessary, tasks are combined into larger tasks to improve performance or to reduce development costs.
- 4. <u>Mapping</u>. Each task is assigned to a processor in a manner that attempts to satisfy the competing goals of maximizing processor utilization and minimizing communication costs. Mapping can be specified statically or determined at runtime by load-balancing algorithms.

In the first two stages, we focus on concurrency and scalability and seek to discover algorithms with these qualities. In the third and fourth stages, attention shifts to locality and other performance-related issues.



Figure 11: PCAM design methodology for parallel programs. Starting with a problem specification, develop a partition, determine communication requirements, agglomerate tasks, and finally map tasks to processors.

# 4.2 Analyze parallel algorithms

Whether we want to analyze our parallel algorithm created with the PCAM model or evaluate a general parallel algorithm, we need some metrics.

The classical **metrics** needed to evaluate a parallel algorithm are:

- Time complexity: quantifies the amount of time required to produce a solution.
- Resource complexity: quantifies how many resources are needed to produce the solution in that time.

In general, to analyze a **parallel algorithm**, we can consider its **structure** as a directed acyclic graph  $(DAG)^4$ , where the nodes are the task and the edges are the data dependencies.

## **E** Parallel Algorithm Terminology and Metrics

- Concurrent tasks, each task is executed *independently*.
- **Parallel tasks**, each task is executed at the *same time* (because multiple computing resources are available).
- Work W is the *number of operations executed*. It may be higher than the sequential version of the algorithm due to communication overhead, etc.
- **Span** *S* is the *longest chain of dependencies* (i.e., the critical path) that determines the *minimum time required to execute the algorithm*. This is a *lower bound* on the running time, regardless of the number of processors. The range indicates the ability of an algorithm to get better performance on more processors.

#### **?** How do we calculate the Span metric?

- 1. As we just said, we **represent a parallel algorithm as a DAG** graph, where nodes represent tasks and edges represent dependencies between tasks;
- 2. We assign weights to each node that represent the time required to perform the corresponding task;
- 3. We try to find the Critical Path. In other words, we determine the path from the start node to the end node that has the *maximum cumulative weight*;
- 4. Finally, the sum of the weights of the nodes on the critical path gives us the span value!

 $<sup>^{4}</sup>A$  **Directed Acyclic Graph (DAG)** is a directed graph, i.e. with oriented edges, without cycles.

• **Parallelism** *P* is the *measure of efficiency in the use of resources*. Trivially, it is the number of operations performed divided by the longest chain of dependencies:

$$P = \frac{W}{S} \tag{11}$$

It indicates how many processors can be effectively used by the computation. If the work is equal to the span, the parallelism is 1 and the computation is sequential. Ideally, but not necessarily, we win with polylogarithmic span, because if the work is  $O(n \log n)$  and the span is  $O(\log^2 n)$ , then the parallelism is  $O\left(\frac{n}{\log n}\right)$ , which is actually quite high (and unlikely to be a bottleneck on most machines in the next 25 years). [2]

This measure is one of the most important. It indicates the number of processors that are not idle. It is obvious that a good parallel algorithm is designed to have the lowest possible work (less operation, then less resource usage, then less cost, and so on) and the highest possible parallelism (achievable by reducing the span, and this should be trivial, since the metric P is given by work divided by the span, so reducing the denominator, you can get a higher value).

As in all things, there is a **trade-off** between the lowest possible "work" and the highest possible "parallelism". Reducing the work too much could eliminate the possibility of parallelizing our algorithm, and on the other hand, reducing the span too aggressively could cause communication/synchronization overhead.



Figure 12: Example of DAG implementation with work equal to 9, span equal to 5, and parallelism equal to 1.8  $(9 \div 5)$ . The span calculus is not well known, has been calculated *a priori*.

Finally, we use a mathematical annotation and not only a graphical (DAG) annotation. The **Composition Rules** help determine how to combine smaller parallel tasks into a larger algorithm, while analyzing the Work and Span of the combined algorithm:

• Single operation. An operation takes 1 unit of work and 1 unit of span time.

$$W(op) = 1$$
  $S(op) = 1$ 

# • Sequential Composition.

– The total work of executing  $e_1$  and  $e_2$  sequentially is the sum of their individual work.

$$W(e_1, e_2) = W(e_1) + W(e_2)$$

– The total span of executing  $e_1$  and  $e_2$  sequentially is the sum of their individual spans.

$$S(e_1, e_2) = S(e_1) + S(e_2)$$

# • Parallel Composition.

- The total work of executing  $e_1$  and  $e_2$  in **parallel** is still the sum of their individual works.

$$W(e_1||e_2) = W(e_1) + W(e_2)$$

- The total span of executing  $e_1$  and  $e_2$  in **parallel** is the *maximum of their individual spans*, since they can be executed simultaneously.

$$S(e_1||e_2) = \max(W(e_1), W(e_2))$$

#### 4.3 Technologies

Some famous architecture to work with parallel programming:

• Verilog/VHDL are hardware description languages. The target architectures are ASIC and FPGA. The parallelism and the communication are explicit.

#### ✓ Pros

- Complete control on computation and memory
- No overhead introduced in the computation
- Provides access to potentially large computational power

# A Cons

- Requires specific hardware (e.g., ASIC or FPGA) to implement functionality
- Difficult to learn: completely different programming language and programming paradigm
- Depends on the chosen target architecture
- <u>MPI</u> is a *library*. The target architectures are *Multi CPUs*. The **paral**lelism is implicit and the communication is explicit.

# ✓ Pros

- Can be adopted on different types of architecture
- Scalable solutions
- Synchronization and data communication are explicitly managed

#### **A** Cons

- Communication can introduce significant overhead
- Programming paradigm more difficult than shared memory-based ones
- Standard does not reflect immediately advances in architecture characteristics
- **<u>PThread</u>** is a *library*. The target architectures are *Multi-core CPUs*. The **parallelism** is **explicit** and the **communication** is **implicit**.

#### ✓ Pros

- Can be adopted on different types of architecture
- Explicit parallelism and full control over application

## **A** Cons

- Task management overhead can be significant
- Not easily scalable solutions
- Low level API
- **OpenMP** is a *C*/Fortran extensions. The target architectures are Multicore CPUs. The **parallelism** is **explicit** and the **communication** is **implicit**.

#### ✓ Pros

- Easy to learn
- Scalable solution
- Parallel applications can also be executed sequentially

## **A** Cons

- Mainly focused on shared memory homogeneous systems
- Requires small interaction between tasks
- <u>CUDA</u> is a *C* extensions. The target architectures are *CPU* plus *GPU*(s). The parallelism is implicit/explicit and the communication is implicit/explicit.

## ✓ Pros

- Provides access to the computational power of GPUs
- Writing a CUDA kernel is quite easy
- Already optimized libraries

# A Cons

- Targets only NVIDIA GPUs
- Difficult to extract massive parallelism from application
- Difficult to optimize CUDA kernel
- **OpenCL** is a *C/C++* extensions and *API*. The target architectures are *heterogeneous architecture*. The **parallelism** is **implicit/explicit** and the **communication** is **implicit/explicit**.

#### ✓ Pros

- Target-independent standard
- Hides architecture details
- Same programming infrastructure for every heterogeneous architecture: CPU + GPU (and FPGA)

# A Cons

- Difficult programming paradigm for its heterogeneity
- Hiding of architecture details makes difficult to obtain best performances
- Gradually abandoned
- Apache Spark is an API. The target architectures are *multi CPUs*. The parallelism is implicit and the communication is implicit.
  - ✓ Pros
    - API for different languages
    - Explicit parallelization and communication are not required
    - Preinstalled on cloud provide VMs

# A Cons

- Suitable only for big data applications
- Does not (yet) fully support GPUs

Regardless of these technologies, it is quite common to mix some of them:

- **OpenMP** + **CUDA**: allows to exploit multi-core CPU and GPU. CUDA is used to parallelize GPU code and OpenMP is used to parallelize CPU code.
- MPI + OpenMP: the most common scenario are:
  - 1. MPI used to express coarser parallelism (multi CPU) and OpenMP used to express finer parallelism (multi core).
  - 2. MPI used to implement communication and OpenMP used to parallelize computation.
- **OpenCL** + **Verilog or VHDL**: in principle, hardware kernels (implemented for example on FPGA) can be used as accelerators; OpenMP used to describe parallelism among different processing elements; Verilog/VHDL used to describe hardware kernel. An example of target: Intel Xeon Scalable.

# 4.4 Threads

#### 4.4.1 Flynn's taxonomy

**Flynn's taxonomy** is a **classification of computer architectures**, proposed by Michael J. Flynn. The classification system has been used as a tool in the design of modern processors and their functionalities. Since the rise of multiprocessing central processing units (CPUs), a multiprogramming context has evolved as an extension of the classification system.

The four initial classifications defined by Flynn are based upon the number of concurrent instruction (or control) streams and data streams available in the architecture:

- Single Instruction stream, Single Data stream (SISD)
- Single Instruction stream, Multiple Data streams (SIMD)
- Multiple Instruction stream, Single Data stream (MISD)
- Multiple Instruction stream, Multiple Data stream (MISD)

It is important to quote it because it is the basis for the development of many advanced technologies.

#### 4.4.2 Definition

A UNIX process can be created by the operating system and contains information about program resources and program execution status.

**Definition 3: Thread** 

A thread is an independent stream of instructions within a process. Threads can be scheduled by the operating system, and each thread can run concurrently with other threads. A thread also has local resources and can access the shared process resources.

In other words, a thread can be thought of as any **procedure that runs independently of its main program**. We can create each thread dynamically during execution. A good point is that a multi-threaded program is lighter than a multi-process program. When a thread exists within a process, it shares most of the process resources, for example:

- Changes made by one thread to shared system resources (such as closing a file) will be seen by all other threads.
- Two pointers having the same value point to the same data.
- Implicit communication by reading and writing shared variables.
- Reading and writing to the same memory locations requires explicit synchronization by the programmer. If this rule is not followed, the code may suffer from a data race or race condition <sup>5</sup> problem.

The most common models for threaded programs are the manager / worker model  $^6$  and pipeline.

This chapter introduces the POSIX threads model.

# **Definition 4: pthreads**

**POSIX Threads**, commonly known as **pthreads**, is an **execution model** that exists independently from a programming language, as well as a parallel execution model. It **allows a program to control mul-tiple different flows of work that overlap in time**. Each flow of work is referred to as a thread, and creation and control over these flows is achieved by making calls to the POSIX Threads API.

POSIX threads and OpenMP are two **implementations of a shared memory parallel programming model using threads**. The **programmer is responsible for handling parallelism and synchronization**, usually through a library of subroutines or a set of compiler directives. Typically, hardware vendors have implemented their own proprietary versions of threads, but in this course we will look at POSIX threads (pthreads) and OpenMP.

<sup>&</sup>lt;sup>5</sup>In parallel computing, a **Data Race** or **Race Condition** is a software problem that occurs when two threads (or processes) access the same variables, and at least one does a write. They can finish in a different order than expected.

<sup>&</sup>lt;sup>6</sup>The manager/worker pattern is described as follows. The idea is that the work that needs to be done can be divided by a "manager" into separate pieces and the pieces can be assigned to individual "worker" processes. Thus the manager executes a different algorithm from that of the workers, but all of the workers execute the same algorithm. Most implementations of MPI allow MPI processes to be running different programs (executable files), but it is often convenient (and in some cases required) to combine the manager and worker code into a single program.

#### 4.4.3 pthreads API

In 1995, the IEEE POSIX 1003.1c standard specified the API for explicitly managing threads. An API is a set of C language programming types and procedure calls.

- Header file to include in the main file: pthread.h.
- To compile and use it, it is necessary to add the flag -pthread to the gcc (or g++) options.

The API are divided by what we want to do. In general, there are two sets: thread management and thread synchronization.

- Thread Management
  - Creation (page 49)
  - Termination (page 50)
  - Joining (page 51)
  - Detaching (page 52)
  - Joining through Barriers (page 53)
- Thread Synchronization
  - Mutexes (page 54)
  - Condition variables (page 54)

## 4.4.3.1 Creation

Once threads are created, they are peers, and may create other threads. There is no implied hierarchy or dependency between threads. The maximum number of threads depends on the implementation.

Doc. 🚍

```
pthread API: pthread_create

int pthread_create(
    pthread_t * thread,
    const pthread_attr_t * attr,
    void * (* start_routine) (void *),
    void * arg
)
```

- Return value: on success, pthread\_create() returns 0; on error, it returns an error number, and the contents of \*thread are undefined.
- Arguments:
  - thread: identifier for the new thread returned by the subroutine.
  - attr: used to set thread attributes, such as joinable, detached, scheduling and stack size.

- start\_routine: the C routine that the thread will execute once it is created.
- arg: argument passed to start\_routine. It must be passed by address as a pointer cast of type void.

# 4.4.3.2 Termination

The thread returns from its startup routine when its "life" ends. The thread makes a call to the pthread\_exit subroutine.

Doc. 📃

	$\mathbf{pthr}$	ead API: pthread_exit
1	void	pthread_exit(void *retval)

- Return value: this function does not return to the caller.
- Arguments:
  - retval: function terminates the calling thread and returns a value via retval.

Doc. 📃 The thread is canceled by another thread via the pthread\_cancel routine.

```
pthread API: pthread_cancel
int pthread_cancel(pthread_t thread)
```

- Return value: on success, pthread\_cancel() returns 0; on error, it returns a nonzero error number.
- Arguments:
  - thread: the pthread\_cancel() function sends a cancellation request to the thread thread.

Doc. 📃

## 4.4.3.3 Joining

The join function blocks the calling thread until the specified thread exits.

```
pthread API: pthread_join
1 int pthread_join(pthread_t thread, void **retval)
```

- Return value: on success, pthread\_join() returns 0; on error, it returns an error number.
- Arguments:
  - thread: the pthread\_join() function waits for the thread specified by thread to terminate. If that thread has already terminated, then pthread\_join() returns immediately. The thread specified by thread must be joinable.

If multiple threads simultaneously try to join with the same thread, the results are undefined. If the thread calling pthread\_join() is canceled, then the target thread will remain joinable (i.e., it will not be detached).

- retval: if retval is not NULL, then pthread\_join() copies the exit status of the target thread (i.e., the value that the target thread supplied to pthread\_exit()) into the location pointed to by retval. If the target thread was canceled, then PTHREAD\_CANCELED is placed in the location pointed to by retval.

#### 4.4.3.4 Detaching

The detach function marks a thread as detached. When a thread is detached, its resources are automatically released back to the system when the thread terminates, without the need for another thread to join with it.

### • Why would I need to detach a thread and not join it?

Good question. The answer depends on what we have to do.

- Fire and forget tasks. When we start a thread to perform a task that doesn't require further interaction or result processing, releasing it ensures that the resources are automatically cleaned up when the task is complete.
- **Resource management**. Detaching avoids the need for another thread to call pthread\_join(), which can save system resources and reduce the complexity of our code. It's especially useful in a highly concurrent application with many short-lived threads.
- Avoid deadlocks. When we have potential circular dependencies or complex synchronization between threads, detaching threads can help avoid deadlocks by eliminating the need for one thread to wait on another.
- Long-running background tasks. For tasks that should run independently in the background and not block the main program flow, detaching makes sense. We make sure they clean up after themselves without having to explicitly manage their lifecycle.

Doc. 🚍



- Return value: on success, pthread\_detach() returns 0; on error, it returns an error number.
- Arguments:
  - thread: the pthread\_detach() function marks the thread identified by thread as detached. When a detached thread terminates, its resources are automatically released back to the system without the need for another thread to join with the terminated thread.

Attempting to detach an already detached thread results in unspecified behavior.

## 4.4.3.5 Joining through Barriers

The *barrier init* function **initializes a barrier object**, and the *barrier wait* function **blocks a thread until the specified number of threads have called it**. A **barrier object** is, in parallel computing, a synchronization tool that ensures that multiple threads reach a certain point of execution before any of them continue. It's like a **checkpoint that everyone must reach before continuing**, ensuring coordinated progress in a parallel algorithm.<sup>7</sup>

Doc. 📃

	$\mathbf{pth}$	read <b>API</b> : pthread_barrier_init
1	int	pthread_barrier_init(
2		<pre>pthread_barrier_t * barrier,</pre>
3		<pre>pthread_barrierattr_t * attr,</pre>
4		unsigned int count
5	)	

pthread API: pthread\_barrier\_wait

int pthread\_barrier\_wait(pthread\_barrier\_t \* barrier)

- **Return value**: on success, function return 0; on error, they return an error number.
- Arguments: the main and most important argument is count, which specifies the number of threads to wait for.

<sup>&</sup>lt;sup>7</sup>For example, imagine multiple threads working on different parts of a matrix. A barrier can ensure that all threads finish their part of the computation before moving on to the next phase, such as combining results or performing subsequent operations.

## 4.4.3.6 Mutexes

Mutex variables are the basic method of protecting shared data when multiple writes occur. Only one thread can lock a mutex variable at a time. If multiple threads attempt to lock a mutex, only one thread will succeed. Threads that fail to acquire the mutex are blocked. There is also the trylock function, which returns immediately if the mutex is currently locked (by any thread, including the current thread). Note that a lock function has the potential to create a deadlock situation.

There are also **three types of mutex** that can be set using the **settype** function:

- Normal Mutex (PTHREAD\_MUTEX\_NORMAL). A normal mutex does not check for errors such as deadlock. If a thread tries to lock a mutex it already owns, the thread will deadlock.
- Error Check Mutex (PTHREAD\_MUTEX\_ERRORCHECK). Provides error checking. If a thread tries to lock a mutex it already owns, lock function will return an error instead of deadlocking.
- **Recursive Mutex (PTHREAD\_MUTEX\_RECURSIVE)**. Allows the same thread to lock the mutex multiple times without deadlocking. Each lock must have a corresponding unlock.



## 4.4.3.7 Condition variables

Mutexes implement synchronization by serializing data accesses. Condition variables allow threads to synchronize explicitly by signaling the meeting of a condition. Without condition variables, the programmer would need to poll to check if the condition is met.

# 5 OpenMP v5.2

# 5.1 Introduction

**OpenMP** is a scalable model that gives parallel programmers a simple and flexible interface for developing portable parallel applications in C/C++ and Fortran.

- Header file to include in the main file: omp.h.
- To compile and use it, it is necessary to add the flag -fopenmp to the gcc (or c++) options.

The following link contains about 200 slides on OpenMP. It is an introduction, but it covers every argument required in this PoliMI course. The slides are made by a Senior Principal Engineer, Mattson Tim. He's a Senior Principal Engineer at Intel, where he's been since 1993. The slide link.

## ✓ Benefits

- Standard across a variety of shared memory architectures and platforms.
- Supports three famous languages: Fortran, C and C++.
- Scalable from embedded systems to the supercomputer.
- The directives are intuitive, and with a limited set of directives we can implement parallel algorithms.
- Incremental parallelization of serial program.
- Coarse-grained and fine-grained parallelism. See here here an interesting difference between coarse-grained and fine-grained architecture:



# **?** How it works?

OpenMP is based on the **fork-join paradigm**. A "master" thread forks a specified number of "slave" threads. Tasks are divided among the "slaves", and each "slave" runs concurrently as the runtime allocates threads to different processors.

- 1. Thread #0 born. OpenMP programs start with a single thread;
- 2. Fork. At the start of a parallel region, the *master* creates a team of parallel worker threads (*slaves*).
- 3. **OpenMP code block**. Statements in the parallel block are executed in parallel by each thread.
- 4. Join. At the end of the parallel region, all threads synchronize (implicit barrier, see definition on page 53) and join the master thread. [5]



end

Figure 13: Example of an OpenMP program called Hello. At runtime, the *master* thread forks 3 additional *slave* threads to print hello. The example is very trivial, but here is a graphical representation of the workflow. An interesting thing to note is that **OpenMP creates** a sort of **region where each thread executes all the instructions in the OpenMP block**. This is important to understand. [5]

# 5.2 Basic syntax

We can manage OpenMP work flow using the directive syntax. We remember that the reference guide of OpenMP is available on their website:

Reference Guide



A **directive** is a combination of the base-language mechanism and a *directive-specification* (the *directive-name* followed by *optional clauses*). A construct consists of a directive and, often, additional base language code. In C++ directives are formed from either pragmas or attributes.

	OpenMP: pragma omp
1	<pre>#pragma omp directive-specification</pre>

The number of OpenMP threads can be set using:

- At compilation time: using the environment variable OMP\_NUM\_THREADS
- At runtime: using the function

OpenMP: omp\_set\_num\_threads

Other useful function to get information about threads:

• The number of threads in the current team:

Doc. 📃

Doc. 📃



The binding region for an omp\_get\_num\_threads region is the innermost enclosing parallel region. If called from the sequential part of a program, this routine returns 1.



OpenMP programs execute serially until they reach a parallel directive. As we have explained at page 56, the thread that was executing the code spawns a group of "slave" threads and becomes the "master" (thread ID 0). The code in the structured block is replicated, each thread executes a copy. At the end of the block there is an implied barrier, only the "master" thread continues.

	OpenMP: pragma omp parallel	
1	<pre>#pragma omp parallel optional-clauses</pre>	

The parallel directive has **optional** clauses, the most commonly used are:

- Specify the number of threads to spawn:
- 1 #pragma omp parallel num\_threads(int)

• Conditional parallelization with:

```
1 #pragma omp parallel if (condition)
```

```
Example 1: parallel if condition
1 #include <stdio.h>
2 #include <omp.h>
3
4 void test(int val)
5 {
      #pragma omp parallel if (val != 0)
6
      if (omp_in_parallel()) {
7
          #pragma omp single
8
          printf_s(
9
               "val = d, parallelized with d threadsn",
10
               val, omp_get_num_threads()
11
          );
12
13
      } else {
          printf_s("val = %d, serialized\n", val);
14
      }
15
16 }
17
18 int main( )
19 {
      omp_set_num_threads(2);
20
21
      test(0);
22
      test(2);
23 }
  The output will be:
val = 0, serialized
2 val = 2, parallelized with 2 threads
```

• Data scope clauses (explained in the following pages).

The number of threads in a parallel region is determined by the following factors, in order of priority (high to low):

- 1. Evaluation of the if clause;
- 2. Value of the num\_threads clause;
- 3. Use of the omp\_set\_num\_threads() library function;
- 4. Setting of the OMP\_NUM\_THREADS environment variable;
- 5. Implementation default, e.g., the number of CPUs on a node.

### 5.3 Work sharing

Work-sharing constructs divide the execution of a region of code among the team members who encounter it. A work-sharing construct must be enclosed in a parallel region for the directive to be executed in parallel. Note that the constructs do not start new threads. Also, there is <u>no</u> implicit barrier at the *entry* of a work-sharing construct, but <u>there is</u> an implicit barrier at the *exit* of a work-sharing construct.

#### 5.3.1 For

The for directive shares iterations of a loop across the team (data parallelism).



Figure 14: OpenMP for loop.



The for directive parallelize execution of iterations. The number of iteration cannot be internally modified. Some common clauses are:

- schedule that describes how iterations of the loop are distributed among the threads in the team. The schedule type can be either dynamic, guided, runtime, or static.
  - static. Loop iterations are divided into blocks of size chunk and then statically allocated to threads. If chunk is <u>not</u> specified, the iterations are divided evenly (if possible) among the threads.



Figure 15: static schedule.

- dynamic. Loop iterations are divided into blocks of size chunk and distributed among the threads at runtime; when a thread completes one chunk, it is dynamically allocated another. The default chunk size is 1. In fact, we can see in the image that the order is not always the same.



Figure 16: dynamic schedule.

- runtime. Depends on environment variable OMP\_SCHEDULE.
- *guided*. Static, gradually decreases the chunk size (chunk specifies the smallest one).





Figure 17: guided schedule.

	Example 2: schedule types
1	<pre>#include <stdio.h> #include <stdio.h></stdio.h></stdio.h></pre>
2	#include <omp.n></omp.n>
4	#define NUM_THREADS 4
5	#define STATIC_CHUNK 5
6	#define DYNAMIC_CHUNK 5
7	#define NUM_LOOPS 20
8	#define SLEEP_EVERY_N 3
10	int main()
11	{
12	<pre>int nStatic1[NUM_LOOPS],</pre>
13	nStaticN[NUM_LOOPS];
14	<pre>int nDynamic1[NUM_LOOPS],</pre>
15	nDynamicN[NUM_LUUPS];
16	Int ndulded[NOM_LOOPS];
18	<pre>omp_set_num_threads(NUM_THREADS);</pre>
19	
20	#pragma omp parallel
21	{
22	<pre>#pragma omp for schedule(static, 1) for (int i = 0 ; i &lt; NUM LOODS ; i + i)</pre>
23	101 (INC 1 - 0 ; 1 < NOM_LOUPS ; ++1)
25	if $((i \% SLEEP EVERY N) == 0)$
26	Sleep(0);
27	<pre>nStatic1[i] = omp_get_thread_num( );</pre>
28	}
29	#program orp for schedule(static STATIC (HUNK)
30	
32	{
33	<pre>if ((i % SLEEP_EVERY_N) == 0)</pre>
34	Sleep(0);
35	<pre>nStaticN[i] = omp_get_thread_num( );</pre>
36	}
37	#pragma omp for schedule(dynamic 1)
39	for (int i = 0 ; i < NUM_LOOPS ; ++i)
40	{
41	<pre>if ((i % SLEEP_EVERY_N) == 0)</pre>
42	Sleep(0);
43	<pre>nDynamic1[i] = omp_get_thread_num( );</pre>
44	ł
45 46	<pre>#pragma omp for schedule(dvnamic. DYNAMJC CHUNK)</pre>
47	for (int i = 0 ; i < NUM_LOOPS ; ++i)
48	{
49	<pre>if ((i % SLEEP_EVERY_N) == 0)</pre>

```
Sleep(0);
50
          nDynamicN[i] = omp_get_thread_num( );
       }
52
53
       #pragma omp for schedule(guided)
54
55
       for (int i = 0 ; i < NUM_LOOPS ; ++i)</pre>
       {
56
          if ((i % SLEEP_EVERY_N) == 0)
57
            Sleep(0);
58
          nGuided[i] = omp_get_thread_num( );
59
       }
60
61
    }
62
63
    printf_s("
    _____\n")
    :
    printf_s("| static | static | dynamic | dynamic |
64
    guided |\n");
              1 | %d | 1 | %d |
65
    printf_s("|
     |\n",
            STATIC_CHUNK, DYNAMIC_CHUNK);
66
    printf_s("
67
    _ _ _ _ _ _ _
           -----\n")
    ;
68
    for (int i=0; i<NUM_LOOPS; ++i)</pre>
69
70
    Ł
       printf_s("| %d | %d | %d | %d
71
       1.0
               "%d |\n",
72
                nStatic1[i], nStaticN[i],
73
                nDynamic1[i], nDynamicN[i], nGuided[
74
    i]);
75
    }
76
77
    printf_s("
    -----\n")
78 }
 The result will be:
1 -----
2 | static | static | dynamic | dynamic | guided |
3 | 1 | 5 | 1 | 5 |
                                  1
4 -----
       | 0 | 0
                           | 1 |
5 0
                    | 2
6
     1
       0
              3
                     2
                                1
                                   I
                             1
                     1
                                  1
7
           0
                 3
                         2
     2
                            1
          0
             Ι
       |
                     8
     3
                  3
                         2
                            1
                                1 |
9
     0
           0
              2
                         2
                                1
                             1
                 2
                                  Ι
       Ι
                     Т
              Ι
10
     1
           1
                         3
                                3
                             I.
                 2
11
     2
       1
                         3
                                3
                                  I
                     Ì
     3
                 0
                         3
                                3
12
       1
              0
                     i
       Ι
              Т
13
           1
     0
                         3
                                3
                            14
     1
       - 1
           1
                 0
                         3
                                2
                                  - 1
              |
15
     2
           2
              |
                         0
                                2
                  1
                             1
                     I
           2
                                2
16
     3
                  1
                      0
                             17
     0
       2
                 1
                         0
                                3 |
             Ι
                           Ι
                                3 |
     1
      |
           2
                  2
                         0
18
                     1
19
     2
           2
              2
                      T
                         0
                             0
                                   1
```



- *nowait* to avoid synchronization at the end of the parallel loop. It overrides the barrier implicit in a directive.
- 1 **#pragma** omp for nowait

```
Example 3: nowait clause
1 #include <stdio.h>
2
3 #define SIZE 5
4
5 void test(int *a, int *b, int *c, int size)
6 {
7
       int i;
       #pragma omp parallel
8
9
       {
            #pragma omp for nowait
for (i = 0; i < size; i++)
        b[i] = a[i] * a[i];</pre>
10
11
12
13
            14
15
16
       }
17
18 }
19
20 int main( )
21 {
       int a[SIZE], b[SIZE], c[SIZE];
22
23
       int i;
24
       for (i=0; i<SIZE; i++)</pre>
25
26
           a[i] = i;
27
       test(a,b,c, SIZE);
28
29
       for (i=0; i<SIZE; i++)
    printf_s("%d, %d\n", a[i], b[i], c[i]);</pre>
30
31
32 }
  The output will be:
1 0, 0, 0
2 1, 1, 0
3 2, 4, 1
4 3, 9, 1
5 4, 16, 2
```

#### 5.3.1.1 Reduction

In parallel programming, sometimes there are some exceptional cases when we use the **for** statement where the variables inside the code block are not so easy to manage (memory viewpoint). For example, consider the following case:

```
1 #include "stdio.h"
2 #include "omp.h"
3 #define MAX 10
5
6 int main(int argc, char const *argv[])
7 {
       double ave = 0.0;
8
       double A[MAX] = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10};
9
10
       int i;
       #pragma omp parallel for
11
12
       for(i = 0; i < MAX; i++) {</pre>
           ave += A[i];
13
14
      }
       ave = ave / MAX;
15
      printf("Value %f\n", ave);
16
17
       return 0;
18 }
```

#### **A** Too many threads modifying the same variable

In this case, we are combining values into a single accumulation variable (called **ave**). There is a true dependence between loop iterations that can't be trivially removed. A **continuous execution produces different results!** 

```
1 $ ./example.out
2 Value 1.300000
3 $ ./example.out
4 Value 2.400000
5 $ ./example.out
6 Value 2.500000
7 $ ./example.out
8 Value 2.100000
9 $ ./example.out
10 Value 1.900000
```

This is a very common situation and a solution, which can also be **used as a** synchronization technique, is called a reduction.

A reduction variable in a loop **aggregates** (i.e., accumulates) a **value that depends on each iteration of the loop** and **doesn't depend on the iter-ation order**.



A reduction clause:

• It makes a local copy of each *list* variable and initialized depending on the *operator*;

- It updates occur on the local copy;
- Local copies are reduced into a single value and combined with the original global value.

Therefore, the variables in *list* must be shared in the enclosing parallel region.

Many different associative operands (  $operator\ {\rm value})$  can be used with reduction:

- $\bullet\,$  + with initial value 0
- \* with initial value 1
- - with initial value 0
- min with initial value as largest positive number
- max with initial value as most negative number
- & with initial value  $\sim 0$
- | with initial value 0
- ~ with initial value 0
- && with initial value 1
- || with initial value 0

Using the **reduction** clause, the code written at the beginning of the paragraph can be fixed as follows:

```
1 #include "stdio.h"
2 #include "omp.h"
3 #define MAX 10
4
5
6 int main(int argc, char const *argv[])
7 {
      double ave = 0.0;
8
      double A[MAX] = {1, 2, 3, 4, 5, 6, 7, 8, 9, 10};
9
10
      int i;
11
      // use reduction
      #pragma omp parallel for reduction(+: ave)
12
      for(i = 0; i < MAX; i++) {
13
           ave += A[i];
14
      }
15
      ave = ave / MAX;
16
      // now it prints the correct result 5.5
17
      printf("Value %f\n", ave);
18
19
      return 0;
20 }
```

✓ Avoid race condition

#### 5.3.2 Sections

Section identifies code sections to be divided among all threads.

Sections allow to specify that the enclosed section(s) of code are to be executed in parallel. Each section is executed once by a thread in the team.

Doc. 📃

	OpenMP: sections
1	<pre>#pragma omp [parallel] sections [clauses] </pre>
3	t #pragma omp section
4 5	code_block
6 7	} }

The sections directive identifies a noniterative work-sharing construct that specifies a set of constructs that are to be divided among threads in a team. Each section is executed once by a thread in the team.

Each section is preceded by a section directive, although the section directive is optional for the first section. The section directives must appear within the lexical extent of the sections directive. There's an **implicit barrier** at the end of a sections construct, unless a nowait is specified.

Restrictions to the sections directive are as follows:

- A section directive must not appear outside the lexical extent of the sections directive.
- Only a single nowait clause can appear on a sections directive.



Figure 18: Breaks work into separate, discrete sections, each executed by a thread (functional parallelism).

## 5.3.3 Single/Master

A section (not the directive) of code should be executed on a single thread, not necessarily the main (master) thread. The single directive identifies a construct that specifies that the associated structured block is executed by only one thread in the team (not necessarily the master thread).

	OpenMP: single and master
1	#pragma omp parallel
2	{
3	#pragma omp single
4	{
5	/* code section */
6	}
7	# pragma omp master
8	
9	/* COUE SECTION */
11	ነ
11	J

- single specifies that a section of a code is executed only by a single thread.
- Doc. 📃

Doc. 📃

• master specifies that a section of a code is **executed only by the mas**ter.

There's an **implicit barrier** after the **single** construct unless a **nowait** clause is specified.

#### 5.3.4 Tasks

The following section has been enhanced with slides from Senior Principal Engineer Mattson Tim. He's a senior principal engineer at Intel, where he's been since 1993. His profile can be seen here and the slides are available online here. He has also made an interesting YouTube series on the introduction to OpenMP.

Tasks are independent units of work. They consist of: *code to execute*, *data environment*, and *internal control variables* (ICV). Threads perform the work of each task. The runtime system decides when to execute tasks; each task can be deferred or executed immediately.

In other words, an OpenMP task is a block of code contained in a parallel region that can be executed simultaneously with other tasks in the same region.

Some useful terminology:

- *Task construct*. It identifies the task directive plus the structured block.
- *Task*. It is the package of code and instructions for allocating data created when a thread encounters a task construct.
- *Task region*. It is the dynamic sequence of instructions generated by the execution of a task by a thread.

Tasks are guaranteed to complete at thread barriers (using the **barrier** directive) or at task barriers (using the **taskwait** directive):

```
1 #pragma omp parallel // omp directive to parallel the code
2
  {
      #pragma omp task // multiple foo tasks created here,
3
4
                         // one for each thread
5
      foo():
      #pragma omp barrier // all foo tasks guaranteed
6
                            // to be completed here
      #pragma omp single
                           // only one thread can access to
8
                            //\ {\tt this} piece of code
9
      {
           #pragma omp task // one bar task created here
           bar();
13
      7
       // foo task guaranteed to be completed here
14
15 }
```

#### Example 4: Fibonacci with tasks

Let us see a Fibonacci example of data scoping using the tasks. In the following code, we create the Fibonacci function and we create two tasks, but each task has a private variable and these variables are also used in the return statement:

```
1 int fib(int n) {
2 int x, y;
3 if(n < 2)</pre>
```

```
4 return n;
5 #pragma omp task
6 x = fib(n-1);
7 #pragma omp task
8 y = fib(n-2);
9 #pragma omp taskwait
10 return x + y;
11 }
```

A good solution is to "share" the x and y variables because we need both values to calculate the sum.

```
1 int fib(int n) {
2
      int x, y;
      if(n < 2)
3
          return n;
4
5
      #pragma omp task shared(x)
6
      x = fib(n-1);
      #pragma omp task shared(y)
7
      y = fib(n-2);
8
      #pragma omp taskwait
9
10
      return x + y;
11 }
```

## ✓ Main advantage

Note the following code:

```
1 // create a team of threads
2 #pragma omp parallel
3
  ſ
       // one thread executes the single construct
4
5
      // and other threads wait at the implied
      // barrier at the end of the single construct
6
      #pragma omp single
7
      { // block 1
8
          node *p = head;
9
           while(p) { // block 2
10
              // the single thread creates a task
11
               // with its own value for the pointer p
12
               #pragma omp task firstprivate(p)
13
                  process(p);
14
               p = p \rightarrow next; // block 3
15
16
           }
           // execution moves beyond the barrier
17
18
           // once all the tasks are complete
      }
19
20 }
```

The tasks have the **potential to parallelize irregular patterns and recur**sive function calls. See Figure 19 (page 71) to understand how the runtime system can optimize execution using the tasks.



Figure 19: The main advantage of the tasks is to parallelize irregular patterns and recursive function calls.

# Synchronization

When a thread encounters a task construct, the task is created but not immediately executed. The tasks are guaranteed to be completed:

- At a **barrier** (implicit or explicit)
- At task synchronization points:
  - taskwait construct specifies a wait on the completion of child tasks of the current task.



Doc. 📃

	$\mathbf{OpenMP}:$ pragma omp taskwait	
1	#pragma omp taskwait	
		J

 taskgroup construct specifies a wait on the completion of child tasks of the current task (such as taskwait) and their descendent tasks (main difference).



#### 5.3.4.1 Task dependences

By creating tasks instead of sections, each thread can execute any task as long as its input is ready. Since the internal scheduler decides how to manipulate the execution of tasks, there is a useful **clause to indicate a dependency between tasks**.

Doc. 📃

	OpenimP: aepena
1	<pre>#pragma omp task depend(dependence-type: variable)</pre>
	The depend clause enforces additional constraints on the scheduling of tasks or loop iterations. These constraints establish dependencies only between sibling tasks or between loop iterations. The dependence-type can be in or out.

In addition to the depend clause, we can also use the priority clause to hint that more important tasks should be executed more frequently.

The priority clause is a hint for the priority of the generated task. The priority-value is a non-negative integer expression that provides a hint for task execution order. Among all tasks ready to be executed, higher priority tasks (those with a higher numerical value in the priority clause expression) are recommended to execute before lower priority ones. The default priority-value when no priority clause is specified is zero (the *lowest priority*).

If a value is specified in the priority clause that is higher than the maxtask-priority-var ICV (internal control variables) then the implementation will use the value of that ICV. A program that relies on task execution order being determined by this priority-value may have unspecified behavior.

• The omp\_get\_max\_task\_priority routine returns the maximum value that can be specified in the priority clause.





• The OMP\_MAX\_TASK\_PRIORITY environment variable controls the use of task priorities by setting the initial value of the *max-task-priority-var* ICV. The value of this environment variable must be a non-negative integer.

#### Doc. 📃

#### A Possible overhead

The task in general, but especially the **dependencies between tasks**, can introduce overhead and reduce performance.
```
Example 5: dependences
```

Let the following parallel code:

```
1 #pragma omp parallel default(none) \
                         shared(fp_read) \setminus
2
                         shared(n_io_chunks) \
3
4
                         shared(n_work_chunks) 
                         shared(a, b, c) \setminus
5
                         shared(status_read, status_processing) \setminus
6
7
                         shared(status_postprocessing)
8 {
9
      #pragma omp single nowait
10
      {
           for(int64_t i = 0; i < n_io_chunks; ++i) {</pre>
12
               #pragma omp task depend(out: status_read[i]) \
                                  priority(20)
13
14
               {
                    (void) read_input(
15
                        fp_read, i, a, b, &status_read[i]
16
                   );
17
               } // End of task reading in a chunk of data
18
19
20
               #pragma omp task depend(in: status_read[i]) \
                            depend(out: status_processing[i]) \
21
                            priority(10)
22
23
               {
                    (void) compute_results(
^{24}
25
                        i, n_work_chunks, a, b, c,
                        &status_processing[i]
26
                   ):
27
               } // End of task performing the computations
28
29
               #pragma omp task depend(in: status_processing[i])
30
                                  priority(5)
31
               {
32
                    (void) postprocess_results(
33
                        i, n_work_chunks, c,
34
35
                        &status_postprocessing[i]
36
                   );
               } // End of task postprocessing the results
37
           } // End of for-loop
38
      } // End of single region
39
40 } // End of parallel region
41
```

• Row 11. We are going to process n\_io\_chunks of data.

• Rows 12, 20. Refer to read and are compute dependence.

• Rows 21, 30. Refer to compute and are postprocess dependence.



### **?** Custom number of iterations

it is implied before and after every task.

Each task gets assigned a number of iterations which is the minimum between grainsize and the total number of iterations.

If a grainsize clause is present, the number of logical iterations assigned to each generated task is greater than or equal to the minimum of the value of the *grain-size* expression and the number of logical iterations, but less than two times the value of the *grain-size* expression.

If the grainsize clause has the *strict* modifier, the number of logical iterations assigned to each generated task is equal to the value of the *grain-size* expression, except for the generated task that contains the sequentially last iteration, which may have fewer iterations. The parameter of the grainsize clause must be a positive integer expression.

Doc. 📃

```
OpenMP: pragma omp taskloop grainsize
```

## **?** Number of created tasks

To keep the number of created tasks low, the clause num\_tasks sets the number of tasks that the runtime system can generate.

If num\_tasks is specified, the taskloop construct creates as many tasks as the minimum of the *num-tasks* expression and the number of logical iterations. Each task must have at least one logical iteration. The parameter of the num\_tasks clause must be a positive integer expression.

If the num\_tasks clause has the *strict* modifier for a task loop with N logical iterations, the logical iterations are partitioned in a balanced manner and each partition is assigned, in order, to a generated task. The partition size is

 $\left[\left\lceil \frac{N}{\textit{num-tasks}}\right\rceil\right]$  until the number of remaining iterations divides the number of

 $\left| \left| num - tasks \right| \right|$ remaining tasks evenly, at which point the partition size becomes  $\left[ \left| \frac{N}{num - tasks} \right| \right]$ .

<b>OpenMP:</b> pragma	omp	taskloop	num_tasks

```
1 #pragma omp taskloop num_tasks([strict] num-tasks)
```

If neither a grainsize nor num\_tasks clause is present, the number of loop tasks generated and the number of logical iterations assigned to these tasks is implementation defined.

## 5.4 Synchronization

The following section has been enhanced with slides from Senior Principal Engineer Mattson Tim. He's a senior principal engineer at Intel, where he's been since 1993. His profile can be seen here and the slides are available online here. He has also made an interesting YouTube series on the introduction to OpenMP.

OpenMP is a multi-threaded, shared address model. This means that threads communicate by sharing variables. Unfortunately, this can cause some problems such as race conditions (page 48). The solution is to **use synchronization to protect against data conflicts**. The good news is that synchronization can avoid data race problems, but it is also an **expensive method**. So we can use synchronization, but we **need to change the way data is accessed to minimize the need for synchronization**.

Synchronization brings one or more threads to a well-defined and known point in their execution. The two most common forms of synchronization are:

- *Barrier*: each thread wait at the barrier **until all threads arrive**.
- *Mutual exclusion*: define a block of code that only one thread at a time can execute.

The OpenMP directives are: critical, atomic, and barrier. These are highlevel synchronization directives, but there are also low-level synchronization directives, such as flush and locks, but they are too complex at the moment, we will see them later.



(a) Barrier. Each thread wait at the barrier until all threads arrive.



(b) Mutual exclusion. Define a block of code that only one thread at a time can execute.

**Barrier**. Each thread waits until all threads arrive.

Doc. 📃

```
OpenMP: barrier

    #pragma omp barrier name
```

An optional name may be used to identify the critical region. A thread waits at the beginning of a critical region until no other thread is executing a critical region (anywhere in the program) with the same name. All unnamed critical directives map to the same unspecified name.

```
Example 6: synchronization with barrier directive
```

The following example includes several critical directives. The example illustrates a queuing model in which a task is dequeued and worked on. To guard against many threads dequeuing the same task, the dequeuing operation must be in a **critical** section. Because the two queues in this example are independent, they're protected by **critical** directives with different names, *xaxis* and *yaxis*. [9]

```
#pragma omp parallel shared(x, y) private(x_next, y_next)
{
    #pragma omp critical ( xaxis )
        x_next = dequeue(x);
    work(x_next);
    #pragma omp critical ( yaxis )
        y_next = dequeue(y);
    work(y_next);
}
```

<u>Mutual exclusion</u>. Only one thread at a time can enter a *critical* region.

Doc. 📃

```
OpenMP: critical
```

1 **#pragma** omp critical

	omp critical	omp single
Meaning	Run code segment one by one by all threads	Run code segment once by any thread
Number of times code is executed	Number of threads	Only one
Use case	Avoid race condition	Manage control variables or signals

Table 3: 🛕 omp critical vs omp single

```
Example 7: synchronization with critical directive
  Note the following code:
1 float res;
3 #pragma omp parallel
4 {
      float B;
5
      int i, id, nthrds, niters = big_number;
6
\overline{7}
     id = omp_get_thread_num();
8
      nthrds = omp_get_num_threads();
9
     for (i = id; i < niters; i += nthrds) {</pre>
10
         B = big_job(i);
         #pragma omp critical // threads wait their turn;
         13
     }
14
15 }
16
```

<u>Atomic</u>. Provides mutual exclusion, but only when updating a memory location. It ensures that a particular memory location is accessed atomically. It is valid only for the following statement and not for a structured block.

The statement inside the atomic must be one of the following forms:

- x binop = expr
- x++ or ++x
- x-- or --x

Where  $\mathbf{x}$  is an lvalue of scalar type and **binop** is a non-overloaded builtin operator.





## 5.5 Data environment

OpenMP is based on the shared memory programming model, so most variables are shared by default. Global variables are also shared between threads. But not everything is shared; for example, *stack variables* in functions called from parallel regions are **private**, as are *automatic variables* within a statement block.

### Example 9: data sharing

In the following code, the variable temp is private (local to each thread) because it is in the stack of the function work; meanwhile, the variables A, index, and count are shared by all threads.

```
double A[10];
2 int main() {
3
      int index[10];
      #pragma omp parallel
4
           work(index);
      printf("%d\n", index[0]);
6
  }
7
8
9
  void work(int *index) {
      double temp[10];
      static int count;
       /* other code */
12
13 }
```

We can refer to these arguments as **Data Scope Attribute Clauses** because the issue is really about the visibility and value of each data in each scope. Although OpenMP shares variables by default, there is (and it is a very common and *best practice*) the option to:

- Selectively change storage attributes for construct using the following clauses: shared, private and firstprivate.
- The final value of a private inside a parallel loop can be transmitted to the shared variable outside the loop with: lastprivate.
- The default attributes can be overridden with: default(private | shared | none)

A Note that when we say "copy" we mean the *shallow copy*, not the *deep copy*. So when the following clauses create a local copy, they create a *shallow copy*.

private clause. The statement private(var) creates a new local copy of var for each thread. The value of the private copies is *uninitialized* and also the original variable value remains unchanged after the region.

```
OpenMP: private(...)
1 #pragma omp parallel directive private(var1-name, var2-name, ...)
```

#### Example 10: private clause and dirty memory location

In the following code we try to use the private clause inside a parallel for. The code is very trivial, we set the number of threads to two for better understanding, so we start the parallel code with the for directive and the private clause. It has private\_test as a private variable. So each thread will copy the variable and the initial value will be undefined.

```
1 #include <iostream>
2 #include "omp.h"
3 #define MAX 6
4
5 int main(int argc, char const *argv[])
6 {
7
      int i, private_test = 10;
      printf("Memory location of private_test: %p\n",
8
             &private_test);
9
      // set limit to 2 threads for better understanding
10
      omp_set_num_threads(2);
      printf("Master will execute for in parallel!\n");
12
      #pragma omp parallel for private(private_test)
13
      for(i = 0; i < MAX; ++i) {</pre>
14
           // initialize private_test
          private_test = i == 0 ? 0 : ++private_test;
16
          printf(
17
               "Thread #%i, iter_i: %d, private_test: %d\n",
18
               omp_get_thread_num(), i, private_test
19
          );
20
      }
21
      printf(
22
          "private_test outside the parallel region: %d\n",
23
          private_test
      );
25
26
      return 0:
27 }
```

Unfortunately, when we examine the output, we see a problem. Thread zero (master) executes the for statement for the first 3 iterations, while thread one (slave) executes the for statement for the last 3 iterations. The zero thread behaves as expected because we initialize the private\_test variable to zero on the first for iteration (when i is 0). The thread one, has made a copy of the variable in another memory location and the value is unknown; so it continues to add a single value to each iteration in a dirty memory location. This is a trivial example that highlights the unknown values that we can find inside the private variables if we don't do any initialization.

```
1 $ g++ -fopenmp example.cpp -o example
2 $ ./example
3 Memory location of private_test: 0x7ffecdfa3aa4
4 Master will execute the for statement in parallel!
5 Thd #0, i:0, private_test:0, mem: 0x7ffecdfa3a40
6 Thd #0, i:1, private_test:1, mem: 0x7ffecdfa3a40
7 Thd #0, i:2, private_test:2, mem: 0x7ffecdfa3a40
8 Thd #1, i:3, private_test:687869953, mem: 0x76a0297ffdd0
9 Thd #1, i:4, private_test:687869954, mem: 0x76a0297ffdd0
10 Thd #1, i:5, private_test:687869955, mem: 0x76a0297ffdd0
11 private_test outside the parallel region: 10
```

firstprivate clause. The variables are initialized from the shared variable, but as in the private clause, the updated value doesn't leave the parallel region.

#pragma omp parallel directive firstprivate(var1-name, ...)

### Example 11: firstprivate clause

**OpenMP:** firstprivate(...)

A very trivial example to see how the firstprivate clause works. The variable private\_test is copied to local and initialized with the value outside the parallel region.

```
1 #include <iostream>
2 #include "omp.h"
3 #define MAX 6
4
5 int main(int argc, char const *argv[])
      int i, private_test = 10;
6
       printf("Memory location of private_test: %p\n",
7
              &private_test);
8
9
       // set limit to 2 threads for better understanding
      omp_set_num_threads(2);
      printf("Master will execute for in parallel!\n");
       #pragma omp parallel for firstprivate(private_test)
12
      for(i = 0; i < MAX; ++i) {</pre>
13
           // initialize private_test
           ++private_test;
           printf(
               "Thd #%i, i:%d, private_test:%d, mem: %p\n",
               omp_get_thread_num(), i,
18
               private_test, &private_test
19
           );
20
      }
21
      printf(
           "private_test outside the parallel region: %d\n",
           private_test
       );
25
26
       return 0:
27 }
  Note that the value is not propagated outside the parallel region.
1 $ g++ -fopenmp example.cpp -o example
2 $ ./example
3 Memory location of private_test: 0x7ffc5cd153b0
4 Master will execute for in parallel!
5 Thd #0, i:0, private_test:11, mem: 0x7ffc5cd15350
6 Thd #0, i:1, private_test:12, mem: 0x7ffc5cd15350
7 Thd #0, i:2, private_test:13, mem: 0x7ffc5cd15350
8 Thd #1, i:3, private_test:11, mem: 0x77001d9ffdd0
9 Thd #1, i:4, private_test:12, mem: 0x77001d9ffdd0
```

10 Thd #1, i:5, private\_test:13, mem: 0x77001d9ffdd0 11 private\_test outside the parallel region: 10

# Example 12: be careful with pointers using the firstprivate clause

The following code is very similar to the previous one. The difference here is that the parallel region also gets a pointer. Note that the pointer is in C style, because using the unique pointer technique (suggested in C++) will create an exception, because C++ doesn't allow the copy of a unique pointer. However, each thread creates a shallow copy of the pointer, but not a copy of the value pointed to! In this test, we use the pointer to the value of private\_test to modify the value of private\_test.

```
1 #include <iostream>
2 #include "omp.h"
3 #define MAX 6
5 int main(int argc, char const *argv[]) {
6
      bool print_flag = true;
      int i, private_test = 10;
7
      // C pointer, not a good practice in C++...
8
      // used only for the example
9
      int *ptr_private_test = &private_test;
      printf("Memory location of private_test
                                                    : %p\n".
             &private_test);
12
      printf("Memory location of ptr_private_test: %p\n",
13
             &ptr_private_test);
14
      // set limit to 2 threads for better understanding
      omp_set_num_threads(2);
16
      printf("Master will execute for in parallel!\n\n");
      #pragma omp parallel for firstprivate(private_test,
18
      ptr_private_test, print_flag)
      for(i = 0; i < MAX; ++i) {</pre>
19
          if (print_flag) {
20
               printf("Memory location ptr %p\n",
21
                     &ptr_private_test);
22
               print_flag = false;
23
          }
24
          // increase value pointed to by ptr
25
           ++*ptr_private_test;
26
           // increase simple variable
27
28
          ++private_test;
          printf(
29
              "Thread #%i, i:%d\n- private_test:%d,
30
      ptr_private_test:%d, mem: %p\n\n",
              omp_get_thread_num(), i, private_test,
31
32
               *ptr_private_test, &private_test
          );
33
      }
      printf(
35
           "private_test outside the parallel region: %d\n",
36
           private_test
37
38
      );
39
      return 0:
40 }
```

Note an interesting observation. The variable private\_test is incremented at each iteration; in the same way, the value pointed to by the pointer ptr\_private\_test is also incremented. Finally, the variable  $private_test$  is modified because the pointer was copied in each thread and each slave, including the master, increased the value. This is a very bad practice and we want to suggest to use unique pointers of C++ or to avoid shallow copies.

```
1 Memory location of private_test
                                     : 0x7fff3849c224
2 Memory location of ptr_private_test: 0x7fff3849c228
3 Master will execute for in parallel!
5 Memory location ptr 0x7fff3849c1a0
6 Thread #0, i:0
7 - private_test:11, ptr_private_test:11, mem: 0x7fff3849c198
9 Thread #0, i:1
10 - private_test:12, ptr_private_test:12, mem: 0x7fff3849c198
12 Thread #0, i:2
13 - private_test:13, ptr_private_test:13, mem: 0x7fff3849c198
14
15 Memory location ptr 0x7b710cfffdb0
16 Thread #1, i:3
17 - private_test:11, ptr_private_test:14, mem: 0x7b710cfffda8
18
19 Thread #1, i:4
20 - private_test:12, ptr_private_test:15, mem: 0x7b710cfffda8
21
22 Thread #1, i:5
23 - private_test:13, ptr_private_test:16, mem: 0x7b710cfffda8
24
25 private_test outside the parallel region: 16
```

The expected value for private\_test should remain 10 because the firstprivate doesn't affect the values of the variables after the parallel region, but in this case we are using a pointer and a bad practice.

lastprivate clause. The variables update shared variables with the value from the last iteration, so the order of execution of the threads is important here.



```
int i, private_test = 10;
6
       printf("Memory location of private_test: %p\n",
7
               &private_test);
8
9
       // set limit to 2 threads for better understanding
       omp_set_num_threads(2);
11
       printf("Master will execute for in parallel!\n");
       #pragma omp parallel for lastprivate(private_test)
for(i = 0; i < MAX; ++i) {</pre>
12
            // initialize private_test
14
            private_test = i;
16
            printf(
17
                 "Thd #%i, i:%d, private_test:%d, mem: %p\n",
                omp_get_thread_num(), i,
18
19
                private_test, &private_test
            );
20
       }
21
22
       printf(
            "private_test outside the parallel region: %d\n",
24
            private_test
       );
25
       return 0;
26
27 }
  The private_test variable initially has a value equal to 10, but with
  lastprivate we have overwritten it.
1 Memory location of private_test: 0x7ffc4c82b8c0
2 Master will execute for in parallel!
3 Thd #0, i:0, private_test:0, mem: 0x7ffc4c82b860
4 Thd #0, i:1, private_test:1, mem: 0x7ffc4c82b860
5 Thd #0, i:2, private_test:2, mem: 0x7ffc4c82b860
6 Thd #1, i:3, private_test:3, mem: 0x72c7dddffdd0
7 Thd #1, i:4, private_test:4, mem: 0x72c7dddffdd0
8 Thd #1, i:5, private_test:5, mem: 0x72c7dddffdd0
9 private_test outside the parallel region: 5
```

<u>default clause</u>. The default storage attribute is default(shared). To change the default we can write simply the value shared or none inside the brackets:

• default(share) is the default choice for OpenMP, so there is no need to use it except for the clause pragma omp task.

	OpenM	<b>P:</b> d	efault(sh	are)		
1	#pragma	omp	parallel	directive	default(share)	

Against the **private** clauses, if we want to share some variables, we can use **shared** clause.



• default(private), each variable in the construct is made private as if specified in private clause.



• default(none), no default for variables in static extent. Must list storage attribute for each variable in static extent. It is a good programming practice.



Example 14: default(none)

```
1 #include <iostream>
2 #include "omp.h"
3 #define MAX 6
4
5 int main(int argc, char const *argv[]) {
      double private_test = 10.0;
6
      int i;
7
      // set limit to 2 threads for better understanding
8
9
      omp_set_num_threads(2);
      #pragma omp parallel for default(none) private(i,
10
      private_test)
      for(i = 0; i < MAX; i++) {</pre>
12
           private_test = i;
13
           printf(
                "Thread #%i, value: f n,
14
                omp_get_thread_num(), private_test
15
           );
16
      }
17
18
      printf(
           "private_test outside the parallel region: f\n"
19
       ,
20
           private_test
      );
21
22
      return 0;
23 }
1 Thread #0, value: 0.000000
2 Thread #0, value: 1.000000
3 Thread #0, value: 2.000000
4 Thread #1, value: 3.000000
5 Thread #1, value: 4.000000
6 Thread #1, value: 5.000000
7 private_test outside the parallel region: 10.000000
```

## 5.6 Memory model

OpenMP supports a **shared memory model**. It is a model where **all threads share an address space**, but it can get complicated, for example in the following example (picture) we can see a shared space that is also in the cache of process 3; so how can we manage this situation? What are the methods to adapt? Furthermore, what happens when a thread modifies a shared address space? How does the system behave?



In general, a memory model is defined in terms of:

- <u>Coherence</u>: behavior of the memory system when a single address is accessed by multiple threads.
- **Consistency**: read, write, or synchronization (RWS) orders with **differ**ent addresses and through multiple threads.

Remark: what the compiler does at the low level

When we write a program and ask the compiler to compile it, it does a lot of "magic" under the hood.

- 1. Our source code is decoded into very low level operations. These operations respect the order of the high-level operations of our code.
- 2. The compiler, smarter then us, tries to optimize the code while creating the executable code; so it reorders the low-level operations that are **semantically equivalent** to our program, but often allow to gain performance.
- 3. During the execution of the code, if it is parallel, some threads are created and each of them has a private memory address.
- 4. Finally, each thread writes/reads from memory, also called the commit order, using some rules.



At any given time, the private view seen by a thread may differ from the view in shared memory. For this reason, there are **consistency models** that **define constraints on the order of RWS** (Reads, Writes, Synchronizations) **operations**.

In general, a multiprocessor adopts the **Sequential Consistency Model**. It says that given n operations (RWS), they are sequentially consistent if:

- They remain in *program order* for each processor.
- They are seen to be in the same overall order by each of the other processors.

Also, in a sequential consistency model, program order is the same as code order and commit order.

OpenMP uses a **Relaxed Consistency Model** where the **compiler cannot reorder synchronization operations with read or write operations on the same thread**. The consequences are:

- ✓ All threads have the same view of memory at specific points in the code, called *Consistency Points*.
- ✓ Between two consistency points, each thread has its own temporary view of memory, which may be different from the other temporary views of other threads.

- $\checkmark$  Data are read-only, this guarantee to avoid consistency issues.
- ✗ Shared data that need to be modified can create possible race conditions.

<u>flush directive</u>. Defines a *sequence point* at which a **thread is guaranteed** to see a consistent view of memory with respect to the flush-set. The flush-set means *all thread visible variables* for a flush construct without an argument list, and it also means a list of variables when the flush(list) construct is used. The action of flush is to guarantee that:

- All read/write operations that overlap the flush-set and occur before the flush will be completed before the flush is executed.
- Any read/write operations that overlap the flush-set and occur *after* the flush will not be performed until after the flush.
- Flushes with overlapping flush-sets can not be reordered.

In other words, the flush forces data to be updated in memory so that other threads see the most recent value.

Doc. 📃

transme own fluck fluck act		OpenMP: flush			
"pragma omp riusn juusn-sei	1	#pragma omp flush <i>flush-set</i>			

A flush operation is **implied** by default by OpenMP synchronizations:

- At entry/exit of parallel/critical regions;
- At implicit and explicit barriers;
- At exit from work-sharing constructs, unless nowait is specified.

And it is **not implied**:

- At entry of work-sharing constructs;
- At entry and exit of master.

## 5.7 Nested Parallelism

## **?** How does OpenMP create multiple threads?

OpenMP uses a **fork-join model** of parallel execution. When a thread encounters a **parallel** construct, the **thread creates a team composed of itself** and **some additional** (possibly zero) **number of threads**. The encountering **thread becomes the** *master* **of the new team**. The **other threads of the team** are **called** *slave* threads of the team.



Figure 21: OpenMP fork-join model.

## • What is the life history of each thread (*slave*) created?

All team members execute the code inside the **parallel** construct. When a thread finishes its work within the parallel construct, it waits at the implicit barrier at the end of the parallel construct. When all team members have arrived at the barrier, the threads can leave the barrier. The *master* thread continues execution of user code beyond the end of the **parallel** construct, while the *slave* threads wait to be summoned to join other teams.

OpenMP **parallel regions can be nested inside each other**. If nested parallelism is:

- **Disabled**, then the **new team** created by a thread encountering a parallel construct inside a parallel region **consists only of the encountering thread**.
- Enabled, then the new team may consist of more than one thread.

### United Weights The Analysian Strength The Strength Strengt Strengt Strength Strength Strength Strength Strength Strengt

The OpenMP runtime library maintains a pool of threads that can be used as *slave* threads in parallel regions. When a thread encounters a parallel construct and needs to create a team of more than one thread, the thread will check the pool and grab idle threads from the pool, making them *slave* threads of the team. The *master* thread might get fewer *slave* threads than it needs if there is not a sufficient number of idle threads in the pool. When the team finishes executing the parallel region, the *slave* threads return to the pool.

### Summary

- 1. **Parallel construct**. Our main thread starts to execute our code. It encounters a **parallel** construct.
- 2. Pool verification. The OpenMP library checks its pool of threads. If within its pool of available threads have something of disposable, it allocates the *slave* (thread requested) to the *master* (thread that want to create the team). We refer to a single thread, but obviously this can be extended to multiple thread request (e.g. *master* thread requests 3 threads to OpenMP). Finally, the number of requested *slaves* cannot always be satisfied; OpenMP guarantees the best, so it continues to give the requested threads to the applicants. If it cannot satisfy the request, it returns the maximum number of *slaves* it can satisfy (e.g. *master* requests 4 threads, but OpenMP has a pool of only 2 threads available; therefore it returns 2 *slaves*).
- 3. Assign and start execution. Ideally, OpenMP returns the number of threads requested by the *master*. Otherwise, it returns the maximum number. The team now consists of the main thread, called the *master*, and its *slaves*. Each member of the team executes the code specified by the programmer within the parallel construct.
- 4. End of execution of a thread. A thread of the team finishes its work. It can finally rest, and its state changes from "running" to "waiting". It waits for its other thread friends. Each thread has an implicit barrier at the end of the parallel construct.
- 5. Any thread finish. Finally, each thread finishes its work. The *master* releases each member of the team to the OpenMP library. OpenMP updates its thread pool with the returning threads, and the *master* thread continues its life independently from the released threads.

The previous flow works if and only if nested parallelism is enabled. Otherwise, if a *master* asks to create a new team, it will ignore the request and tell the requester to continue alone.

## X Implementation

Nested parallelism can be enabled or disabled by passing true or false as arguments to the runtime function:

Doc. 🔳

	OpenMP: omp_set_nested
1	<pre>void omp_set_nested(int nested)</pre>

We can set a default number of threads at different levels of nested parallelism with:

OMP\_NUM\_THREADS = [list, of, integers]

If the nesting level is deeper than the number of entries in the list, the last value is used for all subsequent nested parallel region.

- OMP\_MAX\_ACTIVATE\_LEVELS defines the upper limit on the number of active parallel regions that may be nested.
- OMP\_THREAD\_LIMIT avoids that recursive applications create too many threads.

Finally, since we are in nested parallelism, the thread number returns the thread number partially and not globally, we need other useful functions:

• Returns the maximum number of OpenMP threads available in contention group:

OpenMP: omp\_get\_thread\_limit

int omp\_get\_thread\_limit()

• Returns the maximum number of nested active parallel regions when the innermost parallel region is generated by the current task.

Doc. 📃

Doc. 🚍

OpenMP: omp\_get\_max\_active\_levels

• Limits the number of nested active parallel regions when a new nested parallel region is generated by the current task.

Doc. 📃



• Returns the number of nested parallel regions on the device that enclose Doc. 📃 tha task containing the call.  $\overline{\mathbf{OpenMP}}:$  omp\_get\_level int omp\_get\_level() • Returns the number of active, nested parallel regions on the device enclos-Doc. 📃 ing the task containing the call. **OpenMP:** omp\_get\_active\_level int omp\_get\_active\_level() • Returns, for given nested level of the current thread, the thread number Doc. 📃 of the ancestor of the current thread.  $OpenMP: \verb"omp_get_ancestor_thread_num"$ int omp\_get\_ancestor\_thread\_num(int level) • Returns, for a given nested level of the current thread, the size of the thread team to which the ancestor of the current thread belongs. Doc. 📃 **OpenMP:** omp\_get\_team\_size int omp\_get\_team\_size(int level)

## 5.8 Cancellation

As of OpenMP 4.0, a thread can be cancelled using a combination of two commands:

• cancel construct cancels the innermost enclosing region of the specified type.

In other words, it allows us to cancel the current thread. But be careful! The directive only allows to set the cancellation flag to a value of one. So it is necessary to also use the cancellation point command or the thread must hit a barrier (implicit or explicit).

The syntax of the cancel construct is as follows:

Doc. 📃

	OpenMP: pragma omp cancel			
1	<pre>#pragma omp cancel construct-type-clause Where construct-type-clause is one of the following: parallel, sections, for, taskgroup.</pre>			

• The cancellation point construct introduces a user-defined cancellation point at which implicit or explicit tasks check whether cancellation of the innermost enclosing region of the specified type has been enabled.

In other words, when a thread encounters the cancellation point, the cancellation flag has been checked. The thread execution is stopped. This is an explicit cancellation request because there are other points where cancellation flag is checked, such as at another cancel region or at a barrier.

Doc. 📃

```
OpenMP: pragma omp cancellation point

  #pragma omp cancellation point
```

Since there is an **overhead in checking for cancellation**, it can be enabled manually using the OMP\_CANCELLATION environment variable (false by default).

#### A Immediate cancellation is not guaranteed

OpenMP does not guarantee that cancellation will result in immediate termination.

### ✓ When to use?

When there is a **need to stop the execution**, such as in the **divide-and-conquer algorithms** (for example, to stop a search when we find the element), or when we **need to handle some errors**.

# 5 OpenMP v5.2

### Example 15: thread cancellation

Assume that from a certain point in our algorithm there are 5 threads alive (including the *master*), and the construct pipeline is as follows.



Thread 3 hits a cancellation point, but there is no cancel directive before it, so the cancellation flag is set to zero by default and the thread hasn't been broken.



Thread 1 requests the cancellation and waits for a synchronization point, such as a barrier or an cancellation point. From that point on, it is idle and waits.



Thread 0 calls a cancellation point to check the flag and terminates because thread 1 (last step) has set the cancellation flag to 1. At this point, thread 1, which was waiting for a synchronization point, also terminates.



At the same time, thread 2 is cancelled because the cancel directive checks the cancellation flag first.



At this point the thread 3 has been terminated.



Finally, thread 4 never encounters a cancellation point and finishes execution normally.

## 5.9 SIMD Vectorization

A SIMD processor exploits data parallelism by providing instructions that operate on blocks of data (called vectors). SIMD provides data parallelism at the instruction level and can be combined with other OpenMP constructs to achieve multi-level parallelism.

# What compilers must do to understand whether a loop can be vectorized

SIMD instructions use **SIMD registers**. The compilers deal with **several** issues to determine whether a loop can be vectorized by **SIMD** instructions. It does:

- An analysis of the dependencies across iterations;
- An alias analysis of pointers;
- An analysis of the data layout/alignment issues;
- An analysis of conditional executions;
- Checks of the loop bounds that must not be multiple of vector length.

### Other compiler problems: Loop Peeling and Loop Tail

Also, the **loop iterations at the beginning and end may not be vec-torized** (loop peeling, tail). This is because when a compiler tries to optimize a loop using vectorization (i.e., applying the same operation to multiple data points simultaneously to speed up execution), it often encounters problems with the iterations at the beginning and end of the loop. These iterations may not fit neatly into the vectorized operations because the total number of iterations of the loop may not be a perfect multiple of the vector length.

Essentially, the compiler may have to split the loop into three parts:

- 1. Loop Peeling. Handle the initial few iterations that don't align with vector boundaries.
- 2. Vectorized Main Loop. Process the majority of the loop iterations using vectorized operations.
- 3. Loop Tail. Handle the remaining iterations that can't be processed with vector operations due to their small number.

This approach ensures that the loop is as optimized as possible, even if some parts of it cannot be vectorized efficiently.

## 💥 Use OpenMP SIMD

The simd construct can be applied to a loop to indicate that the loop can be transformed into a SIMD loop (i.e., multiple iterations of the loop can be executed simultaneously using SIMD instructions).

Doc. 📃

OpenMP: p	cagma omp simd
1 #pragma_omp	simd
· pragma omp	

The loop is divided into chunks, and all iterations are executed by a single thread using SIMD vector instructions. The chunks should fit into a vector register for performance, and each iteration is executed by a *SIMD lane*. The compiler will generate SIMD instructions, it is up to the user to ensure this maintains correct behavior.

## Possible clauses

- Data scope clauses (page 79) can be used in a simd directive.
- A collapse clause can be used to fuse two perfectly nested loops, but the complexity can be increase.
- The simdlen(*size*) clause suggests a **preferred vector length**. Maybe the code will work better with a specific vector length, but the compiler is free to ignore it (is only a suggestion make by the programmer). It can also hurt performance but the results remain correct.
- The safelen(*size*) clause sets an upper limit to the vector length that the compiler cannot exceed.

## For SIMD

The omp for simd directive distributes the iterations of one or more associated loops across the threads that already exist in the team and indicates that the iterations executed by each thread can be executed concurrently using SIMD instructions.

	OpenMP: pragma omp for simd	
1	<pre>#pragma omp for simd</pre>	

The number of threads and scheduling policy greatly affect performance. If the number of threads increases, work for each thread is smaller. Each thread should work with a chunk corresponding to the vector length. Ideally, it is correct to distribute iterations among threads in a team, then each thread uses SIMD instructions. The clause schedule avoid performance degradation specifying the scheduling type and chunk size for the loop iterations. The static schedule divides the iterations into chunks of *chunk-size*, distributing them to the threads.



Finally, we can also declare a function to be compiled for calls inside a SIMD loop.

```
OpenMP: pragma omp declare simd

#pragma omp declare simd
/* function definition */
```

# 6 GPU Architecture

## 6.1 Introduction

In the image below, we can see a very basic GPU architecture:



• **GPU Structure** (left). The GPU is made up of a **grid of** smaller blocks, each representing a **core**. All the blocks form a **multi-core structure** that allows the GPU to handle many tasks simultaneously.

Within a **single core**, the GPU uses **SIMD** (Single Instruction, Multiple Data) **execution**. This means that many execution units within a core can simultaneously execute the same instruction on different pieces of data. This results in highly efficient execution of parallel tasks such as rendering graphics or running simulations.

In addition, **each core supports multi-threaded execution**, which allows multiple threads to be processed simultaneously. This further enhances the GPU's ability to perform multiple tasks simultaneously.

• Memory Connection (right). The GPU is connected to DDR5 DRAM, a type of dynamic random access memory. Fast memory is essential to handle the large amounts of data that GPUs process. The more powerful the DRAM, the faster the data transfer.

Initially, GPUs were designed with a specific purpose: to render graphics quickly and efficiently. However, their role has expanded significantly over the years.

**General-Purpose computing on Graphics Processing Units (GPGPU)** was originally designed to **render graphics**, but GPUs have evolved to perform a wide range of computations beyond traditional graphics tasks. GPGPU takes advantage of the parallel processing capabilities of GPUs to perform computations typically handled by the CPU.

## 6.2 GPU compute mode

**GPU compute mode** refers to **GPU hardware that is optimized for general-purpose computing rather than graphics rendering**. This mode allows users to run non-graphics programs on the GPU's programmable cores, taking advantage of the GPU's parallel processing capabilities for tasks such as scientific simulations, data analysis, and machine learning.

### Example 1: how to run code on a GPU (prior to 2007)

Now let us see how to run a simple code on a GPU. Suppose a user wants to draw a picture on a GPU:

- GPU Shader Program Binaries. The application, via the graphics driver, supplies the GPU with shader program binaries. These are compiled programs that the GPU will execute to perform rendering tasks.
- Graphics Pipeline Parameters. The application sets various parameters for the graphics pipeline, such as the output image size, to control how the rendering should be processed.
- Vertex Buffer. The application provides the GPU with a buffer of vertices. Vertices are data points that define the shape of the objects to be rendered.
- Draw Command. The application sends a draw command to the GPU using the function call drawPrimitives(vertex\_buffer). This command instructs the GPU to start rendering using the provided vertex data.

The stages of the graphics pipeline:

- 1. **Input Vertex Buffer**: The initial stage where the vertex data is input to the pipeline.
- 2. Vertex Generation: Vertices are generated or fetched from the vertex buffer.
- 3. Vertex Processing: The vertices undergo various transformations and shading calculations.
- 4. **Primitive Generation**: The processed vertices are used to generate geometric primitives (such as triangles).
- 5. Fragment Generation (Rasterization): The primitives are converted into fragments (potential pixels).
- 6. **Fragment Processing**: Fragments undergo shading and texturing calculations to determine their final color and properties.
- 7. **Pixel Operations**: Final operations are performed on the fragments, such as depth testing and blending.
- 8. **Output Image Buffer**: The processed fragments are written to the output image buffer, resulting in the final rendered image.

## **D** Some history

Before 2007 the only way to interface with GPU hardware was through the graphics pipeline. This meant that GPUs were *designed and used specifically for tasks related to graphics rendering*. The pipeline stages (such as vertex processing, fragment generation, and pixel operations) were all designed to transform vertex data into pixels displayed on the screen.

Because they were optimized to handle parallel tasks associated with rendering images, their architecture and interfaces were tightly coupled with graphics APIs.

By 2007, the concept of using GPUs for General-Purpose computing on Graphics Processing Units (GPGPU) was emerging. Thanks mainly to the introduction of a new architecture signed NVIDIA called Tesla and CUDA, a parallel computing platform and programming model (also OpenCL was emerging).

The **NVIDIA Tesla architecture**, introduced with the GeForce 8800 GPU in 2006, marked a significant shift in GPU design by unifying graphics and computing capabilities. This architecture featured a scalable parallel array of processors that could be programmed in C or via graphics APIs2. The Tesla architecture enabled **flexible**, **programmable graphics and high-performance computing**, making it possible to use GPUs for a wide range of applications beyond traditional graphics rendering. This unification enabled massive multithreading and parallel processing, dramatically improving performance for computationally intensive tasks. [7]

From this point on, the programmable cores of the GPU are used:

- Application could allocate buffers in GPU memory and copy data to/from buffers;
- Application (via the graphics driver) provides a single kernel program binary to the GPU;
- Application tells GPU to run kernel in SPMD fashion.

## 6.3 CUDA

6.3.1 Basics of CUDA

• What is CUDA?

**Compute Unified Device Architecture (CUDA)**, is a **parallel computing platform and Application Programming Interface** (API) **model** created by NVIDIA. It allows developers to utilize NVIDIA GPUs for generalpurpose processing, enabling them to perform a wide range of computations more efficiently than with traditional CPU processing alone.

CUDA was introduced with the NVIDIA Tesla architecture, which marked a significant shift in GPU capabilities, enabling general purpose computing on GPUs. **CUDA is designed to be similar to the C programming lan-guage**, making it familiar to many developers. It allows programmers to write code that runs on GPUs using the compute-mode hardware interface.

CUDA's abstractions are relatively low-level and closely match the performance characteristics and capabilities of modern GPUs. This design goal helps maintain a low abstraction layer, ensuring that developers can take full advantage of the hardware's potential.

Note that **Open Computing Language (OpenCL)** is an open standards version of CUDA that runs on both CPUs and GPUs from multiple vendors. While CUDA runs only on NVIDIA GPUs, OpenCL is designed to be more versatile and work on hardware from multiple vendors.

### **?** CUDA Thread Hierarchy

CUDA organizes threads into a hierarchical structure to efficiently manage parallel computations on GPUs. To understand how it works, let's look at it from the deepest level up:

1. Threads. Threads (or CUDA Threads) are the smallest unit of execution in CUDA. Each thread runs a single instance of a kernel function<sup>8</sup>.

Threads are **identified by their unique thread IDs**, which are used to calculate memory addresses and control decisions.

2. Thread Blocks. Threads are grouped into blocks (called also CUDA Blocks). Each block can contain multiple threads that execute concurrently.

Threads within the same block can communicate and share data through shared memory and synchronization primitives like barriers and atomic operations.

The *maximum number* of threads per block is limited by the GPU architecture, typically up to 1024 threads per block.

 $<sup>^{8}\</sup>mathrm{A}$  kernel function in CUDA is a function that runs on the GPU (device) but is called from the CPU (host). These functions are executed by many parallel threads on the GPU

3. Grids. Blocks are organized into a grid (called also CUDA Grids). A grid is a collection of blocks that execute the same kernel function.

All threads in a grid share the same global memory space.

The grid can be multi-dimensional, allowing for flexible organization of blocks to match the problem's dimensions.

Note that CUDA uses the x, y, and z dimensions for threads, blocks, and grids because this **multi-dimensional structure** aligns well with many common computational problems. Many computational problems naturally fit into a multi-dimensional space. For example, image processing involves 2D data, and volumetric simulations involve 3D data.



Figure 22: The figure shows an example of a CUDA grid consisting of 6 blocks, each block consisting of 12 threads. The number of threads and the number of blocks per column/row are customizable, this is just an example. In total, there are 72 CUDA threads (12 threads per block times 6 blocks in the grid).

## **CUDA Kernels**

A **CUDA kernel** is a **function that gets executed on the GPU**. It contains the parallel portion of the application, which is executed by multiple threads in parallel. Unlike regular C/C++ functions that run on a single thread, CUDA kernels can run thousands of threads simultaneously.

### Device vs Host

In CUDA, there is a term to identify the code that runs on the CPU and GPU.

Definition 1: CUDA Host (CPU)

The **CUDA Host refers to the CPU** and its associated memory. It is **responsible for managing the overall program execution**. This includes allocating memory, launching CUDA kernels, and transferring data between the CPU and the GPU.

It is typically written in the standard programming language used (e.g., C, C++, Java, Python, etc.) and contains the logic for setting up and controlling the execution of CUDA kernels on the device.

## Definition 2: CUDA Device (GPU)

The **CUDA Device refers to the GPU** and its associated memory. It is **responsible for running parallel code** (CUDA kernels) and **performs the bulk of the computation**. This takes advantage of the parallel processing power of the GPU.

The device code (kernels) is written in the CUDA programming language and is designed to run on the multiple parallel cores of the GPU.

## Horizonta Series CUDA Syntax

Here is a sample code written in CUDA:

```
1 #include <cuda_runtime.h>
2 #include <iostream>
3 #define Nx 12
4 #define Ny 6
6 // Kernel definition
7 __global__ void MatAdd(
      float A[Ny][Nx],
8
9
      float B[Ny][Nx],
      float C[Ny][Nx]
10
11 ) {
      int i = blockIdx.x * blockDim.x + threadIdx.x;
12
      int j = blockIdx.y * blockDim.y + threadIdx.y;
13
      // guard against out of bounds array access
14
15
      if (i < N && j < N)</pre>
           C[i][j] = A[i][j] + B[i][j];
16
17 }
18
19 int main() {
      // Define the hierarchy
20
      dim3 threadsPerBlock(4, 3);
21
      dim3 numBlocks(
22
           Nx / threadsPerBlock.x,
23
24
           Ny / threadsPerBlock.y
      );
25
      // Kernel invocation
26
      // Assume matrices A, B, C are already allocated (dim Nx x Ny) \,
27
      MatAdd<<<numBlocks, threadsPerBlock>>>(A, B, C);
28
29 }
```

- Rows 3-4 Variables Nx and Ny define the dimensions of the matrices. In this case, they are  $12 \times 6$ .
  - Row 21 The threadsPerBlock function specifies that each block will have 4 threads in the x dimension and 3 threads in the y dimension. In other words, it defines how a block should be composed (see the figure 22).
  - Row 22 The numBlocks function defines the number of blocks required to cover the entire matrix. The number of blocks is calculated by dividing the matrix dimensions by the number of threads per block in each dimension. In other words, it defines how a grid should be composed (see the figure 22).
  - Row 28 The execution configuration syntax <<<...>>> is required to specify the number of threads per block and the number of blocks per grid (both numbers can be of type int or dim3).

The function invocation starts the MatAdd kernel with the given grid and block dimensions. This kernel runs on the GPU and performs the matrix addition.

- Row 7 Defines a kernel function called MatAdd to be executed on the GPU. The \_\_global\_\_ keyword indicates that this is a kernel function.
- Rows 12-13 Computes the global column index i for each thread. This combines the block index and the thread index within the block to get the overall position.

It also does the same with the j index.

- Row 15 The if condition ensures that the thread does not access out-of-bounds elements in the matrices.
- Row 16 Finally, it performs the element-wise addition of matrices A and B and stores the result in matrix C.

As we said in Figure 22 (page 104), the example spawns 72 CUDA threads.

### 6.3.2 Memory model

The CUDA memory model consists of several types of memory, each with different characteristics and uses. In general, the **Host (CPU) and the Device (GPU) have different address spaces**, each one has its private memory address.

For example, the cudaMemcpy function in CUDA is used to copy data between different memory spaces, specifically between host (CPU) memory and device (GPU) memory.

```
1 // allocate buffer in host mem
2 float* A = new float[N];
4 // populate host address space pointer A
5 for (int i = 0; i < N; ++i) {
      A[i] = (float)i;
6
7 }
9 // allocate buffer in device (GPU) address space
10 int bytes = sizeof(float) * N;
11 float* deviceA:
12 cudaMalloc(&deviceA, bytes);
13
14 // populate deviceA
15 cudaMemcpy(deviceA, A, bytes, cudaMemcpyHostToDevice);
16 // deviceA:
17 //
           Destination memory address (either on the host or device).
18 //
19 // A:
           Source memory address (either on the host or device).
20 //
21 //
22 // bytes:
23 //
           Number of bytes to copy.
24 //
25 // cudaMemcpyHostToDevice:
26 //
           Type of memory copy operation.
_{27} //
           Copies data from host memory to device memory.
```

Note that directly accessing deviceA[i] is an invalid operation, because we cannot manipulate the contents of deviceA directly from host, since deviceA is not a pointer to the host's address space.

## **Types of CUDA device memory models visible to kernels**

1. **Per-thread Private Memory**. This memory is **private to each thread**. Each thread has its own memory space that other threads cannot access.

**?** Usage. It is ideal for storing variables that are only relevant to individual threads and do not need to be shared with other threads.

Access. It has fast access, limited by the number of registers available.

2. **Per-block Shared Memory**. This memory is **shared by all threads** within a block. It allows threads within the same block to cooperate by sharing data.

**?** Usage. It is useful for tasks where threads within a block need to communicate or share intermediate results. It is often used to optimize memory access patterns and reduce global memory accesses.

Access. It is much faster than global memory, but limited in size. Access is almost as fast as registers when used properly.

3. Device Global Memory. This memory is accessible to all threads across all blocks. It provides a large amount of memory, but has higher latency and lower bandwidth than shared memory.

**?** Usage. It is suitable for storing large amounts of data that must be accessed by threads in different blocks.

Access. It has the **slowest access** of the three types, but is necessary for large data storage and inter-block communication.
### 6.3.3 NVIDIA V100 Streaming Multiprocessor (SM)

The NVIDIA V100 is a powerful GPU designed for data centers, primarily used for Artificial Intelligence (AI), High Performance Computing (HPC), and data science. Meanwhile, the **NVIDIA V100 Streaming Multiprocessor (SM)** is a key component of the V100 GPU architecture.

#### **?** How is architecture composed?

See Figure 23 (page 110) for a graphical representation.

• Warp Selector and Fetch/Decode:

The *Warp Selector* and *Fetch/Decode* units are responsible for **managing the execution of warps** (groups of threads) and **decoding instructions**.

- Functional Units:
  - SIMD fp32 functional unit (Yellow).

It handles single-precision floating-point operations. Control is shared across 16 units, allowing for 16 multiply-add (MUL-ADD) operations per clock cycle. This translates to one 32-wide SIMD operation every two clocks.

- **SIMD** int functional unit (Orange).

It manages integer operations, also shared across 16 units, with the same performance characteristics as the fp32 unit ( $16 \times MUL-ADD$  per clock).

- SIMD fp64 functional unit (Brown).

It is **responsible for double-precision floating-point operations**. Control is shared across 8 units, allowing for 8 MUL-ADD operations per clock cycle, equating to one 32-wide SIMD operation every four clocks.

- **Tensor core unit** (Red).

It is **specialized for tensor operations**, which are crucial for deep learning and AI workloads.

– Load/store unit (Green).

It handles memory operations, such as loading data from and storing data to memory.

• Warp Scheduler:

The diagram below shows the scheduling of warps (Warp 0, Warp 4, Warp 60, etc.) across the functional units, indicating how different warps are processed in parallel.



Figure 23: A "sub-core" of the NVIDIA V100 Streaming Multiprocessor (SM) architecture.

# • What is a Warp?

A Warp is a group of 32 threads that execute the same instruction at the same time. Threads within a block are divided into warps. For example, a block of 256 threads would have 8 warps (256 threads / 32 threads per warp). Each SM in the V100 can schedule and interleave the execution of up to 16 warps. This means that multiple warps can be executed simultaneously, improving the overall throughput of the GPU. Finally, each warp has some registers to store the data needed by the threads.

# **?** How is a Warp executed?

Threads within a warp execute the same instruction simultaneously, taking advantage of SIMD execution to improve performance.

When threads within a warp do not share the same instruction, it results in divergent execution, which can degrade performance due to the need to serialize instructions. However, the check of the same instruction by the 32 threads is done dynamically by the GPU hardware. Finally, although not part of CUDA, understanding warps is critical to optimizing CUDA programs on modern NVIDIA GPUs.



Figure 24: A NVIDIA V100 Streaming Multiprocessor (SM) architecture.

## 6.3.4 Running a CUDA program on a GPU

The following section is dedicated to understanding the execution of the "convolve" kernel on a fictitious dual-core GPU. In other words, we present an example of a kernel function execution (and therefore GPU-executed) that implements a convolution operation. It also aims to show why memory management is also fundamental inside the GPU.

The kernel execution requirements for this explanation are:

- Each thread block must execute 128 CUDA threads.
- Each thread block must allocate  $130 \times \text{sizeof(float)} = 520$  bytes of shared memory. In other words, each thread block requires 520 bytes of shared memory.

Let's take an array of size N as **input** to the kernel function. When the kernel function is executed (launched), it generates thousands of thread blocks because the array size N is assumed to be very large.

Where:

- N/THREADS\_PER\_BLK is the number of blocks per grid.
- THREADS\_PER\_BLK is the number of threads per block, 128 CUDA threads in our case.

The main task of the *GPU Work Scheduler* is to manage the two available cores (let's say Core 0 and Core 1), where each core has its own **Fetch/Decode** units, execution context storage for 384 CUDA threads (12 warps), and shared memory storage (1.5 KB).

Note that this architecture has fictitious cores that are smaller than V100 SM cores, with fewer execution units, less support for active warps, and less shared memory.



#### **Execution**

- 1. The host (CPU) sends a command to the CUDA device (GPU), which is the execution of the kernel function.
  - **Execute**: convolve (kernel function)
  - Args:
    - -N = 128'000
    - input\_array
    - output\_array
  - Number of blocks: 1000. Note that the number of blocks is given by the formula:

Therefore, the size of the array is easily calculated as:

$$\frac{N}{128} = 1000 \implies N = 128 \times 1000 = 128'000$$

2. The *scheduler* maps *block* 0 to *Core* 0, reserving execution contexts for 128 threads and 520 bytes of shared memory to meet requirements.



3. The *scheduler* continues to map blocks to available execution contexts, so it now maps *block 1* to *Core 1*. This shows **interleaved mapping** (where the scheduler maps blocks to available execution contexts across different cores, ensuring efficient use of resources).



4. As in the previous step, there is a interleaved mapping phenomena. The scheduler maps *block* 2 to *Core* 0. But now the shared memory (*Core* 0) is saturated because three concurrent blocks allocate 520 bytes  $\times 3 = 1.56$  KB > limit (1.5 KB).



5. The scheduler assigns *block* 3 to *Core 1*. But now the shared memory of *Core 1* is also **saturated**, because three concurrent blocks allocate 520 bytes  $\times 3 = 1.5$  KB > limit (1.5 KB). So we can say that only two thread blocks fit on one core.



6. The scheduler waits for a task to complete on a block. The following figure shows block  $\theta$  completing on Core  $\theta$ . Now Core  $\theta$  is ready to host execution blocks again.





7. When the task is complete, the scheduler assigns  $block \not \downarrow$  to Core 0.

8. Thread block 2 completes on Core 0.



9. Finally, thread *block* 5 is scheduled on *Core*  $\theta$ .



The explanation is intended to illustrate a phenomenon where the GPU scheduler has to manage limited shared memory resources across multiple thread blocks.

- Shared Memory Saturation: When a GPU core's shared memory is fully occupied by existing thread blocks, new thread blocks cannot be scheduled until sufficient shared memory is freed up by the completion of some of the current thread blocks.
- Idle Periods: While the scheduler is waiting for shared memory to become available, the **GPU cores may be idle**. This doesn't mean the entire GPU is idle, but certain cores may not have new blocks to execute until resources are freed up.
- Resource Contention: This example shows how shared memory contention can affect the scheduling efficiency of a GPU. Efficient use of shared memory is critical to maximizing GPU performance.
- The concept of **resource contention**, whether it be shared memory, registers or other resources, is well known in parallel computing and GPU programming. It highlights the **importance of optimizing memory usage to avoid bottlenecks and ensure efficient execution**.

The example demonstrates how GPUs must juggle limited resources while maximizing throughput, a key aspect of parallel computing. By showing that the scheduler must wait before allocating new blocks, it emphasizes the **importance of careful resource management in kernel design and execution**.

#### 6.3.5 Implementation of CUDA abstractions

We assume that we have a fictitious **Streaming Multiprocessor (SM) core** (Figure 23 page 110, same as NVIDIA V100, page 109) with only **four warps** of parallel execution in hardware. So there are 4 warps times 32 threads, and **128 threads** can be executed in parallel each time.



Figure 25: Streaming Multiprocessor (SM) core, with 4 warps and 128 threads in total.

# **?** Why allocating all threads in a block might be inefficient

Now imagine we want to run a CUDA program where a thread **block** consists of **256** CUDA threads, even though our GPU architecture can *only* execute 128 threads at a time. A naive implementation might execute the entire CUDA block by executing four warps (threads 0-127) to completion, and then execute the next four warps (threads 128-255) to completion. This sequential execution of warps can lead to inefficiencies because there may be idle periods where some warps are stalled waiting for memory accesses or synchronization points.

#### Use interleaving execution

A good alternative is to use interleaved execution. Interleaved execution means that the **GPU** schedules warps so that they overlap. While some warps are waiting for memory access or synchronization, others can execute. This overlapping helps to hide latencies and keep the **GPU** cores busy.

However, CUDA kernels can create dependencies between threads in a block. To manage these dependencies, the programmer can use the function \_\_syncthreads() to synchronize threads within a block. \_\_syncthreads() ensures that all threads in the block reach the synchronization point before any thread can continue. This means that threads 128-255 cannot continue until threads 0-127 reach the synchronization point.

# Why interleaving execution is optimal when there are dependencies

If we run four warps to completion before starting the next four, we **may not be using shared resources** (such as shared memory and execution units) efficiently. This can also **lead to scenarios where some warps are stalled indefinitely waiting for other warps to reach synchronization points**, causing potential <u>deadlocks</u> or inefficiencies.

By interleaving the execution of warps, the GPU can better manage thread dependencies, hide latencies, and make more efficient use of its resources.

```
1 #define THREADS_PER_BLK 256
  __global__ void convolve(int N, float* input, float* output)
{
3
4
       __shared__ float support[THREADS_PER_BLK * 2];
int index = blockIdx.x * blockDim.x + threadIdx.x;
5
6
       support[threadIdx.x] = input[index];
8
       if (threadIdx.x < N) {</pre>
9
            support[
                 THREADS_PER_BLK + threadIdx.x
12
            ] = input[index + THREADS_PER_BLK];
       }
13
14
       __syncthreads();
15
16
       float result = 0.0f; // thread-local
17
       for (int i = 0; i < 5; i++)</pre>
18
            result += support[threadIdx.x + i];
19
20
       output[index] = result;
21
22 }
```

# E Summary

- 1. Thread blocks can be scheduled in any order by the system.
  - The system assumes no dependencies between blocks.
  - Blocks are logically concurrent, similar to ISPC tasks (Implicit SPMD Program Compiler, page 31).
- 2. CUDA threads in the same block run concurrently (live at the same time).
  - When a block begins executing, all threads exist and have register state allocated.
  - A CUDA thread block is an SPMD (Single Program, Multiple Data) program, similar to an ISPC gang of program instances.
  - Threads in a thread block are concurrent, cooperating "workers".

## 3. CUDA implementation.

- An NVIDIA GPU warp has performance characteristics *similar* to an ISPC gang of instances.
- All warps in a thread block are scheduled onto the same SM (Streaming Multiprocessor), allowing for high-bandwidth, low-latency communication through shared memory variables.
- When all threads in a block complete, block resources (shared memory allocations, warp execution contexts) become available for the next block.

#### 6.3.6 Advanced thread scheduling

The *main goal* of this section is to show how a CUDA kernel uses hardware execution resources: thread block allocation to execution resources, execution resource capacity constraints, and zero-overhead thread scheduling.

In general, **CUDA thread blocks execute independently and can run** in any order. The hardware is free to assign blocks to any processor at any time. This flexibility allows the GPU to optimize resource utilization and balance the load. A kernel (the function that runs on the GPU) scales to any number of parallel processors. This means that the same code can run efficiently on GPUs with different numbers of cores.

Thread blocks are the basic unit of work in CUDA and are assigned to SMs in block granularity (as we saw in Chapter 6.3.4). This means that a **thread block cannot be split across multiple SMs, but is executed entirely within a single SM**. Each SM has a *limit* on the number of threads and thread blocks it can support simultaneously. For example, the **Volta SM can handle up to 2048 threads**. The number of blocks an SM can hold depends on the number of threads per block:



- If a block has 256 threads, up to 8 blocks can fit  $(256 \times 8 = 2048 \text{ threads})$ .
- If a block has 512 threads, only 4 blocks can fit  $(512 \times 4 = 2048 \text{ threads})$ .

The SM manages the indexes of the threads and blocks assigned to it, enabling scheduling and execution.

#### Von Neumann model with SIMD units

The Von Neumann Model consists of a Control Unit, ALU (Arithmetic Logic Unit), Registers, Memory, and I/O components that work in a sequential manner. However, when we integrate SIMD (Single Instruction, Multiple Data) units into the model, we add the ability to process multiple data items simultaneously using a single instruction.

As we have explained in the section 2.1.3 page 25, SIMD allows the same operation to be performed on multiple pieces of data in parallel. This means a Control Unit (CU) sends the same instruction to multiple ALUs, each working on different data at the same time.

## Von Neumann model with SIMD units in GPUs

The architecture uses SIMD units to execute multiple threads in parallel, making GPUs highly efficient at tasks involving large data sets, such as image processing, matrix multiplication, and other data-parallel computations.

Warps (groups of 32 threads) are executed in a SIMD fashion. All threads in a warp perform the same operation, but on different pieces of data. This is critical for speeding up computations that need to process large amounts of data in parallel. SIMD capabilities allow GPUs to efficiently handle large numbers of parallel tasks, making them far more powerful than traditional CPUs for certain workloads, such as graphics rendering and scientific computing.



(SIMD)

Figure 26: Von Neumann model with SIMD units.

However, these features are implementation choices, not part of the CUDA programming model. Therefore, future GPUs may have different numbers of threads in each warp.

#### Example 2: Warp

If 3 blocks are assigned to a Streaming Multiprocessor (SM) and each block has 256 threads, how many warps are there in an SM? Since each warp is made up of 32 threads, if a block is made up of 256 threads, then 8 warps are required for each block:

$$\frac{\text{Threads per block}}{\text{Threads per warp}} = \frac{256}{32} = 8$$

Since the number of blocks to be allocated is 3, if each block requires 8 warps, there are  $8 \times 3 = 24$  warps inside a single SM.

#### Zero-Overhead Warp Scheduling [11]

Zero-Overhead Warp Scheduling is a feature of NVIDIA's GPUs that allows efficient management of thread execution without significant performance penalties. This mechanism is obviously implemented in the Streaming Multiprocessor architectures.

- Warp Status. Each warp has a state that can be:
  - Eligible: the warp is ready to execute its next instruction because all the *necessary operands are available* (ready for consumption).
  - Not Eligible: the warp cannot execute its next instruction because it is *waiting for operands or other resources*.
  - **Busy**: the warp is currently running and executing instructions.

Each warp also has an associated priority value.

- The scheduler has a **Prioritized Scheduling Policy**, so it selects:
  - 1. **Highest Priority and Eligible**: the scheduler first selects warps that have the highest priority and are eligible for execution.
  - 2. Eligible Warps: if no high-priority warps are eligible, the scheduler then selects from the pool of eligible warps.
- Execution Context Switching. After that the scheduler choose a warp to run, how it can change the execution context from a warp to another?
  - Before giving the answer, it is necessary to understand that the Execution Context contains the state of all threads in a warp, such as Program Counters, register values, and other information necessary for execution. This context is <u>stored in hardware</u> resources dedicated to each warp.
  - Thus zero-overhead warp scheduling takes advantage of the power of the hardware. When the warp scheduler decides to switch from one warp to another (to hide latency or because a warp is waiting for data), it does not need to save and restore context to and from memory. Instead, it simply switches the execution state to the context of another warp, which is already stored in dedicated hardware.

This means that the switching process is very fast and has virtually no overhead, hence the term "zero-overhead"!

In other words, since all the necessary state information is already stored in the hardware, this switch is instantaneous and doesn't involve the overhead of saving/loading data to/from memory.

## Advantages

- Efficiency. By leveraging hardware resources for context storage, CUDA ensures that switching between warps incurs virtually no overhead.
- Latency Hiding. This efficient scheduling helps hide latencies and keeps the GPU's computational resources fully utilized, leading to high performance.

#### **Example 3: Matrix Multiplication on Volta Architecture**

This example illustrates the impact of different block sizes on thread utilization when performing matrix multiplication using NVIDIA's Volta GPU architecture.

With the term Block Granularity we refer to the number of threads per block. Choosing the right block size is crucial for maximizing the efficiency of GPU resources.

- In general, each Streaming Multiprocessor (SM) on the Volta architecture can handle up to 2048 threads.
- $4 \times 4$  Threads per Block:
  - Threads per Block: 16 threads  $(4 \times 4)$ .
  - Blocks per SM: the GPU can accommodate up to 32 blocks per SM.
  - Utilization: 16 threads per block mean 2048 threads would fill 128 blocks. However, since an SM can only accommodate up to 32 blocks at a time, only 512 threads will be utilized per SM (16 threads/block  $\times$  32 blocks), leading to underutilization of available threads!
- $8 \times 8$  Threads per Block:
  - Threads per Block: 64 threads  $(8 \times 8)$ .
  - Blocks per SM: with 2048 threads per SM, up to 32 blocks of 64 threads each can be allocated per SM (2048 threads per SM  $\div$  64 threads per block).
  - Utilization: this setup can utilize the full capacity of 2048 threads per SM, provided other resource limitations (such as shared memory or registers) are not a constraint.
- $30 \times 30$  Threads per Block:
  - Threads per Block: 900 threads  $(30 \times 30)$ .
  - Blocks per SM: with 2048 threads per SM, only two blocks of 900 threads each can be accommodated, resulting in 1800 threads (2  $\times$  900), which is less than the SM's maximum capacity.
  - Utilization: this configuration also leads to under-utilization because it does not utilize the full 2048 thread capacity.

The example on page 124 shows some important points to emphasize:

- Choosing Block Size: choosing the optimal block size is critical to maximizing GPU efficiency. In the previous example, a block size of  $8 \times 8$  allows full utilization of the SM's thread capacity.
- **Resource Constraints**: when choosing a block size, we must also consider other resource limitations, such as shared memory and registers, which can affect the number of threads and blocks that can be scheduled on an SM.

#### 6.3.7 Memory and Data Locality in Depth

In CUDA programming, understanding memory and data locality is crucial for achieving high performance.

### **?** Why Memory Hierarchy and Data Locality Matter

We propose a piece of code of a kernel function where there is a computation of the blur in an image:

```
1 // get the average of the surrounding 2xBLUR_SIZE x 2xBLUR_SIZE box
2 for(int blurRow = -BLUR_SIZE; blurRow < BLUR_SIZE+1; ++blurRow)</pre>
  {
3
       for(int blurCol = -BLUR_SIZE; blurCol < BLUR_SIZE+1; ++blurCol)</pre>
4
       {
5
           int curRow = Row + blurRow;
6
           int curCol = Col + blurCol;
7
           // Verify we have a valid image pixel
8
           if (curRow > -1 && curRow < h && curCol > -1 && curCol < w)
9
           Ł
               pixVal += in[curRow * w + curCol];
               // keep track of number of pixels
12
               // in the accumulated total
13
               pixels++;
14
           }
15
       }
16
17 }
18
19 // write our new pixel value out
20 out [Row * w + Col] = (unsigned char)(pixVal / pixels);
```

The code accesses global memory for input matrix elements. This is evident from the line 11 where in is likely a pointer to the global memory holding the image data. Therefore, each thread accesses global memory to read the pixel values within a 2xBLUR\_SIZE x 2xBLUR\_SIZE box around the current pixel.

- Each memory access is 4 bytes per floating point addition.
- The memory bandwidth is 4 bytes per second per FLOP, 4B/s of memory bandwidth/FLOPS.

Assuming a GPU with a peak floating point rate of 1,600 GigaFLOPS and a DRAM bandwidth of 600 GB/s, then 1,600 GigaFLOPS would require 6,400 GB/s of memory bandwidth to achieve the peak FLOPS. However, the 600 GB/s memory bandwidth limits execution to 150 GFLOPS, which is only 9.3% of the peak floating point execution rate. To get close to the 1,600 GigaFLOPS, it is necessary to drastically cut down memory accesses.

In other words, there is an **evident Memory Bandwidth Bottleneck**. Even with a high peak floating-point rate, the actual performance can be limited by memory bandwidth (to achieve 1,600 GigaFLOPS, the kernel would require 6,400 GB/s of memory bandwidth, but the available bandwidth is only 600 GB/s).

Therefore, it is important to understand that minimizing global memory access and optimizing data locality are essential strategies in CUDA programming to achieve high performance. This is because accessing global memory often results in high latency, which can significantly degrade the performance of our GPU application.

- Global memory access. Global memory is the largest and slowest memory available on a GPU. Frequent accesses to global memory can cause significant performance bottlenecks due to high latency.
- Bandwidth and Latency. While global memory provides high bandwidth, the latency associated with accessing it can slow overall performance, especially when multiple threads are accessing it simultaneously.
- Memory hierarchy. GPUs have a hierarchical memory structure that includes registers, shared memory, and global memory. Using a proper memory structure can improve performance and reduce memory bandwidth. We discussed these topics in Section 6.3.2, page 108.
- Data Locality and Caching. Optimizing data locality (keeping frequently accessed data close to where it is processed) is key to improving performance. Using shared memory to cache data that is accessed multiple times by threads can significantly reduce the need for global memory accesses.

#### Example 4: Matrix Multiplication

Matrices:

- Matrix M
- $\bullet\,$  Matrix N
- Matrix P, the resulting matrix.

In the image below, the matrices are divided into blocks with dimensions labeled as WIDTH and BLOCK\_WIDTH, indicating the block-based approach to matrix multiplication.



- The MatrixMulKernel function is defined to run on the GPU (indicated by \_\_global\_\_). It takes pointers to matrices M, N, P, and an integer Width representing the dimensions.
- Calculate Row Index (row 5). It calculates the row index of the current element in matrix P that the thread is responsible for.

- Calculate Column Index (row 8). It calculates the column index of the current element in matrix *P*.
- The if condition ensures that the thread operates within the bounds of the matrices.
- If the condition is true, initializes the Pvalue and iterates over the row of M and column of N. Each iteration accumulates the product of corresponding elements from M and N.
- Finally, stores the computed value in matrix *P*.

Since the previous example shows problems with global memory access (because accessing elements of matrices M, N, and P involves global memory), optimization (it doesn't load elements into shared memory to reduce global memory accesses), and data locality (because consecutive threads don't access successive memory locations), we propose an alternative.

### X Alternative (better) implementation of the previous example

The following figure shows how threads are mapped to elements of the output matrix P during matrix multiplication. It shows how the matrix is divided into blocks and how threads handle these blocks.



- The  $4 \times 4$  matrix P is divided into smaller  $2 \times 2$  blocks. This division helps in managing data more efficiently and improves memory access patterns.
- The BLOCK\_WIDTH is 2, indicating that each block contains  $2 \times 2$  elements.
- Each block of the matrix P is assigned to a specific thread.
  - Block(0,0) is handled by Thread(0,0).
  - Block(0,1) is handled by Thread(0,1).
  - Block(1,0) is handled by Thread(1,0).
  - Block(1,1) is handled by Thread(1,1).

# The mapping ensures that each thread is responsible for computing the values of a specific block in matrix P.

In the following figure, we illustrate an example of how elements  $P_{0,0}$  and  $P_{0,1}$  in matrix P are calculated using elements from matrices M and N.



- To compute  $P_{0,0}$ , are used elements from:
  - The first row of matrix  $M(M_{0,0}, M_{0,1}, M_{0,2}, M_{0,3})$
  - The first column of matrix  $N(N_{0,0}, N_{1,0}, N_{2,0}, N_{3,0})$

The computation involves multiplying corresponding elements and summing the results:

$$P_{0,0} = (M_{0,0} \times N_{0,0}) + (M_{0,1} \times N_{1,0}) + (M_{0,2} \times N_{2,0}) + (M_{0,3} \times N_{3,0})$$

- To compute  $P_{0,1}$ , are used elements from:
  - The first row of matrix  $M(M_{0,0}, M_{0,1}, M_{0,2}, M_{0,3})$
  - The second column of matrix  $N(N_{0,1}, N_{1,1}, N_{2,1}, N_{3,1})$

The computation involves multiplying corresponding elements and summing the results:

$$P_{0,1} = (M_{0,0} \times N_{0,1}) + (M_{0,1} \times N_{1,1}) + (M_{0,2} \times N_{2,1}) + (M_{0,3} \times N_{3,1})$$

And why is this related to storage and data locality? For three reasons:

✓ Memory Access Patterns. By dividing the matrix into blocks and assigning specific threads to handle these blocks, the computation can take advantage of memory locality. Threads working on the same block will likely access contiguous memory locations, which improves memory access efficiency.

- ✓ Shared Memory Usage. Instead of repeatedly accessing global memory, threads can load the necessary block data into shared memory once. All threads in a block can then work on the data in shared memory, significantly reducing global memory access and thus improving performance.
- ✓ Optimization for Performance. Reducing the number of global memory accesses by optimizing data locality and using shared memory can drastically improve the performance of the matrix multiplication kernel. Efficient mapping of threads to data and making use of memory hierarchy are key strategies for achieving high performance in CUDA applications.

#### E Memory/Data Locality are fundamental, now we go deep

Before explaining the keywords used by CUDA, it is important to understand the **programmer's view** of CUDA memory.



- **Host** (CPU) **Memory**. Connected to the GPU, but *distinct* from GPU memory.
- **Global Memory**. Accessible by *all threads* and the *host*. It's the *largest* but also the *slowest* type of memory.
- Constant Memory. Read-only memory accessible by *all* threads.
- Grid. Contains multiple blocks, each consisting of threads (we have already seen and discussed this in Section 2, page 103).
- Shared Memory. Faster than global memory, shared among threads within the same block.

• **Registers**. The fastest memory, local to each thread.

CUDA has specific declarations for different types of memory:

- Local Variable (int LocalVar): stored in registers, scope and lifetime are per thread.
- Shared Variable (\_\_shared\_\_ int SharedVar): stored in shared memory, scope and lifetime are per block.
- Global Variable (\_\_device\_\_ int GlobalVar): stored in global memory, scope is the entire grid, and the lifetime is the duration of the application.
- Constant Variable (\_\_constant\_\_ int ConstantVar): stored in constant memory, scope is the grid, and the lifetime is the duration of the application.

Variable Declaration	Memory	Scope	Lifetime
int LocalVar	Register	Thread	Thread
shared int SharedVar	Shared	Block	Block
device int GlobalVar	Global	Grid	Application
<pre>constant int ConstantVar</pre>	Constant	Grid	Application

Table 4: CUDA Memory Types, Scope, and Lifetime.

There are two observations to make:

- 1. The \_\_device\_\_ keyword is optional when used with \_\_shared\_\_ or \_\_constant\_\_.
- 2. The **automatic variables** (those that are automatically managed by the compiler) **reside in the registers** because they are the fastest type of memory available to threads (very close to the processor).

However, there's an exception for per-thread arrays: when we declare an array inside a kernel function, this array is unique to each thread and can be relatively large. Due to their size and potential complexity, these per-thread arrays cannot fit in registers and are stored in global memory instead.

#### • And how do I decide where to put the variables?

It depends on the implementation. The good question to ask is: *can the host access the declared variable?* 

- If the host can access the variable, it should be a global or constant variable.
  - Declared outside of a function;
  - Accessible by both host (CPU) and device (GPU).

- If the host cannot access the variable, it should be a register or shared variable.
  - Declared inside the kernel function;
  - If it is shared, it is accessible to all threads within the same block;
  - On the other hand, if it is register (local), it is only accessible to individual threads, suitable for frequently accessed variables.

# In-depth analysis of shared memory in CUDA

Some features of shared memory in CUDA:

1. Shared Memory in Each Streaming Multiprocessor (SM). Each SM in a CUDA GPU has its own shared memory.

Shared memory is significantly faster than global memory, both in terms of latency and throughput.

2. Scope and Lifetime. The scope of shared memory is limited to the block; only threads within the same block can access the same shared memory.

The lifetime of shared memory is tied to the thread block's lifetime. Once the block finishes execution, the shared memory is released.

3. Access. Shared memory is accessed using memory load/store instructions.

It acts as a scratchpad memory in the computer architecture, allowing threads to quickly share and exchange data.



Figure 27: Hardware View of CUDA Memories.

- Global Memory. A large memory space accessible by all threads and the host (CPU). Used for data storage and retrieval but has higher latency compared to shared memory.
- Shared Memory. A smaller, faster memory space within each SM. Used for data sharing among threads in the same block.
- **Processing Unit**.Contains Arithmetic Logic Units (ALUs) and a Register File for performing computations. Registers are the fastest type of memory, used for storing per-thread data.
- **Control Unit**. Manages the execution of instructions, including the Program Counter (PC) and Instruction Register (IR).
- I/O. Represents input/output operations.

#### 6.3.8 Tiling Technique

The **Tiling Technique**, also known as *blocked matrix multiplication* or *tiling*, is a strategy to enhance the performance of matrix computations by optimizing memory access patterns. It leverages shared memory in CUDA to reduce the number of global memory accesses, improving efficiency and throughput. A lot of parallel algorithms adopt the tiling technique.

### **?** What is Tiling?

Tiling can be thought of as the process of breaking a large matrix into smaller sub-matrices (called *tiles* or blocks) that can fit into faster, limited shared memory. The main goal of tiling is to:

- Minimize slower global memory accesses;
- Maximize the use of faster shared memory.

Instead of a large matrix, we can think of the global memory contents as tiles and focus the computation of CUDA threads on one or a small number of tiles at a time.

### E Great analogy to understand the basic concept of Tiling

Reducing the number of vehicles in a congested traffic system can significantly improve the delays experienced by all vehicles. This is analogous to carpooling for commuters. We can image:

- Drivers: represent threads accessing their memory data operands.
- **Cars**: represent *memory access requests*.

Just as carpooling reduces the number of cars on the road, tiling reduces the number of global memory accesses by loading data into shared memory. The result is a reduction in traffic (memory access requests) and an obvious improvement in overall efficiency.

Unfortunately, just like in real life, there are some problems. For example, there are the **challenges of carpooling**. In fact, some carpools are easier to organize than others because the participants need to have similar work schedules. So certain vehicles may be more suitable for carpooling. However, other **commuters may have different needs**, so the number of carpools may increase and there is a risk of increasing traffic again.

Similar challenges exist in tiling calculations. Some computations may be easier to tile based on data access patterns and the nature of the computation. Organizing data and computations efficiently to fit into tiles may be more challenging for certain algorithms. So what is the general euristic to adopt in order to use the tiling technique or not? In general, it is:

✓ Good to use tiling when people have similar schedule. In computing, is good when threads have similar access timing.

**×** Bad to use tiling when people have very different schedule. In computing, is bad when threads have very *different timing*.

But synchronization is also important. Just as workers' schedules must be aligned for effective carpooling, **threads** in parallel computing **must be synchronized** for efficient execution. Efficient data access and memory usage depend on synchronized operations to reduce latency and improve performance. The following figure shows synchronization between multiple threads.



Figure 28: Barrier Synchronization for Tiling.

On the left are multiple threads (Thread 0, Thread 1, Thread 2, ..., Thread N-1) progressing over time. The wave represents when each thread reaches its barrier on the code; at that point, the thread must wait until all threads have arrived before it can continue. This ensures that all threads are synchronized at certain points during execution. Execution of all threads resumes when the last thread (in the picture, Thread N-2) reaches the barrier.

Synchronization is fundamental in the tiling technique because it ensures that all threads have their share of data loaded into shared memory and are ready to proceed before they perform any computations. After the computation, they use another synchronization barrier to ensure that all threads have completed their work before moving to the next tile.

## Summary - How it works

- 1. **Identify a Tile**. Determine a section of global memory content that multiple threads will access. Dividing the workload into smaller tiles allows for efficient memory access and utilization of shared memory.
- 2. Load the Tile. Transfer the tile from global memory to on-chip memory (shared memory). Loading data into shared memory reduces the latency associated with accessing global memory.
- 3. **Barrier Synchronization**. Ensures that all threads are ready to begin the computation phase. It also ensures that all threads have the necessary data before starting the computation.
- 4. Access Data. Multiple threads access their data from the on-chip memory. Threads perform computations using the data stored in shared memory, benefiting from its faster access time.
- 5. Barrier Synchronization. Ensure all threads have completed the current phase (computations).
- 6. Next Tile. Move on to the next tile and repeat the process.

#### ✓ Advantages

- ✓ Improved Memory Access Patterns. By loading data into shared memory, the number of global memory accesses is reduced, leading to better performance.
- ✓ Higher Computational Throughput. Tiling helps achieve higher computational throughput by leveraging the faster shared memory.

## 6.3.8.1 Tiled Matrix Multiplication

In the following section, we present an **example of matrix multiplication using the tiling technique** to illustrate the efficiency improvements brought about by the tiling technique.

# E Traditional approach

Classical matrix multiplication has the following characteristics

- Each thread accesses a row of matrix M and a column of matrix N.
- Each thread block accesses a strip of matrix M and a strip of matrix N.



In the traditional approach, threads access data directly from global memory, which can be inefficient due to high latency.

# **2 Tiled Matrix Multiplication**

- 1. As a **first step**, since we know the problem and (ideally) how the solution is implemented, we can try to brainstorm on how to apply tiling. In general, matrix operations lend themselves well to the tiling technique. In the matrix multiplication:
  - The execution of each thread can be broken into phases.
  - The data accesses by the thread block in each phase are focused on one tile of *M* and one tile of *N*.
  - The tile is of **BLOCK\_SIZE** elements in each dimension.

# 2. As second step, the threads in a block participate in **loading items into** shared memory using the tiling technique.

As we can see in the following figure, each thread in a block contributes to loading elements from matrices M and N into shared memory. Each thread is responsible for loading one element from the M matrix and one element from the N matrix into shared memory. This parallel loading ensures that data is moved quickly and efficiently from global memory to faster shared memory.



M <sub>0,0</sub> M <sub>0,1</sub> M <sub>0,2</sub> M <sub>0,3</sub>	M <sub>0.0</sub> M <sub>0.1</sub>	P <sub>0,0</sub>	P <sub>0,1</sub>	P <sub>0,2</sub>	P <sub>0,3</sub>
$M_{1,0} M_{1,1} M_{1,2} M_{1,3}$	M <sub>1,0</sub> M <sub>1,1</sub>	P <sub>1,0</sub>	$P_{1,1}$	P <sub>1,2</sub>	$P_{1,3}$
$M_{2,0} M_{2,1} M_{2,2} M_{2,3}$		P <sub>2,0</sub>	P <sub>2,1</sub>	P <sub>2,2</sub>	P <sub>2,3</sub>
$M_{3,0} M_{3,1} M_{3,2} M_{3,3}$		$P_{3,0}$	$P_{3,1}$	$P_{3,2}$	$P_{3,3}$

The matrices M and N are the input and P is the result matrix. Each element is indexed by i and j (e.g.,  $M_{ij}$ ).

- Elements of M are loaded into shared memory by the threads.
- Similarly, elements of N are loaded into shared memory.

This particular phase focuses on the initial loading of elements for the tile corresponding to block (0,0). Each thread in block (0,0) loads one element from M and one from N, populating the shared memory with the necessary data for the computation.

These steps are performed for each block of the matrices. In the following figure, we can see another step of loading into shared memory.

$\begin{array}{c c c c c c c c c c c c c c c c c c c $	Shared Memory	N <mark>-2,0</mark> N <sub>2,1</sub> N-2,0 N <sub>2,1</sub>	Shared Memory
$\begin{array}{c c c c c c c c c c c c c c c c c c c $	$M_{0,2}^{2} M_{0,3}$ $M_{1,2}^{2} M_{1,3}$	$\begin{array}{c c} P_{0,0} & P_{0,1} \\ \hline P_{1,0} & P_{1,1} \\ \hline P_{2,0} & P_{2,1} \\ \hline P_{3,0} & P_{3,1} \end{array}$	$\begin{array}{c c} P_{0,2} & P_{0,3} \\ \hline P_{1,2} & P_{1,3} \\ \hline P_{2,2} & P_{2,3} \\ \hline P_{3,2} & P_{3,3} \end{array}$

- 3. After loading into shared memory, there is the loading step, done in two iterations, into the result matrix. This is only a graphical representation, because in reality this step can be merged with the execution step. This step prepares the operands to be used in the execution step.
  - (a) In the first iteration, the elements from the shared memory  $N_{0,0}, N_{0,1}$  are used against the element from the shared memory  $M_{0,0}, M_{1,0}$ .



(b) In the second iteration, the elements from the shared memory  $N_{1,0}, N_{1,1}$ are used against the element from the shared memory  $M_{0,1}, M_{1,1}$ .

N <sub>0,0</sub> N <sub>0</sub>	1 N <sub>0,2</sub>	N <sub>0,3</sub>			N <sub>0,0</sub>	N <sub>0,1</sub>	Sha	red N	lemory
N <sub>1,0</sub> N <sub>1</sub>	<u>1 N<sub>1,2</sub></u>	N <sub>1,3</sub>	1		N <sub>1,0</sub>	N <sub>1,1</sub>	]		
N <sub>2,0</sub> N <sub>2</sub>	1 N <sub>2,2</sub>	N <sub>2,3</sub>							
N <sub>3,0</sub> N <sub>3</sub>	1 N <sub>3,2</sub>	N <sub>3,3</sub>		1.2.6					
			Share	d Memory	′		_		
M <sub>0,0</sub> M <sub>0</sub>	M <sub>0,2</sub>	M <sub>0,3</sub>	M <sub>0,0</sub>	M <sub>0,1</sub>	<mark>Р<sub>0,0</sub></mark>	<b>B</b> <sub>0</sub> 1	P <sub>0,2</sub>	P <sub>0,3</sub>	
M <sub>1,0</sub> M <sub>1</sub>	_1 M <sub>1,2</sub>	M <sub>1,3</sub>	M <sub>1,0</sub>	M <sub>1,1</sub>	₽ <sup>+</sup> 1,0	<b>B</b> <sub>1,1</sub>	P <sub>1,2</sub>	$P_{1,3}$	
M <sub>2,0</sub> M <sub>2</sub>	M <sub>2,2</sub>	M <sub>2,3</sub>			P <sub>2,0</sub>	P <sub>2,1</sub>	P <sub>2,2</sub>	$P_{2,3}$	
$M_{3,0} M_{3}$	M <sub>3,2</sub>	M <sub>3,3</sub>			P <sub>3,0</sub>	P <sub>3,1</sub>	P <sub>3,2</sub>	$P_{3,3}$	

This step is done for each block of the matrices. In the figure on the next page, we can see two more steps of the load block.



4. After each load, there is the **execution phase**. In the following table, we highlight how four threads in a block perform matrix multiplication using shared memory.

	Phase	0		Phase 1			
thread <sub>0,0</sub>	$\begin{array}{c} \mathbf{M_{0,0}} \\ \downarrow \\ \mathbf{Mds_{0,0}} \end{array}$	$egin{array}{c} \mathbf{N}_{0,0} \ \downarrow \ \mathbf{N}ds_{0,0} \end{array}$	$\begin{array}{l} PValue_{0,0} += \\ Mds_{0,0}*Nds_{0,0} + \\ Mds_{0,1}*Nds_{1,0} \end{array}$	$\mathbf{M}_{0,2}$ $\downarrow$ $\mathrm{Mds}_{0,0}$	$\begin{matrix} \mathbf{N_{2,0}} \\ \downarrow \\ \mathbf{Nds}_{0,0} \end{matrix}$	$\begin{array}{l} PValue_{0,0} += \\ Mds_{0,0}*Nds_{0,0} + \\ Mds_{0,1}*Nds_{1,0} \end{array}$	
thread <sub>0,1</sub>	$\begin{array}{c} \mathbf{M_{0,1}}\\ \downarrow\\ \mathbf{Mds_{0,1}}\end{array}$	$\begin{array}{c} \mathbf{N_{0,1}} \\ \downarrow \\ \mathbf{Nds}_{1,0} \end{array}$	$\begin{array}{l} PValue_{0,1} += \\ Mds_{0,0}*Nds_{0,1} + \\ Mds_{0,1}*Nds_{1,1} \end{array}$	$\mathbf{M}_{0,3}$ $\downarrow$ $\mathbf{Mds}_{0,1}$	$\begin{matrix} \mathbf{N_{2,1}} \\ \downarrow \\ \mathbf{Nds}_{0,1} \end{matrix}$	$\begin{array}{l} PValue_{0,1} += \\ Mds_{0,0}*Nds_{0,1} + \\ Mds_{0,1}*Nds_{1,1} \end{array}$	
thread <sub>1,0</sub>	$\begin{array}{c} \mathbf{M_{1,0}} \\ \downarrow \\ \mathbf{Mds}_{1,0} \end{array}$	$\begin{matrix} \mathbf{N_{1,0}} \\ \downarrow \\ \mathbf{Nds}_{1,0} \end{matrix}$	$\begin{array}{l} PValue_{1,0} += \\ Mds_{1,0}*Nds_{0,0} + \\ Mds_{1,1}*Nds_{1,0} \end{array}$	$\mathbf{M_{1,2}} \\ \downarrow \\ \mathbf{Mds}_{1,0}$	$\begin{matrix} \mathbf{N_{3,0}} \\ \downarrow \\ \mathbf{Nds}_{1,0} \end{matrix}$	$\begin{array}{l} PValue_{1,0} += \\ Mds_{1,0}*Nds_{0,0} + \\ Mds_{1,1}*Nds_{1,0} \end{array}$	
thread <sub>1,1</sub>	$\begin{array}{c} \mathbf{M_{1,1}} \\ \downarrow \\ \mathbf{Mds}_{1,1} \end{array}$	$\begin{vmatrix} \mathbf{N}_{1,1} \\ \downarrow \\ \mathrm{Nds}_{1,1} \end{vmatrix}$	$\begin{array}{l} PValue_{1,1} += \\ Mds_{1,0}*Nds_{0,1} + \\ Mds_{1,1}*Nds_{1,1} \end{array}$	$\begin{array}{c} \mathbf{M_{1,3}} \\ \downarrow \\ \mathbf{Mds}_{1,1} \end{array}$	$\begin{vmatrix} \mathbf{N}_{3,1} \\ \downarrow \\ \mathrm{Nds}_{1,1} \end{vmatrix}$	$\begin{array}{l} PValue_{1,1} += \\ Mds_{1,0}*Nds_{0,1} + \\ Mds_{1,1}*Nds_{1,1} \end{array}$	

time

The values  $Mds_{i,j}$  are the values loaded in the load step from global to shared memory of the M matrix. The same reasoning applies to Nds.

Once the data is loaded into shared memory, each thread uses the loaded values to update the partial product value PValue for the resulting matrix *P*:

٠	$\mathtt{thread}_{0,0}$ :
1	$PValue_{0,0} += Mds_{0,0} * Nds_{0,0} + Mds_{0,1} * Nds_{1,0}$
•	$thread_{0,1}$ :
1	$PValue_{0,1} += Mds_{0,0} * Nds_{0,1} + Mds_{0,1} * Nds_{1,1}$
•	$thread_{1,0}$ :
1	$PValue_{1,0} += Mds_{1,0} * Nds_{0,0} + Mds_{1,1} * Nds_{1,0}$
•	$thread_{1,1}$ :
1	$\texttt{PValue}_{1,1} \texttt{ += } \texttt{Mds}_{1,0} \texttt{ * } \texttt{Nds}_{0,1} \texttt{ + } \texttt{Mds}_{1,1} \texttt{ * } \texttt{Nds}_{1,1}$

5. Barrier Synchronization step. To synchronize all threads in a block, we use the function \_\_syncthreads(). This function acts as a barrier synchronization, ensuring that all threads in a block reach that point before any thread can proceed.

Barrier synchronization is particularly useful for coordinating the execution of tiled algorithms in phases. It is useful in:

- ✓ Loading Phase. Ensures that all elements of a tile are loaded into shared memory before any computation begins.
- ✓ Computation Phase. Ensures that all threads have completed their computation on the current tile before moving to the next phase or tile.

# 6.3.8.2 Implementation Tiled Matrix Multiplication

After a great explanation of how to apply the tiling technique to the matrix multiplication operation, we present the CUDA implementation. As we said, the goal of tiled matrix multiplication with CUDA is to optimize the matrix multiplication process by taking advantage of shared memory (small, fast memory space accessible to all threads within the same block).

#### **E** Introduction to the implementation

The main core of the implementation is about **tile indexing**. It can be 1 or 2 dimensional. In the following figures, to understand the logic, we show 2 dimensional indexing, which is more natural.

• When each thread loads the input from the original matrix (M or N), it needs an index.

```
1 int Row = by * blockDim.y + ty;
2 int Col = bx * blockDim.x + tx;
3 // 2D indexing for accessing Tile 0:
4 M[Row][tx]
5 N[ty][Col]
```

At each iteration, each thread in a block considers the same row of the matrix M and the same column of the matrix N. To distribute the workload among the threads, we assign each thread to each column of the matrix M (using the unique index tx, the index of the thread in the CUDA block), and with the same reasoning, we assign each thread to each row of the matrix N. The row in the matrix M is fixed, but the column is taken entirely by the assignment of all threads in the block (using tx).

In the following figure, we see that the row in the matrix M is fixed, but the column is fully occupied thanks to the assignment of all threads in the block (using tx).



When the first phase is finished, we move on to the second tile. For this reason, we use a kind of **offset** given by the formula  $p \times \text{TILE}_\text{WIDTH}$  (TILE\_WIDTH = BLOCK\_WIDTH), where p is the number of the phase (at the beginning zero, then one, and so on).

In the following image, we see that at phase 1, to load the tile 1, we use the formula:

```
// 2D indexing for accessing Tile 1:
2 M[Row][1 * TILE_WIDTH + tx]
3 N[1 * TILE_WIDTH + ty][Col]
```


#### X CUDA code

```
#define TILE_WIDTH 16
1
2
3 __global__ void MatrixMulKernel(
      float* M, float* N, float* P, int Width
4
5){
       __shared__ float ds_M[TILE_WIDTH][TILE_WIDTH];
6
       __shared__ float ds_N[TILE_WIDTH][TILE_WIDTH];
7
8
      int bx = blockIdx.x; int by = blockIdx.y;
9
      int tx = threadIdx.x; int ty = threadIdx.y;
12
      int Row = by * blockDim.y + ty;
      int Col = bx * blockDim.x + tx;
13
      float Pvalue = 0;
14
15
      // Loop over the M and N tiles
16
17
      // required to compute the P element
       int bound = Width / TILE_WIDTH;
18
      for (int p = 0; p < bound; ++p) {</pre>
19
           // Collaborative loading of {\tt M} and {\tt N} tiles
20
21
           // into shared memory
           ds_M[ty][tx] = M[Row * Width + p * TILE_WIDTH + tx];
22
23
           // = M[Row][p * TILE_WIDTH + tx]
           ds_N[ty][tx] = N[(p * TILE_WIDTH + ty) * Width + Col];
24
25
           // = N[p * TILE_WIDTH + ty][Col]
           __syncthreads();
26
27
           for (int i = 0; i < TILE_WIDTH; ++i) {</pre>
28
               Pvalue += ds_M[ty][i] * ds_N[i][tx];
29
           7
30
31
           __syncthreads();
32
      }
      P[Row * Width + Col] = Pvalue;
33
34 }
```

- Index variables:
  - bx and by are the block indices in the x and y directions.
  - tx and ty are the **thread indices** within a block.
  - Row and Col are the row and column indices of the element in the output matrix.
- Main Loop: ph (phase) determines which tile is currently being processed.
- Loading Tiles into Shared Memory:
  - Each thread loads one element from the current tile of M and N into shared memory.
  - $ds_M[ty][tx]$  loads an element from M.
  - $ds_N[ty][tx]$  loads an element from N.
  - \_\_syncthreads() is called to ensure all threads have loaded their elements before proceeding.

- Matrix Multiplication within a Tile. Once the tiles are loaded into shared memory, each thread computes the partial dot product for the corresponding element in the output matrix. The nested loop (second for loop) accumulates the product of elements from *M* and *N*.
- Finally, after all tiles have been processed, the final value is stored in the output matrix *P*.

#### Final consideration

A bigger block is better and the reason is simple. **Bigger tiles mean more** threads per block. For example:

- TILE\_WIDTH of 16 results in  $16 \times 16 = 256$  threads per block.
- TILE\_WIDTH of 32 results in  $32 \times 32 = 1024$  threads per block.

Therefore, the *workload* per phase is:

- TILE\_WIDTH = 16:
  - Each block performs 512  $(2 \times 256)$  float loads from global memory.
  - Executes 8192  $(256 \times (2 \times 16))$  multiply-add operations (16 floating point operations for each memory load).
- TILE\_WIDTH = 32:
  - Each block performs 2048  $(2 \times 1024)$  float loads from global memory.
  - Executes **65536**  $(1024 \times (2 \times 32))$  multiply-add operations (32 floating point operations for each memory load).

Although a larger block might be better, shared memory is not infinite. It depends on the implementation. If we take a classic Streaming Multiprocessor (SM) with 16KB of shared memory, when we do a memory usage analysis:

- TILE\_WIDTH = 16:
  - Uses **2KB**  $(2 \times 256 \times 4B)$  of shared memory per block.
  - Allows up to 8 blocks per SM in parallel execution  $(8 \times 256 \text{ threads})$ = 2048 threads).

This allows up to 4096  $(8 \times 512)$  pending loads (2 per thread, 256 per block).

- TILE\_WIDTH = 32:
  - Uses 8KB  $(2 \times 32 \times 32 \times 4B)$  of shared memory per block.
  - Allows up to 2 blocks per SM in parallel execution (limited by thread count). If a GPU limits the thread count to 1536 threads per SM, the number of blocks per SM is reduced to one!

Using \_\_syncthreads() ensures that all threads reach a barrier before continuing, which can temporarily reduce the number of active threads. More blocks per SM can be beneficial to balance memory usage and thread count.

In summary, choosing the right tile size and efficiently managing shared memory and threads are critical to optimizing GPU performance. This balance affects how many operations can be performed simultaneously and how effectively memory is used.

#### 6.3.8.3 Any size matrix handling

The following paragraph focuses on the challenge of handling matrix multiplication for matrices of arbitrary size using tiled matrix multiplication. Often, real-world applications require support for matrices that aren't always square or multiples of the tile width (TILE\_WIDTH). So what is the strategy for these situations?

#### **A** Limitations of the Tiled Matrix Multiplication presented

- The base kernel can only handle square matrices whose dimensions are multiples of TILE\_WIDTH. This is a major limitation, since non-square matrices also exist.
- A possible solution would be to apply padding, but padding these matrices to match tile sizes can result in **significant overhead** in terms of space and data transfer time.

The basic idea is that instead of padding, a different technique is proposed to efficiently handle matrices of arbitrary size and prevent access to invalid memory locations.





### $\checkmark$ A simple solution

The main simple and efficient solution is the **conditional loading**. When a thread is to load an input element, **check if the element index is within valid bounds**:

- If <u>valid</u>: proceed to **load the element**.
- If invalid: do not load the element, but write a 0 instead.

Assigning a 0 value ensures that the multiply-add step does not affect the final value of the output element. Also, this simple check helps avoid errors from invalid memory access and ensures correctness.

# • Why do we have to load a zero? We cannot skip this part directly?

- 1. Safety and Validity. When a thread loads a 0 instead of an out-ofbound element, it ensures that the memory access is valid and does not cause runtime errors or fetch garbage data. This is crucial for maintaining the stability of the program.
- 2. Maintaining Computational Integrity. The 0 value acts as a neutral element in multiplication, meaning it does not alter the final sum during the multiply-add operations. For example:

sum += tileM[ty][k] \* tileN[k][tx]

If tileM[ty][k] or tileN[k][tx] is 0, the sum remains unaffected by that particular operation, preserving the integrity of the calculation.

3. Facilitating Parallel Execution. In CUDA, all threads in a warp (a group of 32 threads) execute the same instruction simultaneously. If some threads are out-of-bound, they still participate in the synchronization and memory access patterns, ensuring the warp executes efficiently without branching or divergence.

By loading 0s, these threads can reach synchronization points (such as \_\_syncthreads()) together with other threads that load valid data, ensuring all threads in the block stay in sync.

A Warp Divergence occurs when threads in a warp follow different execution paths due to conditional branches. This means some threads are active while others are idle, leading to inefficiency. The consequences of warp divergence can have a severe impact on performance.

- Performance Impact:
  - Divergence causes some threads to stall while others execute, reducing the overall throughput.
  - All threads in the warp must eventually reconverge to execute the same instructions again, prolonging the execution time for that warp.
- Synchronization Issues:
  - Skipping \_\_syncthreads() or similar synchronization points can lead to incorrect behavior. Threads that do not wait might access incomplete or inconsistent data in shared memory, leading to incorrect results.
  - Ensuring that all threads in a warp (or block) reach synchronization points is crucial for data consistency.
- 4. Shared Memory Utilization. All threads, including those loading 0s, contribute to filling the shared memory tiles. This ensures that when the matrix multiplication is performed, the shared memory contains a complete tile (with zeros in out-of-bound areas). This approach guarantees that the shared memory tiles are properly used for the block's calculations, and threads with 0 elements help maintain the structure and coherence of these tiles.

#### X Implementation

The code snippet is as follows:

```
1 for (int p = 0; p < (Width - 1) / TILE_WIDTH + 1; ++p) {</pre>
       if (Row < Width && p * TILE_WIDTH + tx < Width) {</pre>
2
           ds_M[ty][tx] = M[Row * Width + p * TILE_WIDTH + tx];
3
      } else {
           ds_M[ty][tx] = 0.0;
5
      7
6
       if (p * TILE_WIDTH + ty < Width && Col < Width) {</pre>
           ds_N[ty][tx] = N[(p * TILE_WIDTH + ty) * Width + Col];
8
9
      } else {
           ds_N[ty][tx] = 0.0;
      }
       __syncthreads();
       // Ensuring valid computations and
14
15
       11
         writing to the output matrix
       if (Row < Width && Col < Width) {
16
           for (int i = 0; i < TILE_WIDTH; ++i) {</pre>
17
               Pvalue += ds_M[ty][i] * ds_N[i][tx];
18
           7
19
20
      }
       __syncthreads();
21
22 }
23
24 if (Row < Width && Col < Width) {
25
      P[Row * Width + Col] = Pvalue;
26 }
```

- Matrix *M*. Each thread loads:
  - An element in the position M[Row][p \* TILE\_WIDTH + tx] if the row is less than the width of the matrix (Row < Width) and the tile number (p \* TILE\_WIDTH) plus the index number of the thread tx is less than the width of the matrix (p \* TILE\_WIDTH + tx < Width).</li>
  - Otherwise, load 0.
- Matrix N. Each threads loads:
  - An element in the position N[p \* TILE\_WIDTH + ty][Col] if the column is less than the width of the matrix (Col < Width) and the tile number (p \* TILE\_WIDTH) plus the index number of the thread ty is less than the width of the matrix (p \* TILE\_WIDTH + ty < Width).</p>
  - Otherwise, load 0.
- Boundary condition (Width 1) / TILE\_WIDTH + 1:
  - Width 1: adjusts the maximum index for a zero-based index system. Essentially, it ensures we account for the last valid index in the matrix.
  - / TILE\_WIDTH: divides the total width by the tile width, determining how many full tiles fit within the width.

- TILE\_WIDTH + 1: ensuring that any remaining part of the matrix that doesn't fit perfectly into the last tile is also processed. If the width isn't an exact multiple of the tile width, the +1 ensures that an additional tile is considered to cover the remaining part of the matrix.

#### 6.3.9 Optimizing Memory Coalescing

In this chapter, we introduce the importance of memory coalescing for effectively using memory bandwidth in CUDA.

#### Introduction

Memory bandwidth is important in CUDA because each thread may need to access memory, and efficient memory access is critical to overall performance. Ideally, when multiple threads in a CUDA program access memory, their accesses should be *coalesced*. This means that **memory accesses from multiple threads are combined into a single memory transaction**.

The memory type inside the GPU is DRAM. Since DRAM accesses are not as fast as local registers, an optimization is required. For this reason, the technique of *DRAM bursts* is introduced:

- It allows a block of data to be transferred in one go. When CUDA threads coalesce memory accesses, the entire burst can be used effectively, resulting in *fewer memory transactions and higher memory bandwidth utilization*.
- By coalescing memory accesses into fewer DRAM bursts, the *latency (de-lay) associated with memory access is reduced.* This is because once a burst is initiated, the additional data within the burst can be accessed quickly.
- CUDA developers use a variety of techniques to ensure that thread memory accesses are concatenated to take full advantage of DRAM burst capabilities. These include *aligning data structures and managing memory* access patterns.

For example, consider a CUDA kernel where each thread accesses successive memory locations. When these accesses are combined, a single DRAM burst can fetch multiple data points needed by multiple threads, *significantly speeding up the computation*.

### **?** What is a DRAM burst?

A DRAM (Dynamic Random Access Memory) burst is a way of reading data from or writing data to memory. When accessing DRAM, data isn't retrieved one byte at a time, but rather in bursts. A DRAM burst involves the transfer of multiple bytes of data in a single, continuous sequence, rather than in separate, discrete chunks.

- Non-Burst Timing. There are gaps between data transfers, resulting in inefficiencies.
- Burst Timing. Represents a continuous sequence of data transfer, illustrating the efficiency of burst mode. Burst bytes are transmitted to the processor, but may be discarded if accesses are not sequential.



Figure 29: The figure shows a comparison of non-burst and burst timing in DRAM systems.

Burst mode minimizes the gaps between data transfers, allowing for faster and more efficient data flow. This is in contrast to non-burst mode, where data transfers are inefficient due to gaps.

In more detail, burst mode can be **described by the following features**:

- Burst operation. When accessing a specific memory address, the DRAM retrieves an entire block of adjacent data, called a burst. This allows faster data access than retrieving individual bytes one at a time.
- Burst Length. The length of the burst indicates how many bytes are transferred in one operation. Common burst lengths are 4, 8, or 16 bytes, but larger lengths are used depending on the system and application.
- Memory efficiency. This method improves memory access efficiency. Once the initial memory location is accessed, the DRAM can transfer the rest of the data in the burst with less overhead.
- System Usage. Burst transfers are particularly useful in applications where large blocks of data must be moved quickly, such as graphics processing where textures and images are frequently accessed.

#### Example 6: great analogy with burst technology

We can think of burst mode as a bookshelf, where instead of taking out one book at a time, we take out a whole section at once. This way, we get more books (data) in one go, reducing the time it takes to reach for each book individually. The following figure shows a system view of the DRAM burst. Each address space is divided into burst sections, and when one location is accessed, all other locations in the same section are also delivered to the processor.

Burst section				Burst section				Burst section				Burst section			
0	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15

Figure 30: In the figure, a 16-byte address space is divided into 4-byte burst sections. In practice, address spaces are much larger (e.g., 4 GB) and burst sections are also larger (e.g., 128 bytes or more).

#### Coalesced access vs un-coalesced access

Memory Coalescing refers to the process of combining (or *coalescing*) multiple memory accesses by different threads into a single memory transaction. This is important in the context of GPUs because they run many threads in parallel, and efficient memory access can significantly improve performance.

When threads in a warp (a group of threads running in parallel) access successive memory locations, these accesses are combined into a single memory transaction. This means that all requested data is retrieved in one go.

When threads access memory locations that are scattered or misaligned, multiple memory transactions are required, leading to inefficiencies. This phenomenon is called **Un-Coalesced Access**.

Un-Coalesced Accesses occur when the memory requests of multiple threads in a warp do not fit properly into a single memory transaction. This inefficiency results in *increased memory latency* and *lower overall performance*. It is manifested when:

- Non-Sequential Memory Access. When threads access memory addresses that are not contiguous, the memory controller must handle each access individually or in smaller, less efficient chunks.
- **Crossing Burst Boundaries**. When memory accesses span multiple DRAM burst sections, **multiple memory transactions are required**. Each burst section may only be able to handle a portion of the requested data, resulting in additional overhead.
- Thread misalignment. If the data being accessed by threads is misaligned with the natural boundaries of memory bursts, the accesses cannot be merged effectively. This often happens with poorly structured data layouts.

The un-coalesced accesses are a **penalty for memory optimization because the memory controller cannot combine these accesses into a single transaction because they are spread out**. Instead, it must handle multiple transactions, each fetching only a few bytes relevant to the threads. The consequences of un-coalesced access are:

- Increased DRAM transactions. Each un-coalesced access requires a separate DRAM burst, increasing the number of memory transactions.
- Wasted Bandwidth. Not all bytes in a DRAM burst are utilized. For example, if each burst fetches 32 bytes and only 8 bytes are used by threads, the remaining 24 bytes are wasted.
- **Higher Latency**. More transactions means more latency because **each** transaction requires setup and transmission time.



Figure 31: When all threads of a warp execute a load instruction, if all accessed locations are in the same burst section, only one DRAM request is made and the access is fully merged.



Figure 32: If the accessed locations are spread across burst boundaries, coalescing fails (un-coalesced accesses), multiple DRAM requests are made. This results in some garbage bytes that are not used by threads.



Example 8: difference from coalesced and un-coalesced access

Suppose a warp of 32 threads accesses an array in global memory. If each thread accesses elements sequentially (thread 0 accesses element 0, thread 1 accesses element 1, and so on), a single memory transaction retrieves all 32 elements.

In contrast, if the same warp accesses memory in a non-sequential manner (thread 0 accesses element 0, thread 1 accesses element 4, thread 2 accesses element 8, and so on), multiple memory transactions are required, reducing efficiency.

• How do we guarantee coalesced access?

Accesses in a warp are to consecutive locations if the index in an array access is in the form of:

(expression with terms independent of threadIdx.x) + threadIdx.x \$(12)\$

This formula ensures coalesced memory access in GPU programming.

- threadIdx.x: represents the thread index within a warp.
- Expression Independent of threadIdx.x: this part of the formula ensures that the base index is the same for all threads within a warp. It's crucial for aligning memory access.

But why does it work? For two main reasons:

- 1. Consecutive Access: if the base index (the part of the expression that is independent of threadIdx.x) is the same for all threads, then adding threadIdx.x to that base index means that each thread is accessing a consecutive location.
- 2. Memory Coalescing: using this formula ensures that all threads within a warp are accessing adjacent memory locations, resulting in coalesced access.

Before we continue, we need to understand how a matrix is stored in memory. It depends on the language, the implementation, and so on, but in general, when we say *linear memory space*, a 2-dimensional matrix is stored as in Figure 33 (page 158).



linearized order in increasing address

Figure 33: Linear memory space.

In GPU programming, matrix multiplication involves two main access patterns:

- Matrix A (left operator): the access pattern is A[Row \* n + i]
  - i is the **loop counter** in the inner product loop of the kernel code;
  - Row is the current row being processed;
  - n is the number of columns in matrix A.
- Matrix B (right operator): the access pattern is B[i \* k + Col]
  - i is the loop counter;
  - k is the number of columns in matrix B;
  - Col is calculated as:

blockIdx.x \* blockDim.x + threadIdx.x

This means that threads access elements in matrix B based on their column index.



• Matrix B. The accesses are **Coalesced**. As we can see from the figure 34, the accesses are coalesced. This is because matrix B is stored in memory in a linear, one-dimensional array. For a 2D matrix, the elements are stored row by row.

In a warp, threads are indexed consecutively, like threadIdx.x = 0, 1, .... When i is fixed for a loop iteration, successive threads access successive memory locations in matrix B. For example:

- Thread 0 accesses B[i \* k + 0]
- Thread 1 accesses B[i \* k + 1]
- Thread 2 accesses B[i \* k + 2]



Figure 34: Coalesced accesses.

The main reason for coalesced access in matrix **B** is to **align thread indexes with contiguous memory addresses**. This optimizes memory transactions, making data retrieval more efficient and increasing overall performance.

• Matrix A. The accesses are **Un-Coalesced**. The figure shows why the accesses for matrix A are not coalesced.



Figure 35: Un-Coalesced Accesses.

The access pattern A[Row \* n + i] means that each thread in a warp accesses different rows of the matrix A. If we consider consecutive threads (e.g. thread 0, thread 1, thread 2, thread 3), they access elements in different rows.

Threads in a warp access elements vertically, not horizontally. For example, if Row is fixed for a given iteration of the outer loop, i varies. This means that thread 0 accesses A[Row \* n + 0], thread 1 accesses A[Row \* n + 1], and so on. This results in non-consecutive memory locations being accessed by consecutive threads.

# How to optimize the matrix multiplication to avoid un-coalesced accesses

**Corner Turning** is a **technique used in matrix multiplication to optimize memory access patterns**, especially in parallel computing environments like GPU. The goal is to achieve memory coalescing, which improves performance by ensuring that memory accesses are aligned and contiguous.

Corner Turning works as follows:

- Column-Major Layout. Normally, matrices are stored in a row-major layout (elements are stored row by row). In corner turning, the second matrix (B) is stored in a column-major layout (elements are stored column by column).
- Tiled Access. The matrices are divided into smaller submatrices or tiles. Each thread loads a tile of the first matrix (A) and a tile of the second matrix (B) into shared memory.
- Memory Coalescing. By loading tiles into shared memory, threads can access consecutive memory locations within the tiles. This ensures that memory accesses are coalesced, reducing memory latency and increasing bandwidth utilization.



In practice, it works as shown in the following figure:

- Original Access Pattern:
  - Matrix d\_M. The original access pattern is horizontal. Each thread accesses consecutive elements in a row.
  - Matrix d\_N. The original access pattern is vertical. Each thread accesses elements in different rows.

- Tiled Access Pattern:
  - Matrix d\_M. The matrix is divided into smaller horizontal tiles.
     Each tile is a small submatrix that fits into shared memory.
  - Matrix d\_N. Similarly, this matrix is divided into smaller vertical tiles, which are also small enough to fit into shared memory.
- Shared Memory Operations:
  - Loading Tiles into Shared Memory. Both tiles from d\_M and d\_N are loaded into shared memory. This allows for more efficient access patterns.
  - Matrix Multiplication. The multiplication of these tiles is performed using the values stored in shared memory. This step ensures that the data access is coalesced and reduces latency.

By dividing matrices into tiles and loading them into shared memory, threads can access successive memory locations within a tile. This *ensures that memory accesses are concatenated*, reducing memory transactions and increasing efficiency.

In addition, using shared memory for these tiles reduces the need to repeatedly access global memory, which is slower. Shared memory access is much faster, further improving the performance of matrix multiplication.

From a code point of view, we see:

• Original Pattern:

1	Matrix	d_M (Row-major):
2	Thread	0: M[0][0], M[0][1],
3	Thread	1: M[1][0], M[1][1],
4		
5	Matrix	d_N (Column-major):
6	Thread	0: N[0][0], N[1][0],
7	Thread	1: N[O][1], N[1][1],

- Tiled Pattern:
  - 1. Load Tiles into Shared Memory:

1	Tile	from	$d_M:$	[[MOO,	M01],	[M10,	M11]]
2	Tile	from	$d_N:$	[[NOO,	N10],	[N01,	N11]]

2. Perform Multiplication. Threads use values from shared memory for the multiplication, ensuring coalesced access and reduced memory latency.

# 7 CUDA

Although the CUDA topic has already been discussed in section 6.3.1 (page 103), here we introduce more technical topics, a kind of CUDA laboratory. It is done because in the Parallel Computing course we have done a CUDA theory part and a CUDA practice part.

### 7.1 Introduction

**CUDA**, which stands for **Compute Unified Device Architecture**, is a **parallel computing platform and application programming interface (API) model created by NVIDIA**. It allows developers to use the power of GPUs (Graphics Processing Units) for general-purpose processing, which enables substantial performance improvements for computationally intensive tasks.

# **?** Why CUDA?

GPUs, originally designed to render graphics, have evolved into highly efficient and powerful processors capable of handling thousands of threads simultaneously. This transformation has made GPUs, and by extension CUDA, incredibly valuable for applications requiring massive parallelism, such as scientific simulations, machine learning, and deep learning.

#### Why can we not just use the CPU?

Understanding the fundamental differences between CPU and GPU architectures is key to appreciating CUDA's advantages:

- CPU (Central Processing Unit):
  - Designed for sequential processing.
  - Features powerful Arithmetic Logic Units (ALUs) with low latency.
  - Utilizes large hierarchical caches to optimize access to frequently used data.
  - Employs advanced control mechanisms, such as branch prediction and data forwarding, to minimize delays.
- GPU (Graphics Processing Unit):
  - Optimized for parallel processing.
  - Contains a large number of simpler, pipelined ALUs designed for high-throughput computations, despite having longer latency.
  - Relies on smaller caches to facilitate high memory throughput.
  - Uses simpler control mechanisms, enabling efficient context switching and handling many threads concurrently.

CUDA leverages these GPU characteristics to execute programs with a parallelfirst approach, breaking down tasks into smaller, manageable pieces and processing them simultaneously. This approach leads to significant speedups compared to traditional CPU-only processing, making CUDA a pivotal technology for high-performance computing.

#### 🗏 GPGPU programming paradigms

CUDA helped bring General Purpose computing on Graphics Processing Units (GPGPU). Initially designed to accelerate rendering and processing of graphics, GPUs have evolved into versatile processors capable of handling a wide range of computational tasks beyond graphics. This paradigm shift has allowed GPUs to be used for general-purpose computing, providing significant performance improvements for applications requiring high parallelism and computational power (the definition and introduction of GPGPU can be found on page 100).

The GPU (called a device) acts as a co-processor for the CPU (host):

- CPU (host):
  - General-purpose processor.
  - Handles diverse tasks, running an operating system, and executing a sequence of stored instructions.
  - Efficient for tasks requiring low-latency access to cached data.
- GPU (device):
  - Specialized for high-throughput computation.
  - Contains a large number of processing elements for parallel tasks.
  - Relies on dedicated, high-bandwidth memory.
  - Best for data-parallel tasks, hiding memory latency effectively.

The relationship of these two concepts:

- Both CPU and GPU have their own memory spaces.
- Optimal performance achieved through cooperation.
- CPU handles complex logic and serial tasks; GPU manages parallel processing.

About the architecture, the differences are:

- CPU (host):
  - Composed of control units, ALUs, cache, and DRAM.
  - Efficient for tasks requiring complex control and low-latency data access.
- GPU (device):
  - Made up of DRAM and a grid of processing units.
  - High-throughput design for parallel processing tasks.

**GPGPU** (General-Purpose computing on Graphics Processing Units) **programming paradigms are various approaches or models used to leverage the GPU for general-purpose computation**. These paradigms **allow programmers to write code that runs efficiently on GPUs**. The main paradigms are:

- 1. **Applications**. End-user programs that take advantage of GPU performance. Designed to take advantage of the GPU's processing power to accelerate performance (such as video processing software, scientific simulations, and machine learning models).
- 2. Libraries. Pre-built functions and routines optimized for GPUs. In other words, a collections of pre-written code and routines that are optimized to run on GPUs. Using these libraries, developers can avoid writing low-level GPU code. Examples of libraries are cuBLAS (for linear algebra), cuFFT (for Fast Fourier Transforms), and TensorFlow (for machine learning).
- 3. Compiler Directives. Special instructions embedded in the source code that guide the compiler on how to optimize and parallelize the code for GPU execution. OpenACC and OpenMP are commonly used directives.
- 4. **Programming Languages**. Languages or extensions of languages specifically designed for GPGPU programming. They provide the syntax and constructs needed to write code that executes on the GPU. Examples are CUDA and OpenCL (Open Computing Language).

Given an application code, in general:

- Serial Parts run on the CPU (host). These are the parts of the code that need to be executed sequentially and can benefit from the sophisticated control mechanisms of the CPU.
- Computation-Intensive and Data-Parallel Parts offloaded to the GPU (device). These parts can be executed in parallel, making use of the GPU's many cores for faster computation.

The flow inside the GPU can be described in three general steps:

- 1. Copy Input Data from CPU Memory to GPU Memory. The data is transferred over the PCI bus. This step is critical to prepare the data so that the GPU can access and process it.
- 2. Load GPU Program and Execute, Caching Data on Chip for Performance. The GPU program (kernel) is loaded and executed. Data is cached on the GPU chip to improve performance during execution. This step takes advantage of the parallel processing power of the GPU.
- 3. Copy Results from GPU Memory to CPU Memory. After calculation, the results are transferred back to the CPU memory via the PCI bus. This step is necessary to integrate the results into the larger application or for further processing on the CPU.

#### Common GPGPU issues and solutions

- Data Movement between CPU and GPU is the main Bottleneck.
  - Low Bandwidth. Data transfers between the CPU and GPU are relatively slow because they use the PCI Express (PCIe) bus, which has a bandwidth of about 12-14GB/s. This is much lower compared to the internal memory bandwidth of the CPU and GPU.
  - Relatively High Latency. Data transfer times can be significant, introducing delays that affect overall performance.
  - Data Transfer can take more time than the actual computation. In some cases, moving data between the CPU and GPU can take longer than the time it takes to perform the actual computations on the GPU. This is a critical point to consider when designing GPU-accelerated applications.
- Issues Porting CPU Applications to GPGPU.
  - Ignoring Data Movement can destroy GPU Performance Benefits. When converting CPU applications to run on a GPU, it's crucial to manage data transfers efficiently. Failing to do so can negate the performance advantages of using a GPU.
  - Solutions to Hide/Automate Data Transfer. Some programming techniques and tools can help hide or automate the data transfer process. These solutions can optimize performance by reducing the manual overhead of managing data movement.

In other words, efficient data management is the key to performance. In fact, the performance of GPGPU applications depends heavily on how well data is managed between the CPU and the GPU. Efficient data transfer strategies are essential to unleash the full computing power of GPUs.

## 7.2 CUDA Basics

CUDA, developed by NVIDIA, is a parallel computing platform and programming model that enables developers to harness the immense computational power of NVIDIA GPUs (Graphics Processing Units).

CUDA allows programmers to write code for GPUs using familiar programming languages like C, C++, and Fortran. This accessibility lowers the learning curve, enabling more developers to take advantage of GPU acceleration without requiring extensive knowledge of graphics programming.

The CUDA programming model evolves with the underlying hardware architecture, ensuring that developers can maximize performance gains from the latest GPU advancements. By writing a program for a single thread and instantiating it across many parallel threads, developers can achieve significant speedups for data-parallel tasks.

#### **X** The most important function: the kernel

A kernel is a function that runs on the GPU. When a kernel is launched, thousands of threads execute its code simultaneously. The programmer specifies the number of threads, each acting independently on different data elements. This approach leverages Single Instruction, Multiple Data (SIMD) and Single Program, Multiple Data (SPMD) parallelism.

```
Example 1: comparison between C and CUDA C program
  void vsum(int* a, int* b, int* c) {
1
       int i;
2
       for (i=0; i<N; i++) {</pre>
3
4
           c[i] = a[i] + b[i];
5
       }
6 }
7
8
  void main() {
       int va[N], vb[N], vc[N];
9
       . . .
       vsum(va, vb, vc);
11
12
13 }
    _global__ void vsum(int* a, int* b, int* c) {
2
       int i = ... // get unique thread ID
3
       c[i] = a[i] + b[i];
4 }
5
6 void main() {
       int va[N], vb[N], vc[N];
7
8
       . . .
       vsum<<<N, 1>>>(va, vb, vc);
9
10
11 }
12
```

In the CUDA version, the vsum function is defined as a kernel using the \_\_global\_\_ keyword, and it is launched on the GPU with a specified number of threads. Each thread processes a different element of the input arrays independently, showcasing CUDA's ability to handle parallel tasks efficiently.

#### 7.2.1 GPGPU Best Practices

NVIDIA provides a guide to help developers get the most out of NVIDIA CUDA GPUs:

CUDA C++ Best Practices Guide



Among the suggestions, NVIDIA explains a process for accelerating an application with NVIDIA GPUs called the *Cyclical Process for Accelerating Applications with NVIDIA GPUs*.

The Cyclical Process for Accelerating Applications with NVIDIA GPUs is a systematic approach designed to optimize and enhance the performance of applications by leveraging the computational power of NVIDIA GPUs. This process ensures that applications can take full advantage of the parallel processing capabilities of GPUs for improved performance and efficiency. The process consists of four main stages: Assess, Parallelize, Optimize, and Deploy.

- 1. Assess.
  - (a) **Locate Bottlenecks**. Identify the parts of our application where performance is limited. This involves profiling our application to understand where most of the computation time is spent.
  - (b) Estimate Parallelization Benefits. Determine the potential performance improvements from parallelizing the application. Evaluate how much of the workload can be efficiently offloaded to the GPU.

#### 2. Parallelize.

(a) Apply Libraries, Compiler Directives, or CUDA. Utilize GPUoptimized libraries (such as cuBLAS for linear algebra operations), apply compiler directives (like OpenACC) to guide the parallelization, or write custom CUDA kernels to parallelize the identified computational bottlenecks.

#### 3. Optimize.

- (a) **Apply Optimizations**. Fine-tune our GPU code to improve performance. This can include optimizing memory access patterns to reduce latency, ensuring efficient data transfer between the CPU and GPU, and maximizing thread utilization to fully exploit the GPU's parallel architecture.
- (b) Measure Performance Improvements. Continuously profile and benchmark our application to monitor the impact of the optimizations and ensure that they lead to significant performance gains.

#### 4. Deploy.

- (a) **Compare with Performance Estimations**. Verify that the performance improvements achieved through parallelization and optimization meet the initial estimations. This step ensures that the application performs as expected in a real-world environment.
- (b) **Move to Production**. Once satisfied with the performance, deploy the optimized application to production. This involves integrating the GPU-accelerated code into the main application and ensuring it runs efficiently in the production environment.

The process is depicted as a *continuous cycle*, indicating that **optimization** and assessment are ongoing activities. This iterative approach ensures that the application remains optimized and continues to benefit from GPU acceleration over time.

By following this cyclical process, developers can systematically **identify performance bottlenecks**, **efficiently parallelize** and **optimize** their **applications**, and **achieve significant performance improvements using NVIDIA GPUs**. This methodical approach helps ensure that the application takes full advantage of GPU capabilities, leading to faster, more efficient computing.

#### 7.2.2 Compilation

The compilation of a CUDA file follows a structured process that involves both the CPU and GPU components.

- 1. .cu File. The source file containing CUDA kernels and the rest of the application code is usually saved with a .cu extension.
- 2. **CUDA Kernels**. The CUDA-specific code within the .cu file is processed by the NVIDIA CUDA Compiler (NVCC). This includes all the functions intended to run on the GPU.
- 2. **Rest of the Application**. The non-CUDA parts of the code, intended to run on the CPU, are processed by the host CPU compiler.
- 3. **NVCC Compiler**. NVCC compiles the CUDA kernels into CUDA object files, which are specific to the GPU.
- 3. **CPU Compiler**. The CPU compiler processes the remaining application code into CPU object files, which are specific to the CPU.
- 4. Linker. The linker combines the CUDA object files and CPU object files into a single executable that can run on both the CPU and GPU.

An example of a compilation is the command:

```
nvcc -arch=sm_70 -o hello-gpu 01-hello/01-hello-gpu.cu -run
```

That demonstrates how to compile and execute a CUDA file using NVCC. The -arch=sm\_70 flag specifies the architecture of the GPU, in this case, the Volta architecture (sm\_70).

Useful Compilation Flags for NVCC:

Flags	Description
-x	Treat all input files as .cu files.
-Xcompiler	Pass a host compiler flag that is not supported
	by NVCC.
-g	Include host debugging symbols.
-G	Include device debugging symbols.
-lineinfo	Include line information with symbols.

Table 5: Some compilation flags.



Figure 36: CUDA Compilation Trajectory, source: NVIDIA CUDA Compiler Driver NVCC

#### 7.2.3 Debugging

Given the complexity and parallel nature of GPU programming, effective debugging tools are essential to ensure code correctness and optimize performance. NVIDIA provides a suite of **debugging tools** specifically designed for CUDA applications, helping developers identify and resolve issues in their code.

- cuda-memcheck is a comprehensive tool that detects memory-related errors in CUDA applications. It helps identify issues such as memory leaks, out-of-bounds accesses, and race conditions. Its capabilities:
  - Memory Leaks. Finds memory that is allocated but not freed, preventing unnecessary resource consumption.
  - Memory Errors. Detects accesses to invalid memory locations, which can cause unpredictable behavior.
  - Race Conditions. Identifies scenarios where multiple threads access shared data concurrently, potentially leading to incorrect results.
  - Illegal Barriers. Spots improper use of synchronization barriers in parallel code.
  - Uninitialized Memory. Flags the use of uninitialized memory, which can lead to unreliable outcomes.
- cuda-gdb is an extension of the GNU Debugger (GDB) tailored for debugging CUDA applications. It offers a familiar debugging environment for those already comfortable with GDB. Its capabilities:
  - Setting Breakpoints. Allows developers to pause execution at specific points in the code to inspect the state of the program.
  - Inspecting Memory. Enables examination of variables and memory contents to ensure they hold expected values.
  - **Stepping Through Code**. Provides the ability to step through code line by line, both on the CPU and GPU, to trace the execution flow.

With the debugging tools, there are also some profiling tools provided by NVIDIA.

**CUDA profiling**<sup>9</sup> is the process of measuring various aspects of a CUDA program's performance to **identify inefficient code segments**, **resource bottlenecks**, and **opportunities for optimization**. Profiling helps developers understand how their applications are utilizing GPU resources and make informed decisions to enhance performance.

• **NVPROF** is a command-line profiler provided by NVIDIA that **gives** detailed timing information for each CUDA kernel and memory operation. Its capabilities:

<sup>&</sup>lt;sup>9</sup>Profiling is a process used in software development to analyze and measure the performance characteristics of a program. The goal of profiling is to identify parts of the code that are consuming the most resources or taking the most time, so that developers can optimize these areas and improve the overall performance of the application.

- Kernel Execution Time. Measures the time taken by each CUDA kernel to execute.
- **Memory Transfers**. Monitors the time spent on data transfers between the CPU and GPU.
- API Calls. Tracks the duration of CUDA API calls.
- Occupancy. Analyzes the utilization of GPU resources, helping to identify potential underutilization or over-subscription of resources.

Developers use NVPROF to run their applications and generate detailed profiling reports, which can then be analyzed to pinpoint performance bottlenecks.

- **NVIDIA Visual Profiler (NVVP)** is a **graphical profiling tool** that provides a visual representation of the application's performance, making it easier to identify and address bottlenecks. Its capabilities:
  - Timeline Visualization. Displays a timeline of kernel executions, memory transfers, and API calls, allowing developers to see the sequence and overlap of events.
  - Detailed Metrics. Offers in-depth metrics on kernel performance, memory usage, and other critical aspects of CUDA applications.
  - Optimization Suggestions. Provides recommendations for optimizing code based on the profiling results.

NVVP is particularly useful for visualizing complex interactions within CUDA applications and understanding how different parts of the code affect overall performance.

- **NSIGHT** is an integrated development environment that includes **ad-vanced profiling and debugging features** for CUDA applications. Its capabilities:
  - Advanced Profiling. Combines the features of NVPROF and NVVP, offering a comprehensive set of profiling tools within a single interface.
  - Interactive Analysis. Allows developers to interactively analyze performance data and make real-time adjustments to their code.
  - Unified Development. Integrates debugging and profiling, providing a seamless environment for developing and optimizing CUDA applications.

NSIGHT is ideal for developers who need a powerful, all-in-one tool for debugging and profiling their CUDA applications.

- Third-Party Profiling Tools:
  - TAU (Tuning and Analysis Utilities). A performance analysis tool that can be used to profile CUDA applications along with other types of programs. TAU provides detailed performance data and visualization capabilities.

 VampirTrace. Captures performance data and visualizes it to help optimize parallel applications. It supports a range of profiling features for CUDA and other programming models.

Another powerful profiling system is Nsight. Nsight Systems offers both a command-line profiler and a graphical user interface (GUI), providing comprehensive insights into the execution of CUDA applications. It helps identify performance bottlenecks, understand GPU utilization, and improve overall application efficiency.

- Nsight Command-Line Profiler. nsys can be used to profile an accelerated application by launching it and gathering detailed statistics about its performance. The information reported are:
  - GPU Activity. Insights into how the GPU is utilized during the application's execution.
  - CUDA API Calls. Details on the usage of CUDA API functions.
  - Memory Activity. Information about memory operations, including transfers between CPU and GPU.

An example command is:

```
n nsys profile --stats=true -o vector-add-no-prefetch-report ./
vector-add-no-prefetch
```

This command profiles the application vector-add-no-prefetch and generates a report with detailed statistics.

- Nsight Systems GUI. Provides a visual representation of the profiling data collected by nsys, making it easier to analyze and interpret the results. Its capabilities:
  - **Timeline View**. Displays a comprehensive timeline of CPU and GPU activities, showing how different tasks are executed over time.
  - Detailed Metrics. Offers in-depth metrics on kernel performance, memory usage, and other critical aspects.
  - Interactive Analysis. Allows developers to zoom into specific regions of the timeline and examine detailed activities.

#### 7.2.4 CUDA Kernel

Launching a CUDA kernel involves defining a function that will run on the GPU and then executing this function from the host (CPU) code.

- 1. Defining functions.
  - CPU Function:

```
void CPUFunction() {
    printf("This function is defined to run on the CPU.");
}
```

This function runs on the CPU and prints a message.

• GPU Function:

```
1 __global__ void GPUFunction() {
2     printf("This function is defined to run on the GPU.");
3 }
```

This function is defined to run on the GPU, indicated by the **\_\_global\_\_** qualifier, and it prints a message when executed.

2. Launching the Kernel. In the main function, we launch the GPU function using a special syntax:

```
int main() {
    CPUFunction();
    // Launch the GPU kernel
    // with 1 block and 1 thread
    GPUFunction<<<1, 1>>>();
    cudaDeviceSynchronize();
  }
}
```

- The CPUFunction() is called normally, as it's a CPU function.
- The GPUFunction«<1, 1»>(); syntax launches the GPU kernel with a specified execution configuration: «<1, 1»> means 1 block and 1 thread per block.
- cudaDeviceSynchronize() is called to ensure that the CPU waits for the GPU to finish executing the kernel before continuing.

Just like with variables (table 4, page 132), CUDA provides specific keywords that define the scope and lifetime of functions.

Function Declaration	Executed on	Callable from		
device type DeviceFunc()	Device	Device		
global void KernelFunc()	Device	Host		
host type HostFunc()	Host	Host		

Table 6: CUDA function qualifiers.

#### • How can we customize the kernel?

Kernel configuration in CUDA involves specifying how many blocks and threads will be used to execute a kernel on the GPU. The key parameters are:

- Number of Blocks. Specifies how many blocks of threads will be launched on the GPU.
- Number of Threads per Block. Specifies how many threads will be in each block.

For a *1D hierarchy*, we use simple integer numbers to specify these values because a 1D grid or block can be represented by a single dimension:

```
1 // Example of launching a kernel with 1 block and 256 threads in 1D
2 KernelFunc <<<1, 256>>>();
```

For higher dimensions (2D or 3D), CUDA uses the dim3 type to represent the grid and block dimensions. dim3 is a CUDA-specific type that can hold three unsigned integer values, representing the dimensions in the x, y, and z directions. This provides a flexible way to configure more complex thread hierarchies:

```
    // Example of launching a kernel with a 2D grid and blocks
    dim3 gridDim(16, 16); // 16 blocks in x and y dimensions
    dim3 blockDim(16, 16); // 16 threads per block in x and y dimensions
    KernelFunc<<<gridDim, blockDim>>>();
```

#### \_\_\_\_\_

#### CPU-GPU Synchronization

In CUDA, kernel executions are asynchronous, meaning that the CPU can continue to execute other instructions while the GPU is running the kernel. However, there are times when synchronization is required to ensure that the CPU is waiting for the GPU to complete its tasks.

• Asynchronous Kernel Launch. When a kernel is launched, the CPU can proceed with subsequent instructions without waiting for the GPU to finish.

```
1 KernelFunc <<<1, 256>>>();
2 // The CPU immediately continues executing the next
instructions
```

• Synchronizing CPU and GPU. To synchronize, CUDA provides runtime functions such as cudaDeviceSynchronize(), which ensures that the CPU waits until the GPU has completed all preceding tasks.

```
1 KernelFunc <<<1, 256>>>();
2 // Wait for the GPU to finish
3 cudaDeviceSynchronize();
```

```
s cudubevicebynenionize(),
```

#### Error handling

The errors in CUDA can be caught in two ways:

- Return type: most CUDA runtime functions return a variable of type cudaError\_t. This type is an enumerated value that indicates the success or failure of the function call.
- Kernels return void: CUDA kernel functions return void, meaning they do not provide direct feedback about errors. Instead, errors are checked using specific functions, such as: cudaGetLastError(). It returns the last error that occurred during the execution of a CUDA function.

```
1 cudaError_t err = cudaGetLastError();
2 if (err != cudaSuccess) {
3     printf("CUDA error: %s\n", cudaGetErrorString(err));
4 }
5
```

Asynchronous errors (during kernel execution) are reported as error states of cudaDeviceSynchronize(). It blocks the CPU thread until the GPU has completed all previously requested tasks. This includes kernel executions, memory transfers, and other asynchronous operations issued.

```
1 kernel <<<blocks, threads >>>();
2 cudaError_t err = cudaDeviceSynchronize();
3 if (err != cudaSuccess) {
4     printf("CUDA error: %s\n", cudaGetErrorString(err));
5 }
```

Example 2: error handling

```
1 cudaError_t err1, err2;
2 err1 = cudaMallocManaged(&a, N);
3 SomeKernel<<<1, -1>>>(); // Invalid thread number
4 err2 = cudaGetLastError();
5 if (err1 != cudaSuccess || err2 != cudaSuccess) {
6 printf("Error 1: %s\n", cudaGetErrorString(err1));
7 printf("Error 2: %s\n", cudaGetErrorString(err2));
8 }
```

- err1 = cudaMallocManaged(&a, N); attempts to allocate managed memory and returns an error code if it fails.
- cudaGetErrorString(err1) converts the error code to a readable string.
- SomeKernel <<1, -1 >> (); intentionally uses an invalid thread configuration to generate an error.
- err2 = cudaGetLastError(); captures the error from the kernel launch.
- cudaGetErrorString(err2) converts the kernel launch error code to a readable string.

#### 7.3 Execution Model

The **CUDA execution model defines how parallel computing tasks are organized and executed on NVIDIA GPUs**. It consists of both software and hardware components that work together to efficiently process large amounts of data in parallel.

X Software Hierarchy

- Grid. A grid is a collection of thread blocks that execute a given kernel function. Each grid is associated with a specific kernel launch. Grids can be one-dimensional, two-dimensional, or three-dimensional, depending on the problem's complexity.
- Thread Block. A thread block is a group of threads that execute together and can cooperate by sharing data through shared memory. Each block is independent, allowing the scheduler to execute blocks in any order. Thread blocks can also be organized in one, two, or three dimensions.
- Thread. The smallest unit of execution in CUDA. Each thread executes the same code but operates on different data elements. Threads within a block can communicate and synchronize with each other, enabling collaborative computation.

#### 📟 Hardware Hierarchy

- **GPU**. The physical hardware that executes the parallel tasks. A GPU consists of multiple Streaming Multiprocessors (SMs).
- Streaming Multiprocessor (SM). Each SM can execute multiple threads concurrently. Thread blocks are assigned to SMs for execution. SMs manage and execute warps of threads.
- GPU Core. Individual cores within the SMs that perform the actual computation. Cores execute threads in groups called warps, typically comprising 32 threads.

# A What happens if the kernel startup doesn't match the input dataset?

Execution configuration mismatches occur when the number of threads configured for a kernel launch does not perfectly match the size of the dataset being processed. This can lead to *inefficiencies* or the need for *additional handling in the kernel code*.

• Optimal Thread Configuration: multiple of 32 threads. It's generally desirable to configure blocks with a multiple of 32 threads for performance reasons. This is because GPUs execute threads in groups of 32, known as warps. Ensuring the number of threads per block is a multiple of 32 can prevent under-utilization of GPU resources.

As the warp dimension changes, the optimal thread configuration should also change.

2

З

4

7

9



Figure 37: Graphical representation of the CUDA execution model.

- Dealing with Non-Multiple of 32 threads. If the dataset size (e.g., N=1000) is not a multiple of 32, we can create more than 1000 threads and use an extra check within the kernel to handle the excess threads.
  - 1. We pass the dataset size N as an argument to the kernel.
  - 2. Inside the kernel, we check if the thread ID is greater than or equal to N. If it is, those threads should not perform any operations.

```
__global__ void kernelFunction(float* data, int N) {
1
      int tid = blockIdx.x * blockDim.x + threadIdx.x;
      if (tid < N) {</pre>
          // Perform operations only if thread ID
          // is within the dataset size
          data[tid] = data[tid] * 2.0f;
6
      }
 }
8
```

• Insufficient threads. In some cases, there may be fewer threads than data elements to process, either for performance reasons or because the dataset is very large.

In this case, the solution is using a Stride Factor. We can use a stride factor corresponding to the total number of threads. The stride factor is calculated as gridDim.x \* blockDim.x, representing the total number of threads in the grid. Each thread processes multiple elements by iterating with a step size equal to the stride.

```
__global__ void kernelFunctionWithStride(float* data, int N) {
     int tid = blockIdx.x * blockDim.x + threadIdx.x;
      int stride = gridDim.x * blockDim.x;
      for (int i = tid; i < N; i += stride) {</pre>
          data[i] = data[i] * 2.0f;
      }
6
7
 }
```

# 7.4 Querying Device Properties

Different GPUs have varying capabilities and configurations, such as the number of Streaming Multiprocessors (SMs), maximum thread dimensions, memory size, etc. Knowing these properties helps developers optimize their code to run efficiently on different hardware. The main properties are:

• Get Device ID: cudaGetDevice; to retrieve the current device ID.

```
1 int deviceId;
```

```
2 cudaGetDevice(&deviceId);
```

• Query Device Properties: cudaGetDeviceProperties; to get the properties of the specified device.

```
1 cudaDeviceProp props;
```

```
2 cudaGetDeviceProperties(&props, deviceId);
```

- Understanding the cudaDeviceProp Structure. This structure contains numerous attributes of the device. Some key attributes include:
  - name. Name of the device.
  - totalGlobalMem. Total global memory available on the device.
  - sharedMemPerBlock. Shared memory available per block.
  - regsPerBlock. Number of registers available per block.
  - warpSize. Number of threads in a warp.
  - maxThreadsPerBlock. Maximum number of threads per block.
  - maxThreadsDim. Maximum dimension sizes of a thread block (x, y, z).
  - maxGridSize. Maximum dimension sizes of a grid (x, y, z).
  - clockRate. Clock frequency of the device.
  - multiProcessorCount. Number of streaming multiprocessors on the device.

# Example 3: common queries

Some common queries are:

• Maximum Dimensions of a Thread Block:

```
printf("Max Thread Dimensions: %d x %d x %d\n",
props.maxThreadsDim[0], props.maxThreadsDim[1],
props.maxThreadsDim[2]);
```

• Maximum Number of Threads in a Block:

```
printf("Max Threads per Block: %d\n",
props.maxThreadsPerBlock);
```


# 7.5 Thread hierarchy

The **CUDA thread hierarchy** is a fundamental concept in CUDA programming that allows for organizing and managing parallel computation tasks efficiently on NVIDIA GPUs. As we presented in Section 6.3.1, on page 103, the hierarchy consists of:

## 1. Threads

- **Basic Execution Unit**. A thread is the smallest unit of execution in CUDA. Each thread executes a portion of the overall computation.
- Unique Thread ID. Each thread within a block has a unique ID, which can be accessed using built-in variables like threadIdx.

#### 2. Thread Blocks

- Group of Threads. Threads are grouped into blocks. A thread block can contain up to 1024 threads, depending on the GPU architecture.
- Cooperation and Communication. Threads within the same block can cooperate and share data through shared memory, and they can synchronize using \_\_syncthreads().
- Unique Block ID. Each block within a grid has a unique ID, which can be accessed using blockIdx.

## 3. Grids

- Collection of Blocks. Blocks are grouped into a grid. A grid can contain up to 2<sup>31</sup> - 1 blocks<sup>10</sup>.
- Grid Dimensions. Grids can be one-dimensional, two-dimensional, or three-dimensional. Each block within a grid has a unique position within the grid, identified using blockIdx.x, blockIdx.y, and blockIdx.z.

## **E GPU** hierarchy

This hierarchy maps directly to the NVIDIA GPU architecture (hardware hierarchy):

- 1. Streaming Multiprocessor (SM).
  - Block Execution. Each Streaming Multiprocessor (SM) on a GPU executes one or more thread blocks.
  - Warps. Threads within a block are executed in groups of 32, known as warps. Warps are the basic unit of execution on the GPU.

 $<sup>^{10}</sup>$ The limit of  $2^{31} - 1$  blocks in CUDA grid comes from the maximum range of signed 32-bit integer. CUDA uses signed 32-bit integers to represent the indices of blocks within a grid. A signed 32-bit integer can represent values from  $-2^{31}$  to  $2^{31} - 1$ . Since negative block indices don't make sense in the context of a grid, CUDA only uses positive values. Therefore, the maximum positive value that can be used is  $2^{31} - 1$ , which equals 2'147'483'647.

## 2. GPU Core.

- Thread Execution. Each GPU core executes a single thread from a warp. Multiple GPU cores within an SM work together to execute all the threads in a warp.
- 3. Execution of Grids.
  - Multiple Grids. A GPU can execute one or more grids of thread blocks. Each grid corresponds to a single kernel launch.
  - Interleaved Execution. If the number of blocks exceeds the number of SMs, the execution of blocks is interleaved among the SMs.

#### **?** How to use the hierarchy

The CUDA thread hierarchy (and hardware hierarchy) provides a structured way to manage and organize parallel computation on the GPU. Unconsciously, when we coordinate parallel threads to execute a task, we leverage this hierarchy to maximize performance and resource utilization:

• Kernel Launch Configuration. When launching a kernel, we specify the grid and block dimensions. For example:

```
1 // 256 threads per block
2 dim3 dimBlock(256);
3 // Grid size to cover all elements
4 dim3 dimGrid((N + 256 - 1) / 256);
5 MyKernel<<<dimGrid, dimBlock>>>(a, b, N);
```

This configuration ensures that the kernel has enough threads to process all elements in parallel.

• Mapping Threads to Data. Each thread calculates its unique index based on its position within the block and grid, allowing it to process a specific element of the data array. For example:

```
1 int i = blockIdx.x * blockDim.x + threadIdx.x;
2 if (i < N) {
3 // Each thread processes a unique element
4 a[i] = a[i] + b;
5 }
```

• Handling Data Beyond Block Size. If the data size exceeds the number of threads per block, the grid dimension ensures all data is covered. For example:

```
dim3 dimGrid((N + blocksize - 1) / blocksize);
```

This calculation ensures that even if  ${\tt N}$  is not a multiple of the block size, the entire dataset is processed.

• Scalability. The hierarchy allows the program to scale across different GPU architectures by adjusting the grid and block sizes to match the hardware capabilities (e.g., number of SMs, maximum threads per block).

# X Thread hierarchy Variables

CUDA provides several built-in variables to help manage and identify the hierarchy of threads in our parallel computation. These variables are used within kernel functions to determine the unique identity of each thread, block, and grid:

- Grid and Block Dimensions:
  - gridDim.x: represents the number of blocks in the grid along the x-axis.
  - blockDim.x: represents the number of threads in a block along the x-axis.
- Block and Thread Indices:
  - blockIdx.x: the block index along the x-axis. It ranges from 0 to gridDim.x - 1.
  - threadIdx.x: the thread index within a block along the x-axis. It ranges from 0 to blockDim.x 1.
- Global Thread Index Calculation: to identify the unique index of each thread across the entire grid, we can use the formula:

 $globalID = blockIdx.x \times blockDim.x + threadIdx.x$  (13)

This formula computes the global thread index by combining the block and thread indices.

• 2D/3D Structures: in more complex applications, such as image processing or solving partial differential equations, threads use their IDs to decide which data to process. This simplifies memory addressing when dealing with multidimensional data. Example of thread index calculations in a 2D grid:

- Threads Per Block and Thread Number in Block:
  - threadsPerBlock: total number of threads in a block.

 $threadsPerBlock = blockDim.x \times blockDim.y = 8$ 

- threadNumInBlock: unique thread number within a block.

 $\texttt{threadNumInBlock} = \texttt{threadIdx.x} + \texttt{blockDim.x} \times \texttt{threadIdx.y}$ 

- blockNumInGrid: unique block number within the grid.

 $blockNumInGrid = blockIdx.x + gridDim.x \times blockIdx.y$ 

- tid (Global Thread ID): unique thread ID across the entire grid.

 $\texttt{tid} = \texttt{blockNumInGrid} \times \texttt{threadsPerBlock} + \texttt{threadNumInBlock}$ 

# 7.6 Memory hierarchy

The memory hierarchy in CUDA was explained in Section 6.3.2, page 107. Here is a small summary:

- **Per-thread** (registers):
  - Scope: Per thread.
  - Lifetime: Duration of the thread.
  - Speed: Fastest memory in the CUDA memory hierarchy.
  - Usage: Used for storing frequently accessed variables and temporary data.
  - Limitations: Limited in size; excessive usage can lead to spilling into local memory, which is slower.
- **Per-block** (shared memory, cache):
  - Scope: Per block.
  - Lifetime: Duration of the block.
  - **Speed**: Much faster than global memory, similar to L1 cache.
  - **Usage**: Used for data sharing among threads within the same block, enabling efficient inter-thread communication.
  - Configuration: Typically user-managed, allowing for explicit control over data placement.
  - Limitations: Limited in size; excessive usage can limit the number of active blocks per SM.
- **Global Memory** (off-chip DRAM):
  - **Scope**: All threads.
  - Lifetime: Duration of the application.
  - Speed: Significantly slower than shared memory and registers due to higher latency.
  - Usage: Used for data that needs to be accessed by multiple threads or blocks.
  - Characteristics: Large in size, but high latency; optimizing access patterns (coalesced accesses) can improve performance.

# **E** Memory Accessibility

# • Per-thread:

- Host: cannot directly access registers.
- Device: registers are accessed exclusively by the thread that owns them.
- Operations:
  - \* **Host**: none. The host cannot allocate, deallocate, or access registers directly.
  - \* **Device**: each thread can read from and write to its own registers. But registers are private to the thread, meaning *no other thread* can access another thread's registers.

# • Per-block:

- Host: cannot directly access shared memory, but can specify shared memory size for each kernel launch.
- Device: can read from and write to shared memory within a block.
- Operations:
  - \* **Host**: none directly (can specify size in kernel launch).
  - \* **Device**: Read/Write.
- Global Memory:
  - Host: can allocate and deallocate memory using cudaMalloc and cudaFree. Can copy data to/from global memory using cudaMemcpy.
  - Device: can read from and write to global memory directly.
  - Operations:
    - \* Host: cudaMalloc, cudaFree, cudaMemcpy, cudaMemset.
    - \* **Device**: Read/Write.

## **Memory Management APIs**

#### • cudaMalloc:

- **Purpose**: allocates memory on the GPU.
- **Usage**: used when we need to allocate space for variables or arrays that the GPU will use.
- Function signature:
- 1 cudaError\_t cudaMalloc(void\*\* devPtr, size\_t size);
- Parameters:
  - \* devPtr: pointer to the allocated device memory.
  - \* size: size in bytes of the allocated memory.
- Example:

```
1 float* d_array;
```

```
2 cudaMalloc((void**)&d_array, N * sizeof(float));
```

## • cudaMallocHost:

- Purpose: allocates pinned memory on the host.
- Usage: used for host memory that can be asynchronously copied to the device, improving transfer efficiency.
- Function signature:

```
cudaError_t cudaMallocHost(void** ptr, size_t size);
```

- Parameters:
  - \* ptr: pointer to the allocated host memory.
  - \* size: size in bytes of the allocated memory.
- Example:

```
1 float * h_array;
```

```
2 cudaMallocHost((void**)&h_array, N * sizeof(float));
```

# • cudaFree:

- Purpose: frees memory that was allocated on the GPU.
- Usage: used to deallocate memory that was previously allocated with cudaMalloc.
- Function signature:
- 1 cudaError\_t cudaFree(void\* devPtr);
- Parameters:
  - \* devPtr: pointer to the memory to be freed.
- Example:
- 1 float\* d\_array;

```
2 cudaFree(d_array);
```

#### • cudaFreeHost:

- Purpose: frees pinned memory that was allocated on the host.
- Usage: used to deallocate memory that was previously allocated with cudaMallocHost.
- Function signature:
- 1 cudaError\_t cudaFreeHost(void\* ptr);
- Parameters:
  - \* ptr: pointer to the memory to be freed.
- Example:

```
1 float* h_array;
```

```
2 cudaFreeHost(h_array);
```

### • cudaMemcpy:

- Purpose: copies data between host and device, or between different regions of device memory.
- Usage: used for transferring data to and from the GPU, or between different memory regions on the GPU.
- Function signature:

- Parameters:

- \* dst: destination pointer.
- \* src: source pointer.
- \* count: size in bytes of the memory to be copied.
- Example:

## **A** cudaMallocHost/cudaFreeHost can reduce CPU performance

**Pinned memory** (or page-locked memory) is a **region of system memory that is "locked" and cannot be paged out by the operating system**. This type of memory provides faster data transfer rates between the CPU and GPU because it allows for direct memory access (DMA) without the need for the CPU to perform intermediate steps. Since cudaMallocHost and cudaFreeHost work on this type of memory, the possible worst-case scenarios are:

✗ Limited System Resources. Pinned memory consumes physical RAM. When we allocate a large amount of pinned memory, it reduces the available RAM for other system tasks, which can lead to increased memory pressure and reduced performance for other applications. ✗ Increased Memory Allocation Time. Allocating pinned memory (cudaMallocHost) is generally more time-consuming than allocating pageable memory because the operating system must ensure that the allocated memory pages are locked in RAM and cannot be paged out.

Similarly, freeing pinned memory (cudaFreeHost) involves unlocking these pages, which can also be a time-consuming operation.

- ★ Memory Fragmentation. Frequent allocations and deallocations of pinned memory can lead to memory fragmentation. Over time, this fragmentation can make it harder for the operating system to find contiguous blocks of free memory, which can slow down memory allocation and deallocation operations.
- ✗ Reduced Cache Efficiency. Pinned memory allocations can affect the CPU's cache efficiency. When a large portion of memory is pinned, it may reduce the effectiveness of the CPU's memory caching mechanisms, leading to increased memory access times for other processes.

Is suggest to use the pinned memory when:

- ✓ Performance-Critical Data Transfers. Use pinned memory for data transfers that are critical for performance, where the speedup from faster data transfer rates outweighs the potential downsides.
- ✓ Async Operations. Pinned memory is particularly beneficial for asynchronous data transfers between the host and device, enabling overlap of computation and data transfer for better performance.

**Example 4: Manual Memory Management - Vector Addition** 

```
1 % allocate h_A, h_B, h_C
2 void vecAdd(float *h_A, float *h_B, float *h_C, int n) {
      int size = n * sizeof(float);
3
      float *d_A, *d_B, *d_C;
4
5
      // Allocate memory on the GPU (device)
6
      // for arrays d\_A\,,\ d\_B\,,\ d\_C
7
      cudaMalloc((void**)&d_A, size);
8
      cudaMalloc((void**)&d_B, size);
9
      cudaMalloc((void**)&d_C, size);
      // Copy data from host arrays h_A and h_B
13
      // to device arrays d_A and d_B
      cudaMemcpy(d_A, h_A, size, cudaMemcpyHostToDevice);
14
      cudaMemcpy(d_B, h_B, size, cudaMemcpyHostToDevice);
17
      // Kernel invocation code (not shown in the image)
      // Example kernel launch:
18
      // vecAddKernel <<<blocks, threads>>>(d_A, d_B, d_C, n);
19
20
      // Copy the result from device array
21
       // d_C back to host array h_C
22
      cudaMemcpy(h_C, d_C, size, cudaMemcpyDeviceToHost);
23
24
```

```
// Free the allocated memory on the device
cudaFree(d_A);
cudaFree(d_B);
cudaFree(d_C);
}
30 % free h_A, h_B, h_C
```

- Allocate Host Memory. Before the vecAdd function is called, host memory for arrays h\_A, h\_B, and h\_C is allocated. This memory is used to store the input data and the result on the host (CPU).
- Function Definition. The vecAdd function performs the steps in the code.
- Memory Allocation on Device. cudaMalloc allocates memory on the GPU for d\_A, d\_B, and d\_C. The size of each array is determined by n \* sizeof(float).
- Copy Data from Host to Device. cudaMemcpy copies data from the host arrays h\_A and h\_B to the device arrays d\_A and d\_B using the cudaMemcpyHostToDevice flag. This step transfers the input data from the CPU to the GPU for processing.
- Kernel Invocation. The CUDA kernel (not shown in the image) is invoked to perform vector addition on the device. Each thread on the GPU computes one element of the result vector.
- Copy Data from Device to Host. cudaMemcpy copies the result from the device array d\_C back to the host array h\_C using the cudaMemcpyDeviceToHost flag. This step transfers the computed result from the GPU to the CPU.
- Free Allocated Memory. cudaFree frees the allocated memory on the GPU for d\_A, d\_B, and d\_C. This ensures that no memory leaks occur on the GPU.

• How can we allocate memory that is shared between CPU and GPU?

**Unified Memory in CUDA** is a single memory space that is accessible by both the host (CPU) and the device (GPU). It abstracts away the complexities of explicit memory management, making it easier to develop CUDA applications. Its features:

- Single Address Space. Both the CPU and GPU can access the same memory location, *eliminating the need for explicit data transfers between them.* This means that the same pointer can be used on both the host and the device.
- Automatic Data Migration. The CUDA runtime system handles the movement of data between the host and device automatically. When the

GPU accesses data that resides in the host memory, the CUDA runtime migrates the data to the GPU memory and vice versa.

- On-Demand (Page) Migration. Unified Memory uses a demandpaging mechanism similar to virtual memory in operating systems. When a page of memory is accessed by the CPU or GPU, and it is not currently resident in the respective memory, it is migrated on demand.
- **Pros** 
  - ✓ Simplified Memory Management. Developers do not need to worry about explicit memory copies (cudaMemcpy). The CUDA runtime manages data movement automatically.
  - Ease of Programming. Writing CUDA programs becomes easier, especially for those new to CUDA, as the same pointer can be used for both host and device operations.
  - Efficient Use of Memory. Reduces code complexity, as there is no need for separate host and device memory allocations and management.

#### 8 Cons

➤ Potential Performance Overhead. The automatic data migration can introduce runtime overhead due to page faults<sup>11</sup> when data is accessed.

Unified Memory uses a similar (to operating system) paging mechanism to manage memory across the CPU and GPU. When a memory page is accessed by the CPU or GPU and is not present in the respective memory (host or device), a page fault occurs. The CUDA runtime automatically migrates the page from the current memory location (host to device or device to host) to the memory where the access occurred.

This can be less efficient compared to explicitly managed memory transfers.

- ➤ Limited Control. Developers have less control over when and where data is moved. For performance-critical applications, manual memory management can sometimes yield better performance.
- ✗ Memory Contention. Sharing the same memory space between the CPU and GPU can lead to contention, potentially impacting performance if both are trying to access the same memory simultaneously.

<sup>&</sup>lt;sup>11</sup>Modern operating systems use a virtual memory system where the physical memory (RAM) is abstracted as a larger virtual memory space. This allows programs to use more memory than physically available by using disk storage (paging). A page fault occurs when a program tries to access a part of the memory that is not currently in the physical memory (RAM). The operating system intervenes to load the required memory page from disk into RAM, allowing the program to continue execution.

cudaMallocManaged is a function in CUDA that allocates managed memory, which is accessible by both the host (CPU) and the device (GPU). This unified memory simplifies the programming model by allowing both the CPU and GPU to share a single memory space.

cudaError\_t cudaMallocManaged(void \*\*devPtr, size\_t size);

- devPtr: pointer to the allocated unified memory.
- size: size in bytes of the allocated memory.

How to avoid page faults with cudaMallocManaged

Asynchronous memory prefetching is a technique used to proactively move data between the host and device to avoid page faults and improve performance. This is particularly useful in Unified Memory, where data can be accessed by both the CPU and GPU.

Instead of waiting for a page fault to occur (which would trigger an on-demand data transfer, a scenario we would avoid due to performance overhead), we prefetch the required data to the desired memory location before it is needed. This **operation is done asynchronously**, meaning that it **does not block the execution of other operations**. This allows the program to continue running while the data is being transferred in the background.

In CUDA, this technique is used with the function cudaMemPrefetchAsync:

- devPtr: pointer to the memory to be prefetched.
- count: size of the memory to be prefetched, in bytes.
- dstDevice: the destination device (can be a GPU device ID or the result of the function cudaCpuDeviceId for the host).
- stream: the stream to perform the operation in (optional).

An **example** of use:

```
int deviceId;
cudaGetDevice(&deviceId);
// Prefetch data to the device
cudaMemPrefetchAsync(pointerToSomeUMData, size, deviceId);
// Prefetch data back to the host
cudaMemPrefetchAsync(pointerToSomeUMData, size, cudaCpuDeviceId);
```

## 7.7 Streams

**CUDA Streams** are sequences of operations (like kernel launches or memory copies) that execute in order. By *default*, all operations in CUDA run in the default stream, which is *blocking* and *sequential*.

Is important to understand the CUDA streams, because by changing the default order, we can gain performance:

- Concurrency. By using multiple streams, we can **perform operations** in **parallel**, leading to better performance.
- Overlap Computation and Data Transfer. For example, while one stream is running a kernel on the GPU, another stream can be copying data to or from the GPU.

# Default vs Non-Default Streams

- Default Stream:
  - Executes operations **sequentially**.
  - Blocks all other streams until its operations are complete.
- Non-Default Streams:
  - Allow for **concurrent** execution of operations.
  - Operations within the same stream execute sequentially, but operations in different streams can run in parallel.

# **X** CUDA implementation

1. Creating Streams. We can create streams using cudaStreamCreate.

```
1 cudaStream_t stream1, stream2;
2 cudaStreamCreate(&stream1);
```

- 3 cudaStreamCreate(&stream2);
- 2. Launching Kernels in Streams. Launch kernels in different streams to execute them concurrently.

```
1 // Launching a kernel in stream1
2 kernel1<<<blocks, threads, 0, stream1>>>(...);
3
4 // Launching a kernel in stream2
5 kernel2<<<blocks, threads, 0, stream2>>>(...);
```

3. Synchronizing Streams. We can synchronize individual streams or all streams.

```
1 // sync specific stream:
2 cudaStreamSynchronize(stream1);
3
4 // sync all streams
5 cudaDeviceSynchronize();
```

4. **Destroying Streams**. Once we're done with the streams, it's important to destroy them to free up resources.

```
1 cudaStreamDestroy(stream1);
2 cudaStreamDestroy(stream2);
```

# Example 5

Imagine we have two kernels to execute, kernel1 and kernel2. If we use the default stream, they will execute one after the other:

- 1. Launch kernel1;
- 2. Wait for kernel1 to complete;
- 3. Launch kernel2;
- 4. Wait for kernel2 to complete.

This sequential execution means the GPU is not fully utilized. Using two non-default streams, we can launch both kernels to execute concurrently:

1. Create two streams:

```
1 cudaStream_t stream1, stream2;
2 cudaStreamCreate(&stream1);
```

```
3 cudaStreamCreate(&stream2);
```

2. Launch kernel1 in stream1 and kernel2 in stream2:

```
1 kernel1<<<blocks, threads, 0, stream1>>>(...);
2 kernel2<<<blocks, threads, 0, stream2>>>(...);
```

Now, kernel1 and kernel2 can run in parallel, allowing the GPU to be used more efficiently.



```
2. Tasks A1, A2, and A3 in Different Streams:
1 // Stream 1
2 kernelA1<<<blocks, threads, 0, stream1>>>(...);
3 // Stream 2
4 kernelA2<<<blocks, threads, 0, stream2>>>(...);
5 // Stream 3
6 kernelA3<<<blocks, threads, 0, stream3>>>(...);
```

3. Synchronize Streams Before Dependent Tasks:

```
cudaStreamSynchronize(stream1);
cudaStreamSynchronize(stream2);
cudaStreamSynchronize(stream3);
```

4. Tasks A4, A5, A6, and A7 in Non-Default Streams:

```
1 // Stream 1
2 kernelA4<<<blocks, threads, 0, stream1>>>(...);
3 // Stream 2
4 kernelA5<<<blocks, threads, 0, stream2>>>(...);
5 // Stream 1
6 kernelA6<<<blocks, threads, 0, stream1>>>(...);
7 // Stream 2
8 kernelA7<<<blocks, threads, 0, stream2>>>(...);
```

5. Synchronize Streams Again Before Final Task:

```
1 cudaStreamSynchronize(stream1);
2 cudaStreamSynchronize(stream2);
3 cudaStreamSynchronize(stream3);
6. Task A8 in Default Stream:
1 kernelA8<<<blocks, threads>>>(...); // Default stream
```

7. Destroying Streams:

```
1 cudaStreamDestroy(stream1);
```

```
2 cudaStreamDestroy(stream2);
3 cudaStreamDestroy(stream3);
```

```
3 cudastreamDestroy(stream3
```

Using concurrent CUDA streams helps manage complex task dependencies in DAG-like applications. By running independent tasks in different streams, we can achieve parallel execution and optimize the performance of our CUDA applications. The example shows how to create streams, start kernels in these streams, synchronize them, and finally destroy the streams to free up resources. Finally, non-default streams and manual memory management allow for overlapping data transfers and computations.

# 7.8 CUDA and OpenMP or MPI

## 7.8.1 Motivations

In today's computing landscape, achieving high performance and efficiency in complex applications often requires the power of parallel processing. This need has given rise to several parallel computing frameworks, each designed to address specific aspects of parallelism. Among these, CUDA, OpenMP, and MPI stand out as key technologies that enable efficient utilization of computing resources, whether on a single machine with multiple GPUs or across distributed clusters.

# 2 Systems with multiple GPUs - CUDA + OpenMP

### • OpenMP

- Purpose: used to dispatch parallel tasks across multiple GPUs.
- Why OpenMP?
  - \* **Simplified Parallelism**. OpenMP provides a straightforward way to parallelize tasks using compiler directives.
  - \* **Task Scheduling**. It allows for efficient scheduling and management of tasks across multiple GPUs.
  - \* **Shared Memory Model**. OpenMP works well with shared memory systems, making it easier to manage and synchronize tasks.

# • CUDA

- Purpose: used for programming NVIDIA GPUs to perform parallel computations.
- Why CUDA?
  - \* **Fine-Grained Control**. CUDA provides detailed control over GPU resources and performance optimization.
  - \* Massive Parallelism. Enables the execution of thousands of threads in parallel, maximizing GPU utilization.
  - \* **Optimized Performance**. Designed specifically for NVIDIA GPUs, ensuring optimal performance and efficiency.

OpenMP is particularly useful for tasks that benefit from shared memory parallelism, making it easier to write efficient and portable code for multi-core processors. It is often used in conjunction with CUDA to manage the CPU-side parallelism, thereby optimizing the performance of the entire system.

# Distributed Clusters with Multiple Nodes Containing GPUs - CUDA + MPI

**MPI** (Message Passing Interface) is a standardized and portable message-passing system designed for parallel computing in distributed memory environments, such as clusters of computers. MPI excels in managing communication between nodes in a distributed system, allowing for efficient coordination and data exchange. When combined with CUDA, MPI enables developers to scale their applications across multiple nodes, each leveraging the power of GPUs, thus tackling larger and more complex problems than would be possible on a single machine.

- MPI
  - Purpose: used for communication across nodes in a distributed system.
  - Why OpenMP?
    - \* **Scalability**. MPI is designed for high-performance communication in distributed memory systems, allowing for efficient parallel computing across multiple nodes.
    - \* **Inter-Node Communication**. Provides robust mechanisms for data exchange between nodes, ensuring coordination and synchronization in distributed environments.
    - \* **Flexibility**. Works with various hardware and software configurations, making it versatile for different parallel computing scenarios.

# • CUDA

- Purpose: used within each node's GPU to perform parallel computations.
- Why CUDA?
  - \* **Performance**. Ensures that computations within each GPU are optimized for maximum throughput.
  - \* **Integration with MPI**. CUDA can be effectively combined with MPI to handle local computations within each node, while MPI manages communication between nodes.

# Example 7: Scenario CUDA + MPI

A distributed cluster with multiple nodes, each containing one or more GPUs. MPI processes (e.g., MPI Process N, MPI Process N+1) manage communication across nodes, while CUDA handles computations within each GPU.

Technology	When?
OpenMP	
	• Ideal for managing parallel tasks within a single system with multiple GPUs.
	• Simplifies task scheduling and synchronization in shared memory environments.
MPI	
	• Essential for communication in distributed clusters with multiple nodes containing GPUs.
	• Provides scalable and efficient data exchange be- tween nodes.
CUDA	
	• Used for fine-grained parallel computations within each GPU.
	• Ensures optimized performance and maximum GPU utilization.

Table 7: When to use each technology.

# **A** Batch processing vs Cooperative patterns

The computation patterns in a Multi-GPU environment are divided into batch and cooperative patterns.

- Batch Processing. Batch processing is ideal for scenarios where the same task needs to be performed multiple times with different data sets. It's a simple way to maximize GPU utilization. In other words, run the same independent task multiple times with different data. Steps involved:
  - 1. **Identify the number of available GPUs**. Use CUDA APIs to determine how many GPUs are available for processing.
  - 2. Initialize and allocate memory. Allocate necessary memory on each GPU. This step involves copying the data required for computation from the host (CPU) to the device (GPU).
  - 3. Create CUDA streams. CUDA streams enable concurrent execution of kernels. Creating multiple streams allows us to run multiple tasks in parallel on the GPU.
  - 4. Launch the kernel. Dispatch the kernels for execution. Each GPU runs its own copy of the kernel, processing a different subset of the data.

- 5. Synchronize. Ensure all GPU tasks are complete. Use synchronization mechanisms to manage dependencies and ensure data integrity.
- 6. **Retrieve results**. Copy the results from the device back to the host.

## Pros

- ✓ **High throughput**. Efficiently handles repetitive tasks.
- ✓ Scalability. Easy to scale by adding more GPUs.

# Cons

- ✗ Limited to independent tasks. Not suitable for tasks that require inter-GPU communication.
- Cooperative Patterns. Tasks need to work together to achieve a common goal. These tasks are interdependent and require communication between GPUs.

Steps involved:

- 1. **Task division**. Split the task into smaller sub-tasks that can be distributed across GPUs.
- 2. Memory allocation and initialization. Allocate memory for each sub-task and initialize the required data.
- 3. **Kernel execution**. Launch kernels that perform the sub-tasks. Unlike batch processing, these kernels may need to communicate with each other.
- 4. **Inter-GPU communication**. Implement communication protocols to share data and results between GPUs. This can involve techniques like GPU direct RDMA (Remote Direct Memory Access).
- 5. Synchronization and coordination. Use synchronization mechanisms to coordinate the execution of sub-tasks and ensure they are completed in the correct order.
- 6. **Result aggregation**. Combine the results from all GPUs to produce the final output.

## **Pros**

- ✓ Solves complex tasks. Suitable for problems that require collaborative computation.
- ✓ Efficient use of resources. Leverages the combined power of multiple GPUs.

# Cons

- ✗ Complex implementation. Requires careful design and management of inter-GPU communication.
- ➤ Potential bottlenecks. Synchronization and communication can introduce delays.

The main differences are:

- Task Independence vs. Interdependence. Batch processing excels with independent tasks, whereas cooperative patterns manage interdependent tasks.
- Communication Needs. Batch processing minimizes communication between tasks, while cooperative patterns facilitate necessary intertask communication.
- Implementation Complexity. Batch processing is generally simpler to implement, whereas cooperative patterns require more sophisticated design and coordination.

By dividing the computation patterns this way, it becomes easier to choose the most appropriate approach for different types of workloads, ensuring optimal performance and efficient use of GPU resources.

# 7.8.2 CUDA API for Multi-GPUs

In high-performance computing, the use of multiple GPUs can significantly increase computational throughput and efficiency. **CUDA provides several API calls that allow developers to effectively manage and utilize multiple GPUs**. The most important of these are:

- The cudaSetDevice() function is used to specify which GPU device should be active for subsequent CUDA operations on the host thread. By setting the desired GPU device, developers can control where kernel executions, memory allocations, and other device-specific calls take place. This feature is especially important when working with systems that have multiple GPUs, as it allows fine-grained control over which device is used for specific tasks.
  - Function:
  - 1 cudaSetDevice(int device)
  - Description:
    - \* Sets the GPU device to use for subsequent CUDA operations on the active host thread.
    - \* This function specifies which GPU to use for operations like kernel launches, memory allocations, and other device-specific calls.
  - Parameters:
    - \* device: the integer ID of the GPU to be set as the active device.
  - Usage:
    - \* Does not affect other host threads, meaning the device setting is local to the thread where this function is called.
    - \* Does not affect previous asynchronous calls.
  - Example:

1 cudaSetDevice(0); // Sets GPU 0 as the active device

## CUDA Runtime Calls Affected by cudaSetDevice()

If cudaSetDevice() is called before:

- Kernel Launch. The kernel will execute on the specified active device.
- Memory Allocations. All memory allocations will be made on the specified active device.
- Stream Creation. The stream will be associated with the specified active device.
- Synchronization Functions. These functions will synchronize tasks on the specified active device and active host thread only.

• The cudaGetDevice() function retrieves the ID of the GPU currently being used by the active host thread. This function is useful for confirming which GPU is set as active, especially in debugging scenarios. Knowing the active device ensures that operations are being performed on the intended GPU, preventing potential errors and resource conflicts.

```
– Function:
```

- 1 cudaGetDevice(int \*device)
- Description:
  - \* Retrieves the ID of the GPU currently being used by the active host thread.
  - \* Helps to confirm which GPU is currently set as active.
- Parameters:
  - \* device: a pointer to an integer where the ID of the active device will be stored.
- Usage:
  - \* This function is useful for debugging and ensuring that the correct GPU is being utilized.
- Example:

```
1 int device;
2 // Gets the ID of the current active GPU
3 // and stores it in 'device'
4 cudaGetDevice(&device);
```

- The cudaGetDeviceCount() function is used to determine the number of CUDA-capable GPUs available in the system. This function is typically called during the initialization phase to understand the GPU resources available. By knowing the number of GPUs, developers can design their applications to efficiently distribute workloads across multiple devices, maximizing performance and resource utilization.
  - Function:

```
1 cudaGetDeviceCount(int *count)
```

- Description:
  - \* Determines the number of CUDA-capable GPUs available in the system.
  - \* Helps in discovering the total number of GPUs that can be utilized for computation.
- Parameters:
  - \* count: a pointer to an integer where the number of CUDAcapable devices will be stored.

# - Usage:

- \* This function is typically called during the initialization phase to understand the GPU resources available.
- Example:
- int deviceCount;
- 2 // Gets the number of CUDA-capable GPUs
  3 // and stores it in 'deviceCount'
- 4 cudaGetDeviceCount(&deviceCount);

### 7.8.3 Memory Management with Multiple GPUs

In systems with multiple GPUs, efficient memory management is critical to optimizing performance and ensuring smooth operation. There are two primary approaches to memory management in such environments: manual memory management and unified memory.

• Manual Memory Management requires setting the active device using the cudaSetDevice() (page 202) function before any memory allocation or kernel launch. This ensures that subsequent operations are directed to the specified GPU.

For example, setting GPU 0 as the active device allows for memory allocation on that particular GPU. This method provides fine-grained control over which GPU handles specific tasks, allowing for optimized resource utilization.

- Unified Memory, on the other hand, offers a more automated approach. If the flag cudaDevAttrConcurrentManagedAccess:
  - Is set for all devices, memory can be allocated using the function cudaMallocManaged() without the need to set the active device. This simplifies the process by allowing all GPUs to access the allocated memory automatically.
  - Is not set, but devices can still access each other's memory, it becomes necessary to set the active device before memory allocation. This setup ensures that all other devices can access the data through PCIe, facilitating efficient data transfer and resource sharing.

## Example 8: vector addition with multiple GPUs

This example demonstrates how to perform vector addition using multiple GPUs.

```
1 float *m_AO, float *m_BO, *m_A1, float *m_B1, int n;
2
  int size = n * sizeof(float);
_4 // Set the active device to GPU 0
  cudaSetDevice(0);
6 // Allocate memory on GPU (device) 0
7 cudaMalloc((void**) &m_A0, size);
  cudaMalloc((void**) &m_B0, size);
8
10 // Set the active device to GPU 1
11 cudaSetDevice(1):
12 // Allocate memory on GPU (device) 1
13 cudaMalloc((void**) &m_A1, size);
14 cudaMalloc((void**) &m_B1, size);
16 // Memory initialization on the host (CPU) and memory
      transfers
18 // Set the device for kernel execution
19 cudaSetDevice(0):
20 // Launch kernel on GPU O
```

```
21 vecAdd<<<gridDim, blockDim>>>(m_A0, m_B0);
22
23 // Set the device for kernel execution
24 cudaSetDevice(1);
25 // Launch kernel on GPU 1
26 vecAdd<<<gridDim, blockDim>>>(m_A1, m_B1);
27
28 // Free memory on GPU 0 and GPU 1
29 cudaFree(m_A0); cudaFree(m_B0);
30 cudaFree(m_A1); cudaFree(m_B1);
```

- Row 5. Setting the Active Device: it sets GPU 0 as the active device. Any subsequent CUDA operations, such as memory allocation or kernel launches, will be directed to GPU 0.
- Rows 7-8. Memory Allocation on GPU 0: memory is allocated on GPU 0 for two arrays, m\_A0 and m\_B0, each of size n \* sizeof(float).
- Row 11. Setting the Active Device to GPU 1: it changes the active device to GPU 1, directing subsequent operations to this device.
- Rows 13-14. Memory Allocation on GPU 1: similar to GPU 0, memory is allocated on GPU 1 for two arrays, m\_A1 and m\_B1.
- Row 16. Memory Initialization and Transfers: the comment mentions initializing memory on the host and transferring it to the devices, although the specific code for this is not shown. Typically, we would use cudaMemcpy() to transfer data from the host to the device.
- Rows 19-21. Kernel Execution: after setting GPU 0 as the active device, the vecAdd kernel is launched to perform vector addition on the arrays m\_A0 and m\_B0.
- Row 24-26. Kernel Execution on GPU 1: similarly, GPU 1 is set as the active device, and the vecAdd kernel is launched on m\_A1 and m\_B1.
- Row 29-30. Freeing Allocated Memory: after the computations are complete, the allocated memory on both GPUs is freed to avoid memory leaks.

#### Memory transfers between GPUs

In CUDA, there are several methods for transferring data between GPUs, each providing a different level of control and ease of use. The three main methods for transferring memory regions between GPUs are:

• Fully Explicit Transfer. In this method, we explicitly specify both the source and destination devices for the memory transfer. This approach gives us full control over the transfer process, but requires more detailed management of the transfer operation.

How it works:

- 1. Set the source device using cudaSetDevice().
- 2. Allocate memory and perform the necessary operations on the source device.
- 3. Set the destination device using cudaSetDevice().
- 4. Allocate memory on the destination device.
- 5. Use cudaMemcpyPeerAsync() to transfer data asynchronously between the two devices.

### **Example 9: Fully Explicit Transfer**

```
int srcDevice = 0;
int dstDevice = 1;
float *d_src, *d_dst;
size_t size = n * sizeof(float);
cudaSetDevice(srcDevice); // Set source device
cudaMalloc(&d_src, size); // Allocate memory on source
device
cudaSetDevice(dstDevice); // Set destination device
cudaMalloc(&d_dst, size); // Allocate memory on
destination device
// Transfer data from source to destination device
cudaMemcpyPeerAsync(d_dst, dstDevice, d_src, srcDevice,
size, stream);
```

cudaMemcpyPeerAsync() is a CUDA runtime API function used to perform asynchronous memory transfers between two devices. This function is particularly useful in multi-GPU systems, where it allows for non-blocking data transfers, enabling concurrent execution of other operations. Function Prototype:

Parameters:

- dst: pointer to the destination memory on the destination device.
- dstDevice: ID of the destination device.
- src: pointer to the source memory on the source device.
- srcDevice: ID of the source device.
- count: size of the memory to be transferred in bytes.
- stream: CUDA stream in which the transfer should be performed (optional). If no stream is specified, the default stream is used.
- Partially Explicit Transfer. This method uses unified addressing, which simplifies the transfer process by allowing us to use a unified address space. We only need to specify one of the devices explicitly, while the CUDA runtime handles the rest.

How it works:

1. Check if unified addressing is supported using:

```
cudaDeviceGetAttribute()
```

- 2. Allocate memory on one device (e.g., the source device).
- 3. Use cudaMemcpy() with the cudaMemcpyDefault flag to transfer data to the destination device.

```
Example 10: Fully Explicit Transfer
 int srcDevice = 0;
2 int dstDevice = 1;
3 float *d_src;
  size_t size = n * sizeof(float);
6 // Check if unified addressing is supported
7 int unifiedAddressing = 0;
8 cudaDeviceGetAttribute(&unifiedAddressing,
      cudaDevAttrUnifiedAddressing, srcDevice);
9
10 if (unifiedAddressing) {
      cudaSetDevice(srcDevice); // Set source device
      cudaMalloc(&d_src, size); // Allocate memory on
12
      source device
13
      // Transfer data to destination device using unified
14
       addressing
      cudaMemcpy(d_dst, d_src, size, cudaMemcpyDefault);
15
16 }
```

• Implicit Transfer. In this method, the CUDA driver automatically handles the transfer of memory between devices without explicit intervention from the programmer. This is the simplest method in terms of coding effort, as the driver takes care of the details.

How it works:

- The CUDA driver internally manages memory transfers between GPUs. This typically involves:
  - 1. Allocate memory (unified memory) on the source device using cudaMallocManaged(). This memory is accessible to all GPUs and the host, allowing CUDA to implicitly handle data transfers.
  - 2. Using unified memory or other mechanisms to handle the data transfer transparently. In other words, access the managed memory from any GPU by setting the active device and performing operations on it. CUDA internally manages the data transfer to ensure the memory is available on the device that needs it.

```
1 cudaSetDevice(0); // Set device 0 and use the memory
2 kernel<<<gridDim, blockDim>>>(d_managed);
3
4 cudaSetDevice(1); // Set device 1 and use the memory
5 kernel<<<gridDim, blockDim>>>(d_managed);
```

#### Example 11: Fully Explicit Transfer

```
1 float *d_managed;
2 size_t size = n * sizeof(float);
3 
4 // Allocate managed memory accessible by both devices
5 cudaMallocManaged(&d_managed, size);
6 
7 // Now d_managed can be accessed by any device as needed
8 cudaSetDevice(0); // Set device 0 and use the memory
9 kernel<<<gridDim, blockDim>>>(d_managed);
10 
11 cudaSetDevice(1); // Set device 1 and use the memory
12 kernel<<<gridDim, blockDim>>>(d_managed);
```

## **?** Communication Channels

There are two main types of communication channels connecting GPUs together:

- Standard PCIe 3.0 Link
  - **Speed**: 32 GB/s
  - Description: PCIe (Peripheral Component Interconnect Express) is a standard communication interface used to connect GPUs to the CPU and other peripherals. While widely used, PCIe 3.0 has limitations in terms of bandwidth, which can impact performance in data-intensive applications.
- NVLink
  - **Speed**: 300 GB/s (on the Tesla V100)
  - Description: NVLink is a high-speed interconnect technology developed by NVIDIA. It provides significantly higher bandwidth compared to PCIe, allowing for faster data transfer between GPUs. This can greatly improve performance in applications that require rapid communication and data exchange between multiple GPUs.

### 7.8.4 Batch Processing and Cooperative Patterns with OpenMP

In this section, we show how to implement batch processing and cooperative patterns using OpenMP.

## **E** Batch Processing OpenMP

The code snippet shows how to manage multiple GPU devices using OpenMP. The process includes:

```
1 #include <cuda_runtime.h>
2 #include <omp.h>
3 #include <vector>
  __global__ void kernel(float* data, int size) {
5
      // Kernel code here
6
7 }
8
9 int main() {
      int deviceCount;
10
       cudaGetDeviceCount(&deviceCount);
11
       std::vector<cudaStream_t> streams(deviceCount);
13
      // Initialize devices and streams in parallel
14
       #pragma omp parallel for num_threads(deviceCount)
15
       for(int dev = 0; dev < deviceCount; ++dev) {</pre>
16
           cudaSetDevice(dev);
17
           cudaStreamCreate(&streams[dev]);
18
19
           // Allocate memory and initialize data
      }
20
21
      // Launch kernels in parallel
22
23
       #pragma omp parallel for num_threads(deviceCount)
       for(int dev = 0; dev < deviceCount; ++dev) {</pre>
24
           cudaSetDevice(dev);
25
26
           kernel<<<gridDim, blockDim, 0, streams[dev]>>>(/* arguments
        */);
       3
27
28
       // Synchronize streams and clean up
29
       #pragma omp parallel for num_threads(deviceCount)
30
       for(int dev = 0; dev < deviceCount; ++dev) {</pre>
31
           cudaSetDevice(dev);
32
33
           cudaStreamSynchronize(streams[dev]);
           cudaStreamDestroy(streams[dev]);
34
35
           // Free allocated memory
      7
36
37
38
       return 0;
39 }
```

- 1. Rows 10-12. Getting the Device Count. This part of the code retrieves the number of CUDA-capable devices (GPUs) in the system using cudaGetDeviceCount(). It then creates a vector of CUDA streams, with each stream corresponding to a GPU.
- 2. Rows 15-20. Allocating Memory and Initializing Streams. This OpenMP parallel for loop iterates over the number of devices. For each device, it sets the current device using cudaSetDevice(), creates a CUDA

stream using cudaStreamCreate(), and then allocates memory and initializes it. By using num\_threads(deviceCount), the loop is parallelized to run on multiple threads, each handling a different GPU.

3. Rows 23-27. Launching Kernels. This OpenMP parallel for loop is similar to the previous one. It sets the current device and launches a kernel on each GPU using the corresponding CUDA stream. The function:

```
kernel«<gridDim, blockDim, streams[dev]»>(...)
```

Specifies the grid and block dimensions, along with the stream to be used for the kernel execution.

Here, the OpenMP code creates some tasks associated with CUDA streams.

## **E** Cooperative Patterns OpenMP

The following enumeration extends the concept of cooperative patterns using OpenMP. The code snippet shows how to synchronize CUDA streams using OpenMP:

1. Initialization of Streams:

```
1 std::vector<cudaStream_t> streams;
2 // Initialization of the streams on each device
3 // ...
```

2. Launching Kernels:

3. Synchronizing Streams:

```
1 #pragma omp for num_threads(streams.size())
2 for(auto& stream : streams)
3      cudaStreamSynchronize(stream);
```

4. Barrier Synchronization:

1 **#pragma** omp barrier

Instead of creating each task independently, OpenMP creates streams but waits for each to finish using a barrier.

#### 7.8.5 OpenMP for heterogeneous architectures

Recent versions of OpenMP support parallel execution on heterogeneous architectures, including:

- Host CPU: the main processor of the system.
- Attached Accelerators: additional hardware such as GPUs, FPGAs, DSPs, etc. Useful for handling specific tasks to increase performance.

In other words, **OpenMP allows the same code to run on both the host** (**CPU**) and the target device (accelerator). This means that different types of hardware can be used together to perform parallel computation more effectively.

To offload the execution of code to an accelerator device, such as a GPU, we use the target directive in OpenMP.

Doc. 📃

	$\mathbf{OpenMP}$ : pragma omp target	
1 #pragma omp target		

- Offloading Execution. The code within the region is executed on the accelerator device if one is present.
  - If no accelerator device is available, the code continues to run on the host (CPU).
  - If there is an if clause that evaluates to false, the code also continues execution on the host.
- Device Thread Execution. A thread on the target device (e.g., GPU) executes the code.
- Synchronous Execution. By default, the host thread blocks (waits) until the device thread has completed execution. To avoid this blocking, we can use the nowait clause.

#### map clause



The map clause in OpenMP is used to specify how variables are mapped from the host to the target device (such as a GPU) and back. This is crucial for ensuring that the data required by the target region is available on the target device and that any results are brought back to the host. It is used mainly to:

- Copying Variables to Device: the variables listed in the map clause are copied from the host to the target device.
- Copying Variables Back to Host: after the target region execution, the updated variables can be copied back to the host.

There are several types of *map* clauses that are used to give information to the compiler to avoid unnecessary data transfers:

- to clause.
  - Syntax: map(to: lst)
  - Description: copies variables (list) from the host to the target device.
  - Summary: Host  $\rightarrow$  Target Device
- from clause.
  - Syntax: map(from: lst)
  - Description: copies variables (list) from the target device to the host after the target region execution.
  - Summary: Host  $\leftarrow$  Target Device
- tofrom clause.
  - Syntax: map(tofrom: lst)
  - Description: copies variables from the host to the target device before the target region and back from the device to the host after execution.
  - Summary: Host  $\leftrightarrow$  Target Device

The default value is tofrom. Because these operations copy memory from one device to another, it is **important to limit their use**. For example, in the following code:

```
1 #pragma omp target map(a, b, c, d)
2 {
3     #pragma parallel for
4     for (i = 0; i < N; ++i) {
5          a[i] = b[i] * c + d;
6     }
7 } // End of target</pre>
```

At map-enter, there is a copy of the variables in device memory (expensive). There is a computation phase where the device memory uses the variables. Finally, at the map-exit, the device copies the variables to host memory (expensive).

## Example 12: SAXPY operation

This example demonstrates how to perform a SAXPY operation (Single-Precision  $A \cdot X$  Plus Y) using OpenMP. The SAXPY operation is a basic linear algebra operation, and here it is implemented to run on a target device like a GPU.

```
void saxpy() {
      double a, x[SZ], y[SZ];
double t = 0.0;
3
       double tb, te;
       tb = omp_get_wtime();
6
       #pragma omp target map(to:x[0:SZ]) \
                            map(tofrom:y[0:SZ])
       for (int i = 0; i < SZ; i++) {</pre>
           y[i] = a * x[i] + y[i];
       }
       te = omp_get_wtime();
       t = te - tb;
       printf("Time of kernel: %lf\n", t);
13
14 }
```

- Variables Initialization.
  - a, x[SZ] and y[SZ] are the main variables involved in the SAXPY operation.
  - -t, tb, and te are used for timing the operation.
- Timing the Operation.
  - tb = omp\_get\_wtime(); records the start time before the computation begins.
  - te = omp\_get\_wtime(); records the end time after the computation.
- OpenMP Target Directive.
  - map(to:x[0:SZ]): copies the array x from the host to the target device.
  - map(tofrom:y[0:SZ]): copies the array y to the target device and copies it back to the host after execution.
- SAXPY Operation. The for loop performs the SAXPY computation on the target device.
- Printing the Time. Finally, calculates the elapsed time for the kernel execution and prints the time.

#### 7.8.6 MPI-CUDA applications

## • What is MPI?

MPI stands for **Message Passing Interface**. It is a standardized and portable message-passing system designed to function on a wide variety of parallel computing architectures.

- **Process Communication**: MPI allows **multiple processes to communicate with each other by sending and receiving messages**. This is essential for coordinating tasks in parallel computing environments.
- **Distributed Computing**: MPI is commonly **used in distributed computing**, where processes run on different nodes (computers) in a network and need to work together on a common task.
- Parallel Execution: Each process in an MPI program runs independently and can perform computations on different parts of the data, leading to efficient parallel execution.
- Scalability: MPI can scale from a few processes on a single computer to thousands of processes on a supercomputer.

In the real-world scenario, it is common to use MPI and CUDA together to solve a computational problem, specifically focusing on wave propagation and heat transfer.

On the next page we see the Wave Propagation Stencil. It is a computational pattern to solve wave propagation problems, such as those found in seismic imaging or heat transfer simulations. It involves calculating the value of a point in a grid based on the values of its neighbors, typically using finite difference methods.

The calculation involves a weighted sum of values from neighboring points in the volume, which is typical in numerical simulations of physical processes such as heat transfer. The volume is divided into subdomains (D1, D2, D3, D4) to parallelize the computation. Domain decomposition is a technique that divides the computational domain (the volume) into smaller parts that can be processed simultaneously by different processors or GPUs. This approach increases computational efficiency by distributing the workload across multiple processing units.

#### • How is the workload shared between MPI and CUDA?

- MPI is used for communication between different processes handling different subdomains. It processes exchange boundary data to ensure continuity and accuracy of the simulation.
- CUDA is used for performing the calculations on each subdomain. Each GPU handles the computations for its assigned subdomain, performing the weighted sum calculations at each time step.
#### **X** Implementation

• Main program: initialize communication, execute process, finalize communication.

```
1 MPI_Init(&argc, &argv);
2 MPI_Comm_rank(MPI_COMM_WORLD, &pid);
  MPI_Comm_size(MPI_COMM_WORLD, &np);
3
5 if(np < 3) {
      if(0 == pid)
6
           printf("Needed 3 or more processes.\n");
      MPI_Abort(MPI_COMM_WORLD, 1);
8
9
      return 1;
10 }
11
12 if (pid < np - 1)
      compute_node(dimx, dimy, dimz / (np - 1), nreps);
13
14 else
      data_server(dimx, dimy, dimz, nreps);
15
16
17 MPI_Finalize();
```

The program starts by initializing MPI, getting the rank of the process (its ID), and the total number of processes.

- Initializes the MPI environment.
- Gets the rank (ID) of the calling process.
- Gets the number of processes.

So it checks if there are at least 3 processes. If not, it prints an error message and aborts. Furthermore, the program decides based on the process ID (pid) whether the process will be a compute node or a data server. Finally, the program closes the MPI environment.

#### • Server process: partition and distribute data.

```
1 /* Find number of MPI processes */
 2 /* Allocate input data */
3 /* Initialize input data */
4 /* Calculate number of points per compute process */
5 for (int process = 1; process <= last_node; process++) {</pre>
       MPI_Send(send_address, int_num_points, MPI_FLOAT, process,
 6
        DATA_DISTRIBUTE, MPI_COMM_WORLD);
       send_address += dimx * dimy * (dimz / num_comp_nodes);
 7
8 }
10 /* Wait for nodes to compute */
11 MPI_Barrier(MPI_COMM_WORLD);
12
13 /* Collect output data */
14 MPI_Status status;
15 for (int process = 0; process < num_comp_nodes; process++) {</pre>
       MPI_Recv(output + process * num_points / num_comp_nodes,
16
       num_points / num_comp_nodes, MPI_FLOAT, process,
       DATA_COLLECT, MPI_COMM_WORLD, &status);
17 }
```

The server process first initializes MPI and determines the total number of MPI processes and the number of compute nodes. It also allocates and initializes the input data and calculates the number of points per compute process.

After that, the server process uses a loop to send data to each compute node.

It calls MPI\_Barrier to synchronize all processes. This ensures that all compute nodes have completed their calculations before continuing.

Finally, the server process uses another loop to receive the computed results from each compute node.

• Compute process: receive data and offload computation to the GPU.

```
1 /* Part 1 */
3 /* Alloc host memory */
4 float *h_input = (float *)malloc(num_bytes);
5 /* Alloc device memory for input and output data */
6 float *d_input = NULL;
7 cudaMalloc((void **)&d_input, num_bytes);
_{\rm 8} /* Receive data and move it to device memory */
9 float *rcv_address = h_input + num_halo_points * (0 == pid);
10 MPI_Recv(rcv_address, num_points, MPI_FLOAT, server_process,
           MPI_ANY_TAG, MPI_COMM_WORLD, &status);
11
12 cudaMemcpy(d_input, h_input, num_bytes, cudaMemcpyHostToDevice
      );
13
14 /* Part 2 */
15 void launch_kernel(float *next, float *in, float *prev, float
      *velocity, int dimx, int dimy, int dimz)
16 {
17
      dim3 Gd, Bd, Vd;
18
      Vd.x = dimx; Vd.y = dimy; Vd.z = dimz;
19
20
      Bd.x = BLOCK_DIM_X; Bd.y = BLOCK_DIM_Y; Bd.z = BLOCK_DIM_Z
21
22
23
      Gd.x = (dimx + Bd.x - 1) / Bd.x;
      Gd.y = (dimy + Bd.y - 1) / Bd.y;
24
      Gd.z = (dimz + Bd.z - 1) / Bd.z;
25
26
      wave_propagation <<<Gd, Bd>>>(next, in, prev, velocity, Vd)
27
      ;
28 }
29
30 /* Part 3 */
31 MPI_Status status;
32 int left_neighbor = (pid > 0) ? (pid - 1) : MPI_PROC_NULL;
33 int right_neighbor = (pid < np - 2) ? (pid + 1) :</pre>
      MPI_PROC_NULL;
34
35 /* Upload stencil coefficients */
36 /* Calculate offsets */
37
38 MPI_Barrier( MPI_COMM_WORLD );
39 /* Compute boundary values needed by other nodes first */
40 launch_kernel(d_output + left_stage1_offset, d_input +
      left_stage1_offset, dimx, dimy, 1/2, stream0);
```

- 1. Part 1: Receiving Data and Allocating Memory. This part shows how the compute process receives data and prepares for computation on the GPU.
- 2. Part 2: Launching the Kernel. This part shows how to set up and launch a CUDA kernel for computation.
- 3. Part 3: Managing Neighbors and Synchronizing Streams. This part shows how to handle boundary conditions and synchronize computations.

## 8 Memory Consistency

## 8.1 Coherence vs Consistency

## **?** Why Memory Consistency?

Memory consistency models are fundamental to parallel computing because they define the rules that govern the visibility and ordering of memory operations across multiple threads. Unlike sequential computing, where the order of operations is straightforward, parallel computing introduces complexity due to concurrent execution. This concurrency can lead to race conditions, making it difficult to determine the "latest" value of a shared memory location.

#### **?** Why Memory Models are Fundamental to Parallel Computing

In an ideal scenario, loads (reads) should return the *most recent* value written to a memory location. However, defining and achieving this "most recent" value in a parallel environment is **complicated because multiple threads may be interacting with the same memory at the same time**. This is where memory consistency models play a critical role.

When we talk about memory, there are two fundamental concepts to explore: coherence and consistency.

• Memory Coherence ensures that all processors see a consistent view of a single memory location.

It defines the requirements for the observed behavior of reads and writes to the <u>same</u> memory location:

- All processors must agree on the order of reads/writes to a single memory location (X). This means that if one processor writes a value to a memory location, all other processors should eventually see that value.
- A timeline of operations involving the same memory location. It is possible to create a timeline such that the observations of all processors are consistent with that timeline. This ensures that each processor sees the most recent write to a memory location in the correct order.
- Memory Consistency extends this concept to the entire memory, ensuring an apparent ordering of operations, which dictates how memory operations performed by one thread become visible to other threads.

It defines the behavior of reads/writes to  $\underline{\text{different}}$  memory locations:

- Coherence guarantees eventual propagation. Coherence ensures that writes to a single memory location (X) will eventually propagate to other processors.
- Consistency deals with the timing of propagation. Consistency addresses when writes to one memory location (X) propagate

to other processors relative to reads and writes to other memory locations. This means that consistency ensures a predictable order for operations across multiple memory locations, considering their interactions.

## **Example 1: Chronology of Operations**

Imagine the following chronology of operations on a memory address (X):

t = 1. Write. PO  $\xrightarrow{5} X$ 

t = 2. Read. P1  $\xleftarrow{5}$  X

t = 3. Write. P2  $\xrightarrow{10}$  X

t = 4. Write. P2  $\xrightarrow{11}$  X

t = 5. Read. P1  $\xleftarrow{11}$  X

This example demonstrates how:

- Memory *coherence* ensures that all processors eventually agree on the order of operations for the same memory location.
- Memory *consistency* ensures a predictable interaction between operations on different memory locations.

#### **?** What happens if there is a cache system?

Modern parallel computing systems rely heavily on caches to improve performance. Therefore, **ensuring that all caches maintain a consistent view of memory** (cache coherence) **becomes critical to the proper operation of the system**. While memory coherence is about maintaining a consistent view of memory, cache coherence is about implementing this consistency in systems where each processor has its own local cache. So here we define again the concepts of consistency and coherence in the cache environment.

• Cache Coherence. This is a more specific implementation of memory coherence. In general, caches are used to store copies of frequently accessed data to speed up processing. However, when multiple processors modify their cached copies of the same memory location, inconsistencies can occur.

Therefore, the main goal is to ensure that the memory system in a parallel computer behaves as if the caches were not there. This is similar to how a memory system in a uni-processor system behaves as if the cache were not there.

In a system without caches, there would be no need for cache coherence. Cache coherence **ensures that all processors see a consistent view of memory, even though each processor may have a local cache**. This means that any changes made to a memory location by one processor will eventually be reflected in the caches of the other processors. • Memory Consistency (in the cache environment). Defines the allowed behavior of loads (reads) and stores (writes) to different addresses in a parallel system. This behavior should be specified whether or not caches are present. A memory consistency model specifies the rules for the order in which memory operations (loads and stores) become visible to other threads. It ensures that all processors in the system observe memory operations in a predictable and coherent manner, regardless of the presence of caches.

In other words, it is the same definition presented on the previous page, but we emphasize that model should also work with the cache.

## 8.2 Definition

After a brief discussion of the difference between coherence and consistency terms, and why it is important to understand these concepts, here we present a deeper view of memory consistency. This is because consistency deals with the broader and more complex issue of how all memory operations (across all memory locations) are ordered and observed in a parallel system. It is also necessary to understand the high-level rules that govern the interactions between processors and memory in a multiprocessor environment.

```
Definition 1: Memory Consistency
```

Memory Consistency models define how memory operations (loads and stores) performed by different processors are <u>ordered</u> and become visible to one another in a multiprocessor system.

# • Why the order decided by the memory consistency model is important

One main reason:

• **Performance**. In multiprocessor systems, memory operations can be reordered to optimize performance. Unfortunately, this **reordering can result in behavior that seems counterintuitive or unusual from the perspective of a programmer** who expects sequential execution. However, it allows optimizations such as overlapping memory accesses with computations and reducing memory access latency.

Most application programmers don't have to deal directly with the effects of memory reordering, because higher-level constructs and synchronization mechanisms handle them. However, understanding memory consistency is critical to writing correct and efficient parallel programs. Developers of system software, such as operating systems and compilers, must deal with these issues to ensure that their low-level code conforms to the hardware's memory consistency model and maintains the correct order of memory operations.

## **†**≦ Memory Operation Ordering

A program defines a sequence of loads and saves. There are **four types of memory operation sequences**:

1.  $W_X \to R_Y$ : Write to X must commit before a subsequent read from Y.

This means that if a write to memory location X occurs before a read from another memory location Y in the program order, the write must be complete and visible before the read.

2.  $R_X \to R_Y$ : Read from X must commit before a subsequent read from Y.

This order ensures that if a read from X occurs before a read from Y in the program, the first read must be completed before the second read occurs.

3.  $R_X \to W_Y$ : Read from X must commit before a subsequent write to Y.

This means that if a read from X occurs before a write to Y in the program order, the read must be completed before the write is performed.

4.  $W_X \to W_Y$ : Write to X must commit before a subsequent write to Y.

This ordering ensures that if a write to X happens before a write to Y in the program, the first write must be completed before the second write is performed.

The word "subsequent" means that each left operation must be completed and its result visible before the right operation can occur.

## 8.3 Sequential Consistency Model

## E Sequential Consistency Model

Sequential Consistency is a memory consistency model concept introduced by Lamport in 1976, which ensures that all operations in a multi-threaded system are executed in some sequential order, as if they were manipulating a single shared memory. This means that each thread's operations occur in program order, maintaining the illusion of a single, consistent timeline of memory operations. In other words, a sequentially consistent memory system maintains all four orders of memory operations (the order of operations seen in the enumerated list on page 224).

Sequential Consistency is the **strongest model**, because it requires all memory operations to appear as if they are executed in a strict sequential order. The degree of reordering of memory operations determines the strength of a model's weakness.

#### E Relaxing Memory Method

**Relaxed Memory** method allows certain memory operation orders to be violated to improve performance. It primarily aim to improve performance by hiding memory latency. By allowing some flexibility in the order of memory operations, these models enable systems to execute instructions more efficiently. So operations like "Write X then Read Y" can be done out of order if they are independent.

#### A Problems with Sequential Consistency Model

There are **four main problems** associated with the sequential consistency model in parallel computing systems:

• Performance Overhead. Requires all operations to appear in a strict sequential order.

Can introduce significant performance overhead due to the necessity of maintaining order, especially when memory writes take a long time (hundreds of cycles).

• Instruction Dependency. Requires waiting for earlier instructions to finish, even if they don't conflict.

Limits the ability of the system to execute independent instructions in parallel.

• Latency Issues. Memory operations, especially writes, can have high latency.

Delays in writing data mean that processors must wait before executing subsequent instructions, leading to inefficiencies.

• Limited Parallelism. Limits the potential for parallel execution of independent instructions.

Reduces the system's ability to effectively use parallelism, which affects overall performance.

## Sequential Consistency Model

The Write Buffer method is a technique used in multiprocessor systems to enhance performance and reduce latency. It involves temporarily storing write operations in a buffer before propagating them to the main memory. This allows processors to continue executing subsequent instructions without waiting for the write to complete.

The write buffer method helps in maintaining sequential consistency while **reducing the performance overhead** and **latency issues**. By buffering writes and allowing processors to read from their own write buffers, this method enhances the efficiency and parallelism of the system.

Note: The write buffer is **only a technique**. The model that will use this feature will be present in the following pages.

### **?** How does Write Buffer work?

- Structure. Each processor has its own write buffer.
- **Buffered Writes**. When a processor writes to a memory location, the **write is placed in the processor's write buffer** instead of being immediately propagated to the shared memory.
- **Read from Buffer**. When the processor reads a memory location, it first checks its write buffer before accessing the shared memory.

```
Example 2: Write Buffer method
```

Initial Setup

Processor 0 and Processor 1 both interact with shared memory. They initialize  $A\ =\ 0$  and  $B\ =\ 0.$ 

Instructions

• Processor 0 executes:

```
1. A = 1
```

```
2. r1 = B
```

• Processor 1 executes:

1. B = 1

2. r2 = A

## Question

Can r1 and r2 both be 0 after executing these instructions?

## Answer

• Sequential Consistency. Under sequential consistency, all operations must appear to be executed in a strict sequential order. r1cannot be 0 if Processor 1 has written B = 1. Similarly, r2 cannot be 0 if Processor 0 has written A = 1.

Therefore, no, r1 and r2 cannot both be 0, because the write from one processor should be visible to the read from the other processor.

- With Write Buffers. Each processor temporarily stores its write operations in its own write buffer before committing them to main memory.
  - Processor 0:
    - 1. Writes A = 1 to its write buffer.
    - 2. Reads B from the main memory (which is still 0 because Processor 1's write is buffered).
  - Processor 1:
    - 1. Writes B = 1 to its write buffer.
    - 2. Reads A from the main memory (which is still 0 because Processor 0's write is buffered).

The result is that r1 and r2 can both be 0 because each processor reads from main memory before the other's buffered write is committed. So yes, with the buffered write technique, r1 and r2 can both be 0.

## Summary

This example shows how write buffers allow processors to perform and cache writes independently, resulting in scenarios where reads may not immediately reflect recent writes from other processors. This can optimize performance by reducing write latency, but introduces complexity in ensuring memory consistency.

## 22 Performance: Sequential Consistency vs. Write Buffer

The Figure 38 shows three different benchmarks that were run to compare the Sequential Consistency and Write Buffer models. The benchmarks executed are: MP3D (Matterport 3D), LU (Master Lu), PTHOR.



Figure 38: Write Buffer Performance.

- MP3D:
  - Base (Sequential Consistency): 100 (normalized execution time)
  - W-R (Write Buffer): 71 (normalized execution time)
  - Performance Improvement: 29% reduction in execution time.
- LU:
  - Base (Sequential Consistency): 100 (normalized execution time)
  - W-R (Write Buffer): 95 (normalized execution time)
  - Performance Improvement: 5% reduction in execution time.
- PTHOR:
  - Base (Sequential Consistency): 100 (normalized execution time)
  - W-R (Write Buffer): 80 (normalized execution time)
  - Performance Improvement: 20% reduction in execution time.

These results indicate that the write buffer method can significantly improve performance in multiprocessor systems, especially in scenarios where write latency is a critical factor.

## 8.4 Memory Models with Relaxed Ordering

The following models are **grouped based on the types of memory opera-tion reordering** they allow. Each model applies the relaxing memory models, so they allow certain memory operation orders to be violated to improve performance.

Before introducing each memory model, we will talk about problems and possible solutions for memory models with relaxed order.

## A Problems with Memory Reordering

Reordering of memory operations can lead to **inconsistencies** and **unpredictable behavior** in multiprocessor systems.

## Solutions: Synchronization Primitives

✓ Memory Fence Instructions (Barriers): Prevent reorderings by ensuring that all memory operations before the fence complete before any new operations begin.

Fence instructions can be costly in terms of performance but are essential for maintaining order and consistency.

- Read-Modify-Write: Ensures atomic read and write operations to a memory location.
- ✓ Compare-and-Swap: Atomically compares a memory location's value and swaps it if it matches a specified value.
- ✓ Transactional Memory: Allows a group of memory operations to be executed atomically.

## 8.4.1 Allowing Reads to Move Ahead of Writes

## **?** Which memory operation is relaxed?

Given the four memory operation sequences (see detailed explanation on page 224), the relaxed operations are marked as cancel:

# ✓ *Relaxed* $W_X \to R_Y$ : Write to X must commit before a subsequent read from Y.

This means that if a write to memory location X occurs before a read from another memory location Y in the program order, the write must be complete and visible before the read.

- $X R_X \to R_Y$ : Read from X must commit before a subsequent read from Y.
- **×**  $R_X$  →  $W_Y$ : Read from X must commit before a subsequent write to Y.
- $X W_X \to W_Y$ : Write to X must commit before a subsequent write to Y.



### **Models**

• Total Store Ordering (TSO)

## **X** How does it work?

It allows a processor to read a variable (e.g., **B**) before its write to another variable (e.g., **A**) is visible to all processors  $(W_{\mathbf{A}} \rightarrow \mathcal{R}_{\mathbf{B}})$ .

This enables the processor to hide the latency of write operations by **allowing reads to proceed independently**.

#### **A** Implications

Other processors cannot see the new value of A (the value written to register A) until the write to A is observed by all processors.

Only  $W_{A} \rightarrow R_{B}$  order is relaxed, while  $W_{A} \rightarrow W_{B}$  constraints still exist, meaning writes by the same thread occur in program order. Other processors see these writes in the correct order, but there might be a delay before the writes are visible due to buffering.

• Processor Consistency (PC)

## **X** How does it work?

Similar to TSO, but with slightly more flexibility.

Any processor can read the new value of **A before the write is observed** by all processors, allowing reads to be even more independent of writes.

#### **A** Implications

Like TSO, only  $W_{\mathtt{A}} \rightarrow R_{\mathtt{B}}$  order is relaxed, and  $W_{\mathtt{A}} \rightarrow W_{\mathtt{B}}$  constraints remain, ensuring that writes by the same thread occur in program order.

## Main differences between TSO and PC

- 1. Read Flexibility
  - **TSO**: Reads by a processor can move ahead of its own writes.
  - **PC**: Reads by any processor can observe new values of writes *before they are globally visible*, allowing even more flexibility.

## 2. Write Order

- Both Models: Maintain the order of writes within the same processor, ensuring that  $W_{\mathtt{A}} \rightarrow W_{\mathtt{B}}$  order is preserved.
- 3. Performance vs. Complexity
  - **TSO**: Strikes a *balance between performance and simplicity* by allowing limited reordering of reads and writes.
  - **PC**: Offers *greater flexibility in read operations*, potentially improving performance but at the *cost of slightly increased complexity*.

## 8.4.2 Allowing writes to be reordered

## • Which memory operation is relaxed?

Given the four memory operation sequences (see detailed explanation on page 224), the relaxed operations are marked as cancel:

✓ *Relaxed*  $W_X \to R_Y$ : Write to X must commit before a subsequent read from Y.

This means that if a write to memory location X occurs before a read from another memory location Y in the program order, the write must be complete and visible before the read.

- $X R_X \to R_Y$ : Read from X must commit before a subsequent read from Y.
- $X R_X \to W_Y$ : Read from X must commit before a subsequent write to Y.
- ✓ *Relaxed*  $W_X \to W_Y$ : Write to X must commit before a subsequent write to Y.

This ordering ensures that if a write to X happens before a write to Y in the program, the first write must be completed before the second write is performed.

## **Models**

• Partial Store Ordering (PSO)

## **X** How does it work?

PSO allows more **aggressive reordering of write operations** compared to TSO (page 231) and PC (page 231).

#### **A** Implications

_	Thread 1 on Processor 1 (P1)
1 2	A = 1; flag = 1;
_	Thread 2 on Processor 2 (P2)

1 while (flag == 0); 2 print A;

P2 may observe the change to flag before the change to A. This shows that PSO allows writes to A and flag to be reordered, improving write performance but potentially complicating program reasoning.

## **O** Benefits

- $-W_X \rightarrow W_Y$ . Write Buffering: Processors can reorder write operations in a write buffer. For example, one write might be a cache miss while another is a cache hit, and reordering them can optimize performance.
- $-R_X \rightarrow R_Y, R_X \rightarrow W_Y$ . Instruction Reordering: Processors can reorder independent read and write instructions within the instruction stream, leveraging out-of-order execution to maximize efficiency.

These reorderings and optimizations are particularly **effective in single instruction streams**, where dependencies between instructions are well understood and managed.

#### 8.4.3 Allowing all reorderings

## **?** Which memory operation is relaxed?

Given the four memory operation sequences (see detailed explanation on page 224), the relaxed operations are marked as cancel:

# ✓ *Relaxed* $W_X \to R_Y$ : Write to X must commit before a subsequent read from Y.

This means that if a write to memory location X occurs before a read from another memory location Y in the program order, the write must be complete and visible before the read.

✓ *Relaxed*  $R_X \to R_Y$ : Read from X must commit before a subsequent read from Y.

This order ensures that if a read from X occurs before a read from Y in the program, the first read must be completed before the second read occurs.

✓ *Relaxed*  $R_X \to W_Y$ : Read from X must commit before a subsequent write to Y.

This means that if a read from X occurs before a write to Y in the program order, the read must be completed before the write is performed.

✓ *Relaxed*  $W_X \to W_Y$ : Write to X must commit before a subsequent write to Y.

This ordering ensures that if a write to X happens before a write to Y in the program, the first write must be completed before the second write is performed.

## **Models**

• Weak Ordering (WO)

## X How does it work?

Operations are divided into critical and non-critical sections. Reordering is allowed outside of critical sections to maximize performance.

**Example**: Can reorder any non-critical operations to enhance efficiency, executing them independently.

• Release Consistency (RC)

## **X** How does it work?

Divides operations into acquire and release categories, allowing extensive reordering within these categories.

**Example**: Reorders operations within acquire or release phases, enabling significant performance gains.

In these models, there are **no strict guarantees about the order of oper-ations on data**. Essentially, everything can be reordered.

## **?** Why allow all reorders?

By overlapping multiple reads and writes, the **system can execute reads as** early as possible and delay writes as late as possible, effectively hiding memory latency and increasing performance.

## 8.5 Languages Need Memory Models Too

Memory models are critical not only for hardware systems, but also for programming languages. They provide a framework that defines how memory operations (reads and writes) can be ordered and observed by multiple threads. This chapter discusses the importance of memory models in programming languages and how they help maintain consistency and predictability in multi-threaded programs.

## X Compiler Optimizations

• **Invisible Optimizations**. Compilers can optimize code in ways that are not directly visible to the programmer, such as reordering instructions to enhance performance.

	Exa	ample 3: optimization <i>not</i> visible to programmer
	Cod	le written by the programmer:
1	X =	0
2	for	i = 0 to 100:
3		X = 1
4		print X
	Cod	le optimized by the compiler:
1	Х =	1
2	for	i = 0 to 100:
3		print X
	_	

These optimizations can lead to unexpected behaviors in multithreaded programs if not properly managed.

• Visible Optimizations. When optimizations are visible to the programmer, it becomes essential to understand how these changes affect the execution order and consistency of memory operations.

Example 4: optimization is visible to programmer
Code written by the programmer:
– Thread 1
$1 \overline{\mathbf{X}} = 0$
2 for i = 0 to 100:
3   X = 1
4 print X
- Thread 2
1 X = 0
<ul> <li>Expected result: 11111111</li> <li>Besult obtained: 111110111</li> </ul>

```
Code optimized by the compiler:

- Thread 1

\begin{bmatrix} x &= 1 \\ for & i &= 0 & to & 100: \\ print & x \end{bmatrix}

- Thread 2

\begin{bmatrix} x &= 0 \\ x &= 0 \end{bmatrix}

- Expected result: 11111111...

- Result obtained: 111110000...
```

## Need for Language-Level Memory Models

- Contract to Programmers. Memory models provide a contract to programmers, ensuring that memory operations will be reordered by the compiler in a way that maintains consistency. For example, there should be no reordering of shared memory operations that could lead to race conditions.
- Guarantees. Modern languages like C11, C++11, and Java 5 guarantee sequential consistency for data-race-free programs, meaning that the program's behavior will be predictable if there are no data races.

## **A** Importance of Synchronization

- Data Races. Without proper synchronization, data races can occur, leading to non-deterministic and buggy behavior. Programs with data races do not have any guarantees and can produce unpredictable results.
- Synchronization Libraries. Using synchronization primitives like locks, barriers, and memory fences ensures that memory operations are executed in the correct order, preventing data races and maintaining program correctness.

## E Summary

Memory models at the language level are essential for maintaining consistency and predictability in multi-threaded programs. They help manage compiler optimizations and provide a framework for programmers to ensure that their code behaves correctly, even when memory operations are reordered.

## 8.6 Implementing Locks

## 8.6.1 Introduction

Locks are essential in concurrent programming for managing access to shared resources and preventing data races. A common mistake in implementing locks is using a simple Load-Test-Store lock sequence, which can lead to severe issues such as data races due to its non-atomic nature.

#### Simple but Incorrect Lock Implementation: Load-Test-Store lock

The idea behind the **Load-Test-Store lock** is to **check if the lock is available** (i.e., not held by any other processor) **and then acquire it by setting it**. This process involves loading the current value of the lock, checking its state, and storing a new value if it's free. Here's the pseudo-code for the implementation:

```
lock:
1
      // Load the value at address into register RO
2
      ld RO, mem[addr]
      // Compare the value in RO to O
      cmp R0, #0
      // If RO is not zero, jump back to 'lock' (retry)
9
      bnz lock
      // Store 1 at the address to indicate the lock is acquired
      st mem[addr], #1
12
13
14 unlock:
      // Store 0 at the address to release the lock
      st
         mem[addr], #0
16
```

In this implementation, a processor repeatedly loads and checks a memory address, acquiring the lock by storing a value to indicate it is locked. However, **this sequence is not atomic**, leading to a **potential data race**:

- Processor 0 (P0) attempts to acquire the lock:
  - ld RO, mem[addr]: PO loads the value from memory address addr into register RO. Suppose the value is O (lock is *free*).
  - cmp R0, #0: P0 compares R0 with 0. Since R0 is 0, the comparison is true.
  - st mem[addr], #1: P0 stores 1 at mem[addr], indicating it has acquired the lock.
- Processor 1 (P1) attempts to acquire the lock simultaneously:
  - ld R1, mem[addr]: P1 loads the value from memory address addr into register R1. Suppose the value is still 0 (before P0 updates the lock).
  - cmp R1, #0: P1 compares R1 with 0. Since R1 is 0, the comparison is true.

- st mem[addr], #1: P1 stores 1 at mem[addr], indicating it has acquired the lock.

Both P0 and P1 believe they have acquired the lock because they both observed the lock as free (0) and updated it to 1. This leads to a **data race where two** processors think they have the lock, causing inconsistent states and potential conflicts in accessing the critical section.

#### • Why does Load-Test-Store suffer from Data Race?

- Non-Atomic Operations: The sequence of load, compare, and store operations are not atomic. During this sequence, *other processors can interrupt and perform their own operations*, leading to race conditions.
- Lack of Synchronization: There is no mechanism to ensure that the load-test-store sequence is executed as a single, uninterruptible operation, which is necessary to prevent data races.

#### Solution: Advanced Locking Techniques

To address these issues, more sophisticated lock implementations are necessary. The following sections will explore *Test-and-Set Based Lock* (page 240) and *Test-and-Test-and-Set Lock* (page 244), which provide reliable and efficient synchronization mechanisms to prevent data races and ensure proper access control.

#### 8.6.2 Test-and-Set based lock

The **Test-and-Set instruction** is a fundamental **atomic operation used for synchronization** in multiprocessor systems. It **checks the value of a lock variable and sets it to a new value in one uninterruptible action**. The operation ensures that no other processors can modify the lock variable simultaneously, preventing race conditions.

#### How does it work?

It performs two actions in one uninterruptible step:

- 1. It loads the value from a memory address into a register;
- 2. Then sets the memory address to a specified value (usually indicating the lock is acquired).

```
      1 ts R0, mem[addr]
      // load mem[addr] into R0

      2
      // if mem[addr] is 0, set mem[addr] to 1
```

## Lock Implementation

To implement a lock using the test-and-set instruction, we must **repeatedly attempt to acquire the lock until it is free**.

```
1 lock:
2 ts R0, mem[addr] // Attempt to acquire the lock
3 bnz R0, lock // If the lock was not free (R0 \neq 0),
4 // retry
```

- ts R0, mem[addr]: Atomically loads the value at mem[addr] into register R0 and sets mem[addr] to 1 if it was 0.
- bnz RO, lock: If RO is non-zero (meaning the lock was already held), it branches back to the start and retries.

#### **Unlock Implementation**

To release the lock, simply we set the lock variable back to 0.

```
1 unlock:
2 st mem[addr], #0 // Release the lock by storing 0
```

• st mem[addr], #0: Stores 0 at the memory address addr, indicating the lock is now free.

## ▲ Coherence Protocol

Using test-and-set based locking is fundamental to **maintaining consistency across multiple processor caches by ensuring that all processors have the same view of the lock variable**. So it involves invalidating and updating cache lines across processors as the lock state changes.

Processor	1	Processor 2	Processor 3
BusRdX	T&S	Invalidate line	Invalidate line
Update line in ca	che (set to 1)		
Invalidate line		BusRdX	
		Attempt to update (t&s fails)	
		Invalidate line	BusRdX
l			Attempt to update (t&s fails)
[P1 is holdir	nglock]	BusRdX T&S	Invalidate line
		Attempt to update (t&s fails)	
		Invalidate line	BusRdX T&S
			Attempt to update (t&s fails)
BusRdX			
Update line in ca	che (set to 0)		Invalidate line
Invalidate line		BusRdX T&S	
		Update line in cache (set to 1)	
= thread has lock			

• Processor 1 (P1):

- Acquiring Lock:

- \* BusRdX Request: P1 sends a Bus Read Exclusive (BusRdX) request to acquire the lock.
- \* Cache Update: P1 sets the lock value to 1 in its cache, indicating the lock is held.
- \* **Invalidation**: Other processors' caches are invalidated for the lock variable.

- Releasing Lock:

- \* **BusRdX Request:** P1 sends another BusRdX request to release the lock.
- \* Cache Update: P1 sets the lock value to 0 in its cache, indicating the lock is free.
- \* **Invalidation**: Other processors' caches are invalidated for the lock variable.

- Processor 2 (P2) and Processor 3 (P3):
  - Attempting to Acquire Lock:
    - \* **Invalidation**: Their cache lines for the lock are initially invalidated.
    - \* **BusRdX Request**: Both processors send **BusRdX** requests to acquire the lock.
    - \* **Retry Loop**: If the lock is not free, they continuously retry, causing repeated BusRdX requests.

#### **?** Implications of Coherence Traffic

• Contention. High contention occurs when multiple processors compete for the same lock at the same time.

Each processor continuously attempts to execute the test-and-set instruction, resulting in repeated BusRdX requests. This competition generates significant traffic on the memory bus and forces processors to repeatedly invalidate each other's cache lines for the lock variable.

The result is a high level of contention that can **cause delays and inef**ficiencies as processors wait for the lock to become available.

• Performance Impact. The frequent BusRdX requests and resulting cache invalidations can significantly degrade system performance, especially as the number of processors increases.

Each BusRdX request incurs a cost in terms of memory bus usage and latency. As more processors contend for the lock, the cumulative effect of these requests becomes more pronounced, leading to:

- ✗ Increased Latency: The time taken for processors to acquire and release the lock increases, slowing down the overall execution of the program.
- ✗ Memory Bus Saturation: The memory bus becomes saturated with coherence traffic, reducing the available bandwidth for other memory operations.
- ✗ Inefficiency: Processors spend more time waiting and retrying to acquire the lock, leading to inefficient use of processing resources.

## **2** Test-and-Set Performance

The following graph plots the performance of the test-and-set lock in terms of time (in microseconds) versus the number of processors. It specifically measures the time taken to acquire and release the lock as the number of processors increases.



- X-Axis: Number of processors (ranging from 0 to 16).
- Y-Axis: Time in microseconds (ranging from 0 to 20).
- Initial Increase: As the number of processors increases from 1 to 4, the time taken to acquire and release the lock increases significantly.
- Fluctuations: There is a noticeable dip in time around 7 processors, followed by fluctuations as the number of processors continues to increase.
- Overall Trend: Despite the fluctuations, the general trend shows an upward increase in time with more processors, indicating higher contention.

The performance of the test-and-set lock shows that with an **increasing num**ber of processors, the time to acquire and release the lock increases due to contention and coherence traffic.

#### 8.6.3 Test-and-Test-and-Set lock

The **Test-and-Test-and-Set lock** mechanism improves upon the simple Testand-Set lock by **reducing interconnect traffic and contention**. It **combines an initial test phase with a subsequent atomic Test-and-Set operation**.

## X Implementation

```
void Lock(int* lock) {
2
       while (1) {
           // Spin-wait until the lock appears free
3
           // (assume *lock is NOT register allocated)
4
           while (*lock != 0);
5
6
           // Try to acquire the lock atomically
7
           if (test_and_set(*lock) == 0)
8
               return;
9
      }
10
11 }
12
13 void Unlock(int* lock) {
       *lock = 0; // Release the lock
14
15 }
```

- Initial Spin Phase:
  - Purpose: Processors continuously check the value of the lock variable (\*lock) in a loop until it becomes 0 (free). This spin-wait phase helps reduce contention on the interconnect by delaying the atomic test-and-set operation until the lock appears free.
  - Implementation: while (\*lock != 0); causes the processor to repeatedly check the lock value without sending any bus requests.
- Atomic Test-and-Set Operation:
  - Purpose: Once the lock appears free, the processor attempts to acquire it using the atomic test\_and\_set instruction. This operation is performed in one uninterruptible step to ensure that only one processor can acquire the lock at a time.
  - Implementation: The line of code if (test\_and\_set(\*lock) ==
    0) return; checks if the lock was successfully acquired (i.e., the function test\_and\_set returns 0) and exits the loop if it was.
- Unlock Operation:
  - Purpose: To release the lock, the processor sets the lock variable back to 0, indicating that the lock is free.
  - Implementation: \*lock = 0; simply sets the lock value to 0.

## **A** Coherence Traffic



- Processor 1 (P1)
  - $\mathbf{BusRdX}: \mathtt{P1}$  sends a Bus Read Exclusive ( $\mathtt{BusRdX})$  request to acquire the lock.
  - Update Line in Cache: P1 updates its cache line, setting the lock value to 1, indicating that it has acquired the lock.
  - [P1 is holding lock...]: P1 holds the lock and performs its critical section work.
  - BusRdX (Release): P1 sends another BusRdX request when it releases the lock.
  - Update Line in Cache (Release): P1 updates its cache line, setting the lock value to 0, indicating that the lock is now free.
  - Invalidate Line: Other processors' caches are invalidated for the lock variable.
- Processor 2 (P2)
  - Invalidate Line: Initially, P2's cache line for the lock is invalidated.
  - **BusRd**: P2 reads the lock value.
  - [Many Reads from Local Cache]: P2 spins, repeatedly reading the lock value from its local cache until it becomes free.
  - Invalidate Line: When the lock is acquired/released, P2's cache line is invalidated again.
  - $\mathbf{BusRd}:$  P2 reads the updated lock value.

- Processor 3 (P3)
  - Invalidate Line: Initially, P3's cache line for the lock is invalidated.
  - **BusRd**: P3 reads the lock value.
  - [Many Reads from Local Cache]: P3 spins, repeatedly reading the lock value from its local cache until it becomes free.
  - Invalidate Line: When the lock is acquired/released, P3's cache line is invalidated again.
  - **BusRd**: P3 reads the updated lock value.
  - BusRdX: P3 sends a BusRdX request to acquire the lock.
  - Update Line in Cache: P3 updates its cache line, setting the lock value to 1, indicating that it has acquired the lock.
  - Invalidate Line: Other processors' caches are invalidated for the lock variable.
  - BusRdX (Failed Attempt): If P3's test-and-set operation fails (because another processor acquires the lock), it continues to spin and retry.

#### Comparison with Test-and-Set

- Slightly Higher Latency than Test-and-Set in Uncontended Cases
  - The test-and-test-and-set lock involves an initial test phase before the atomic test-and-set operation. This extra step can introduce slightly higher latency when there is no contention, as processors spend additional time in the spin-wait phase.
- Generates Much Less Interconnect Traffic
  - One Invalidation per Waiting Processor per Lock Release: Each waiting processor experiences one cache invalidation per lock release, resulting in O(P) invalidations, where P is the number of processors.
  - Comparison to Test-and-Set Lock: The test-and-set lock generates one invalidation per waiting processor per test, leading to significantly higher interconnect traffic.
  - $O(P^2)$  Interconnect Traffic: If all processors have the lock cached, the interconnect traffic can be quadratic  $(O(P^2))$ . However, this is still less than the traffic generated by the simple test-and-set lock.
- More Scalable (Due to Less Traffic):
  - Scalability: The reduced interconnect traffic makes the test-and-test-and-set lock more scalable. It can handle an increasing number of processors more efficiently than the simple test-and-set lock.

- Impact: As the number of processors grows, the performance impact of the test-and-test-and-set lock remains more manageable, making it suitable for larger multiprocessor systems.
- Storage Cost Unchanged (One Integer):
  - Storage Requirements: The storage cost of the test-and-test-andset lock remains the same as the simple test-and-set lock, requiring only one integer to represent the lock.
- Still No Provisions for Fairness:
  - Fairness<sup>12</sup>: The test-and-test-and-set lock does not include mechanisms to ensure fairness. This means that some processors may experience longer waiting times to acquire the lock, leading to potential starvation.
  - Implications: While the lock reduces interconnect traffic and improves scalability, the lack of fairness can still be a significant drawback in systems where equitable access to resources is important.

The test-and-test-and-set locking mechanism offers several advantages over the simple test-and-set lock, including reduced interconnect traffic and improved scalability. However, it introduces slightly higher latency in uncontended cases and does not address fairness issues. Overall, it is a more efficient and scalable locking solution for multiprocessor systems, though not without its limitations.

 $<sup>^{12}</sup>$ Fairness in the context of lock mechanisms refers to the equitable distribution of opportunities for multiple processors or threads to acquire the lock. A fair locking mechanism ensures that all processors have a roughly equal chance of acquiring the lock, preventing any single processor from being starved of access to the critical section.

## References

- Gene M Amdahl. Validity of the single processor approach to achieving large scale computing capabilities, reprinted from the afips conference proceedings, vol. 30 (atlantic city, nj, apr. 18–20), afips press, reston, va., 1967, pp. 483–485, when dr. amdahl was at international business machines corporation, sunnyvale, california. *IEEE Solid-State Circuits Society Newslet*ter, 12(3):19–20, 2007.
- [2] Guy E. Blelloch, Laxman Dhulipala and Yihan Sun. Introduction to parallel algorithms. https://www.cs.cmu.edu/~guyb/paralg/paralg/ parallel.pdf, 2024. [Accessed 22-10-2024].
- [3] Ferrandi Fabrizio. Parallel computing. Slides from the HPC-E master's degree course on Politecnico di Milano, 2024.
- [4] John L Gustafson. Reevaluating Amdahl's law. Communications of the ACM, 31(5):532–533, 1988.
- [5] Johnston Hans. OpenMP by Example. https://people.math.umass. edu/~johnston/PHI\_WG\_2014/OpenMPSlides\_tamu\_sc.pdf, 2024. [Accessed 23-10-2024].
- [6] Vipin Kumar, Ananth Grama, Anshul Gupta, and George Karypis. Introduction to parallel computing, volume 110. Benjamin/Cummings Redwood City, CA, 1994.
- [7] Erik Lindholm, John Nickolls, Stuart Oberman, and John Montrym. Nvidia tesla: A unified graphics and computing architecture. *IEEE micro*, 28(2):39–55, 2008.
- [8] M. McCool, J. Reinders, and A. Robison. Structured Parallel Programming: Patterns for Efficient Computation. ITPro collection. Elsevier Science, 2012.
- [9] Microsoft. The critical directive. https://learn.microsoft. com/en-us/cpp/parallel/openmp/a-examples?view=msvc-170# a5-the-critical-directive, 2024. [Accessed 29-10-2024].
- [10] M. Nemirovsky and D. Tullsen. *Multithreading Architecture*. Synthesis Lectures on Computer Architecture. Springer International Publishing, 2022.
- [11] University of Michigan, EECS Department, Prof. Ronald Dreslinski. Lecture 5, Synchronization I - EECS 570, 2024. [Accessed 24-11-2024].
- [12] Wikipedia. Cache (computing) Wikipedia. https://en.wikipedia.org/ wiki/Cache\_(computing). [Accessed 20-10-2024].

## Index

A Amdahl's Law Arbitrary Concurrent Write Asynchronous memory prefetching	$20 \\ 7 \\ 192$
restrictions as memory protocolling	10-
В	
Bandwidth and Latency	127
Barrier Object	53
Batch Processing	199
Block Multithreading	30
С	
Cache	28
Cache Coherence	221
Cache Hit	28
Cache Miss	28
Coarse-Grain Multithreading	30
Common Concurrent Write	7
Composition Rules	42
Compute Unified Device Architecture (CUDA)	103
Concurrent Read (CR)	7
Concurrent tasks in parallel algorithms	41
Concurrent Write (CW)	7
Cooperative Patterns	200
Corner Turning	160
CUDA	162
CUDA Blocks	103
CUDA Device	105
CUDA execution model	178
CUDA Grids	104
CUDA Host	105
CUDA Interleaved Mapping	114
CUDA kernel	104
CUDA profiling	172
CUDA Streams	193
CUDA thread hierarchy	182
CUDA Threads	103
Cyclical Process for Accelerating Applications with NVIDIA GPU	168
D	
Data Locality and Caching	127
Data Race	48
Data-Parallel model	37
Device Global Memory	108
Directed Acyclic Graph (DAG)	41
DRAM (Dynamic Random Access Memory) burst	153
E	
Error Check Mutex (PTHREAD_MUTEX_ERRORCHECK)	54

Exclusive Read (ER)	7
Exclusive Write (EW)	7
Execution Context	123
P	
	0.47
Fairness Eine Crein Multithuseding (ECMT)	247
Flue-Grain Multilineading (FGM1)	30 47
Flynn S taxonomy	41
G	
General-Purpose computing on Graphics Processing Units (GPG	PU) 100, 102
Global memory access	127
GPU compute mode	101
Gustafson's Law	21
ч	
II Higher Order function	37
inglier-Order function	51
Ι	
Implicit SPMD Program Compiler (ISPC)	31
Instruction-Level Parallelism (ILP)	24
Interleaved execution	118
Interleaved Multithreading	30
т	
L Load Test Store lock	238
Loon Peeling	238 97
Loop Tail	97
M	
Machine Model	6
Matrix Multiply (MM) algorithm	16
Matrix-Vector Multiply (MVM) algorithm	10
Memory Access Latency	20
Memory Bandwidth	27 155
Memory Coherence	220
Memory Consistency	220, 222, 223
Memory hierarchy	127
Message Passing model	36
MPI (Message Passing Interface)	198
Multi-Core Processor (MCP)	25
Multithreaded Processor	28
N	
IN Normal Mutor (DTUDEAD MITTEY NODMAL)	E /
NVIDIA Tesla architecture	54 109
NVIDIA V100 SM Load/store unit	102
NVIDIA V100 SM SIMD fp32 functional unit	109
NVIDIA V100 SM SIMD fp64 functional unit	109
NVIDIA V100 SM SIMD int functional unit	109

Index

	Index
NVIDIA V100 SM Tensor core unit	109
NVIDIA V100 Streaming Multiprocessor (SM)	109
NVLink	210
0	
Open Computing Language (OpenCL)	103
OpenMP	55
Р	
Page Fault	191
Parallel Algorithm	39
Parallel Program	39
Parallel Random-Access Machine (parallel RAM or PRAM)	6
Parallel tasks in parallel algorithms	41
Parallelism metrico for parallel algorithms	42
Partial Store Ordering (PSO)	232
PCAM (Partitioning, Communication, Agglomeration, Mapping)	39
Per-block Shared Memory	108
Per-thread Private Memory	108
Pinned memory	188
POSIX Threads	48
Prefetching	28
Prefix Sum	15
Priority Concurrent Write	( 021
Processor Consistency (PC)	231
Processor Stall	20 179
Froming	172
	40
Race Condition	48
Random Access Machine (RAM)	0 7
Random Concurrent write Decurring Muter (DTUDEAD MITTER DECURCTUE)	( 5 /
Recursive Muttex (PIHREAD_MOTEX_RECORSIVE)	04 225
Relaxed Melliory Release Consistency (RC)	220
release Consistency (RC)	204
S Sequential Consistency	225
Shared Address Space	220
Shared Variables	35
Simultaneous Multithreading (SMT)	30
Single Instruction Multiple Data (SIMD)	
Single Program Multiple Data (SPMD)	20 12
Single Program Multiple Data (SPMD)	31
Span metric for parallel algorithms	41
SPMD programming model	32
Standard PCIe 3.0 Link	210
Superscalar Processor	210
Switch-On-Event Multithreading	$\frac{-1}{30}$
<u> </u>	

## Index

## $\mathbf{T}$

Temporal Multithreading	30
Test-and-Set instruction	240
Test-and-Test-and-Set lock	244
Thread	47
Tiling Technique	135
Total Store Ordering (TSO)	231
U	
Un-Coalesced Access	155
Unified Memory in CUDA	190
V	
Von Neumann model with SIMD units	121
***	
W	
W Warp	110
W Warp Warp Divergence	$\begin{array}{c} 110 \\ 150 \end{array}$
W Warp Warp Divergence Weak Ordering (WO)	$110 \\ 150 \\ 234$
W Warp Warp Divergence Weak Ordering (WO) Work metric for parallel algorithms	$110 \\ 150 \\ 234 \\ 41$
W Warp Warp Divergence Weak Ordering (WO) Work metric for parallel algorithms Write Buffer	$110 \\ 150 \\ 234 \\ 41 \\ 226$
W Warp Warp Divergence Weak Ordering (WO) Work metric for parallel algorithms Write Buffer Z	$110 \\ 150 \\ 234 \\ 41 \\ 226$